

## All India Aakash Test Series for JEE (Advanced)-2024

## TEST - 2A (Paper-1) - Code-C

Test Date : 05/11/2023

## ANSWERS

## CHEMISTRY

1. (A, B, C)
2. (A, C, D)
3. (A, C, D)
4. (C, D)
5. (A, B)
6. (A, D)
7. (02)
8. (02)
9. (03)
10. (02)
11. (03)
12. (03)
13. (03)
14. (00)
15. (C)
16. (A)
17. (B)
18. (B)

## MATHEMATICS

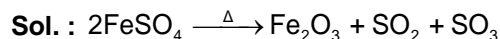
19. (C, D)
20. (A, B, C, D)
21. (B, C)
22. (B, C)
23. (A, B, D)
24. (A, C)
25. (06)
26. (02)
27. (06)
28. (01)
29. (02)
30. (04)
31. (03)
32. (05)
33. (B)
34. (D)
35. (B)
36. (B)

## PHYSICS

37. (A, C)
38. (A, C, D)
39. (B, D)
40. (A, C, D)
41. (A, D)
42. (B, C, D)
43. (00)
44. (02)
45. (12)
46. (10)
47. (02)
48. (04)
49. (03)
50. (12)
51. (B)
52. (B)
53. (C)
54. (D)

**HINTS & SOLUTIONS****PART - I (CHEMISTRY)**

1. Answer (A, B, C)

**Hint :**  $\text{FeSO}_4$  on heating gives  $\text{SO}_2$  and  $\text{SO}_3$ 

2. Answer (A, C, D)

**Hint :** Al is extracted by electrolytic reduction.**Sol. :** Cu, Hg and Pb can be extracted by self reduction process.

3. Answer (A, C, D)

**Hint :** Galena ( $\text{PbS}$ )**Sol. :** Bauxite –  $\text{Al}_2\text{O}_3 \cdot 2\text{H}_2\text{O}$ Haematite –  $\text{Fe}_2\text{O}_3$ Calamine –  $\text{ZnCO}_3$ 

4. Answer (C, D)

**Hint :** Metals which are less reactive than copper may be present as anode mud.**Sol. :** Anode mud in electrorefining of copper contains Ag and Au.

5. Answer (A, B)

**Hint :**  $\text{AgF} \rightarrow$  Soluble in water**Sol. :**  $\text{AgBr} \rightarrow$  Pale yellow $\text{AgCl} \rightarrow$  White ppt. $\text{AgI} \rightarrow$  Bright yellow

6. Answer (A, D)

**Hint :** Acidified potassium permanganate can oxidise ferrous and stannous ions.**Sol. :** In  $\text{Be}^{2+}$  and  $\text{NO}_3^-$ , central atoms are present in their respective highest oxidation states.

7. Answer (02)

**Hint :** Ni is present in +2 oxidation state**Sol. :**  $\text{Cl}^-$  is a weak field ligand and hence pairing will not take place.

8. Answer (02)

**Hint :** Complex is of type  $[\text{Ma}_3\text{b}_3]$ **Sol. :** Facial and Meridional isomers are possible for  $[\text{Ma}_3\text{b}_3]$ 

9. Answer (03)

**Hint :** Complex of type  $[\text{M}(\text{AA})_2\text{a}_2]$ **Sol. :** Cis isomer is optically active

Cis forms – two isomers

Trans form - one isomers

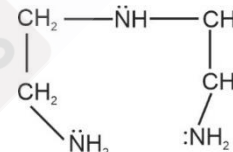
10. Answer (02)

**Hint :**  $\text{Mn}^{2+}$  is pale pink in color

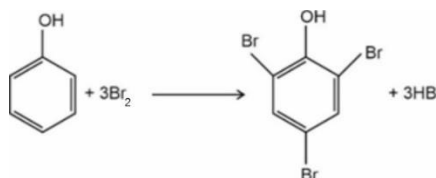
11. Answer (03)

**Hint :** Molecular formula of chromite ore is  $\text{FeCr}_2\text{O}_4$ **Sol.:** Chromite ore is  $\text{FeO} \cdot \text{Cr}_2\text{O}_3$ 

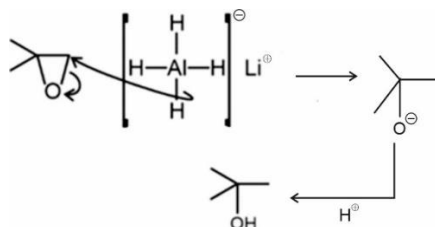
12. Answer (03)

**Hint :** Three nitrogen atoms, each having one lone pair of electrons.**Sol.:** Diethylenetriamine is

13. Answer (03)

**Hint :** White precipitate obtained is 2, 4, 6-tribromophenol**Sol.:**

14. Answer (00)

**Hint :** Tertiary butyl alcohol is obtained**Sol.:**

15. Answer (C)

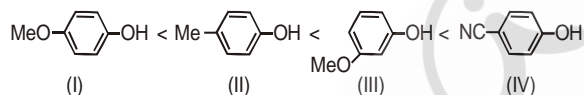
**Hint :** Acids which are stronger than carbonic acid ( $\text{H}_2\text{CO}_3$ )

**Sol. :** Only 2, 4, 6-trinitrophenol (Picric acid) will evolve  $\text{CO}_2$  gas with aqueous  $\text{NaHCO}_3$  due to high acidic nature.

16. Answer (A)

**Hint :**  $-\text{CN}$  group increases the acidity of phenol.

**Sol.:** When electronreleasing group like  $\text{MeO}-$  is present on m-position w.r.t.  $-\text{OH}$  group then it acts as  $-I$  effect group and increases the acidity.  $\text{MeO}-$  is good electron-releasing group in comparison to  $-\text{Me}$ . So, order of acidity becomes as follows



17. Answer (B)

**Hint :**  $\text{N}_2$  is highly inert gas

**Sol.:**  $\text{N}_2$  has the maximum leaving group ability

18. Answer (B)

**Hint :** Group having maximum leaving ability is least basic.

**Sol.:**  $\text{O}=\text{S}(\text{O})_2-\text{C}_4\text{F}_9$  is having maximum leaving ability.

## PART - II (MATHEMATICS)

19. Answer (C, D)

**Hint :**  $\lim_{n \rightarrow \infty} \tan\left(\frac{1}{n}\right) \ln\left(\frac{1}{n}\right) = 0 \Rightarrow f(x) = 1$

**Sol. :**  $\lim_{n \rightarrow \infty} \tan\left(\frac{1}{n}\right) \ln\left(\frac{1}{n}\right) = 0 \Rightarrow f(x) = 1$

$$\Rightarrow \int \frac{dx}{\sin^{1/3} x \cos^{1/3} x} = \frac{-3}{8} (\tan x)^{-8/3}$$

$$-\frac{3}{2} (\tan x)^{-\frac{2}{3}} + C$$

$$\therefore g\left(\frac{\pi}{6}\right) = -\frac{21}{8} \times 3^{\frac{1}{3}}$$

$$\Rightarrow C = 0$$

$$g\left(\frac{\pi}{4}\right) = -\frac{15}{8}$$

20. Answer (A, B, C, D)

**Hint :**

$$f(x) = \int_{-2}^x |t+1| dt = -\int_{-2}^{-1} (t+1) dt + \int_{-1}^x (t+1) dt = \frac{1}{2} + \left(\frac{t^2}{2} + t\right)_{-1}^x$$

$$= \frac{x^2}{2} + x + 1 \text{ for } x \geq -1$$

**Sol. :**

$$f(x) = \int_{-2}^x |t+1| dt = -\int_{-2}^{-1} (t+1) dt + \int_{-1}^x (t+1) dt = \frac{1}{2} + \left(\frac{t^2}{2} + t\right)_{-1}^x$$

$$= \frac{x^2}{2} + x + 1 \text{ for } x \geq -1$$

$f(x)$  is a quadratic polynomial.

Therefore,  $f(x)$  is continuous as well as differentiable in  $(-1, 1)$ .

Also  $f(x)$  is continuous as well as differentiable in  $[-1, 1]$ .

21. Answer (B, C)

**Hint :**  $f(x) = x^3 - x^2 + 100x + 1001$

$$f'(x) = 3x^2 - 2x + 100 > 0 \quad \forall x \in \mathbb{R}$$

**Sol. :**  $f(x) = x^3 - x^2 + 100x + 1001$

$$f'(x) = 3x^2 - 2x + 100 > 0 \quad \forall x \in \mathbb{R}$$

Therefore,  $f(x)$  is increasing (strictly).

$$\text{Therefore, } f\left(\frac{1}{1999}\right) > f\left(\frac{1}{2000}\right)$$

$$\Rightarrow f(x+1) > f(x-1)$$

22. Answer (B, C)

**Hint :**  $f(-x) = -f(x)$

**Sol. :**  $f(x) = ax^3 + bx^2 + cx + d$

Now,  $f(x)$  is odd. Therefore,

$$f(-x) = -f(x)$$

$$\Rightarrow -ax^3 - bx^2 - cx - d = ax^3 + bx^2 - cx + d$$

It gives  $b = 0 = d$

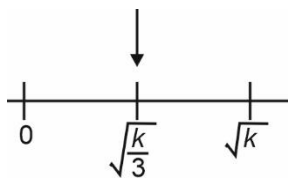
$$f(x) = ax^3 + cx = x(ax^2 + c)$$

$$\text{Therefore, } f'(x) = 3ax^2 + c = 0$$

Only when  $x^2 = -\frac{c}{3a}$  is positive

Therefore,  $c$  and  $a$  are of different signs.

$$\text{Let } -\frac{c}{a} = k.$$



So, non-zero root of  $f(x)$  is  $\pm \sqrt{k}$ .

Also  $\pm \sqrt{\frac{k}{3}}$  is closer to origin than  $\pm \sqrt{k}$

23. Answer (A, B, D)

$$\text{Hint : } F(x) = \int \frac{1}{4 - 3\cos^2 x + 5\sin^2 x} dx$$

$$= \int \frac{1}{9 - 8\cos^2 x} dx$$

$$\text{Sol. : } F(x) = \int \frac{1}{4 - 3\cos^2 x + 5\sin^2 x} dx$$

$$= \int \frac{1}{9 - 8\cos^2 x} dx$$

$$= \int \frac{\sec^2 x}{9\sec^2 x - 8} dx = \int \frac{\sec^2 x}{1 + 9\tan^2 x} dx$$

$$= \frac{1}{3} \tan^{-1}(3\tan x) + c$$

$$\Rightarrow g(x) = 3 \tan x$$

$$\text{Therefore, } g\left(\frac{\pi}{4}\right) = 3$$

$$\text{And } g'\left(\frac{\pi}{3}\right) = 12$$

24. Answer (A, C)

$$\text{Hint : } I_n = \left( \frac{e^{-x} (\sin x)^n}{-1} \right)_0^x + n \int_0^x (\sin x)^{n-1} \cos x e^{-x} dx$$

$$= \int_0^x \left( -(\sin x)^n + (n-1)(1 - \sin^2 x)(\sin x) \right)^{n-2} e^{-x} dx$$

$$= \frac{n(n-1)}{n^2 + 1} I_{n-2}$$

$$\text{Sol. : } I_n = \left( \frac{e^{-x} (\sin x)^n}{-1} \right)_0^x + n \int_0^x (\sin x)^{n-1} \cos x e^{-x} dx$$

$$= \int_0^x \left( -(\sin x)^n + (n-1)(1 - \sin^2 x)(\sin x) \right)^{n-2} e^{-x} dx$$

$$= \frac{n(n-1)}{n^2 + 1} I_{n-2}$$

$$\text{Hence, } \frac{I_{10}}{I_8} = \frac{90}{101}$$

25. Answer (06)

**Hint :**  $f(x)$  can have point of inflection at points where  $f''(x) = 0$ .

**Sol. :** We have

$$f(x) = x^3 - 9x^2 + 200x - 10$$

$$\text{That is, } f'(x) = 3x^2 - 18x + 200 > 0 \quad \forall x \in \mathbb{R}$$

$$f''(x) = 6x - 18$$

$$\text{for point of inflection, } f'(x) = 0$$

$$x = 3$$

$$\Rightarrow x_1 = 3$$

$$\therefore f'(x) = 3x^2 - 18x + 200$$

$$f''(x) = 6x - 18,$$

$$f'''(x) = 6$$

$$\Rightarrow x = x_2 = 3 \text{ is point of local minima for } f(x)$$

26. Answer (02)

**Hint :**  $x = -1$  and  $x = \frac{1}{3}$  are roots of  $f'(x) = 0$ .

**Sol. :**  $x = -1$  and  $x = \frac{1}{3}$  are roots of  $f'(x) = 0$ .

$$\begin{aligned}\text{Therefore, } f'(x) &= a(3x - 1)(x + 1) \\ &= a(3x^2 + 2x - 1)\end{aligned}$$

$$\Rightarrow f(x) = a(x^3 + x^2 - x + b)$$

$$f(-2) = 0$$

$$\Rightarrow b = 2$$

$$\Rightarrow f(x) = a(x^3 + x^2 - x + 2)$$

$$\int_{-1}^1 f(x) dx = \frac{14}{3}$$

$$\Rightarrow \int_{-1}^1 a(x^3 + x^2 - x + 2) dx = \frac{14}{3}$$

$$\Rightarrow a \int_{-1}^1 x^2 + 2 = \frac{14}{3}$$

$$\Rightarrow 2a \left( \frac{1}{3} + 2 \right) = \frac{14}{3}$$

$$\Rightarrow a = 1$$

$$\text{Therefore, } f(x) = x^3 + x^2 - x + 2$$

27. Answer (06)

$$\text{Hint : } g(x) = \frac{d}{dx}(f(x)f'(x))$$

$$\text{Sol. : } g(x) = \frac{d}{dx}(f(x)f'(x))$$

To get the zero of  $g(x)$ , we take function

$$h(x) = f(x)f'(x)$$

Between any two roots of  $h(x)$ , there lies at least one root of  $h'(x) = 0$ . That is,

$$g(x) = 0$$

$$\text{Now, } h(x) = 0 \text{ and } f(x) = 0$$

$$\text{Or } f'(x) = 0$$

As  $f(x) = 0$  has 4 minimum solutions and  $f'(x) = 0$  has minimum 3 solutions,  $h(x) = 0$  has minimum 7 solutions and  $h'(x) = g(x) = 0$  has minimum 6 solutions.

28. Answer (01)

$$\text{Hint : } f'(x) = e^{-(x^2+1)^2} \cdot 2x - e^{-(x^2)^2} \cdot 2x$$

$$\text{Sol. : } f'(x) = e^{-(x^2+1)^2},$$

$$e^{-(x^2+1)^2} \cdot 2x - e^{-(x^2)^2} \cdot 2x = 2xe^{-(x^4+2x^2+1)} (1 - e^{2x^2+1})$$

$$\Rightarrow f'(x) > 0, \forall x \in (-\infty, 0)$$

29. Answer (02)

Hint :

$$\int_0^\pi f^{-1}(x) dx = \int_{f^{-1}(0)}^{f^{-1}(\pi)} tf'(t) dt = [tf(t)]_{f^{-1}(0)}^{f^{-1}(\pi)} - \int_{f^{-1}(0)}^{f^{-1}(\pi)} f(t) dt$$

Sol. :

$$\int_0^\pi f^{-1}(x) dx = \int_{f^{-1}(0)}^{f^{-1}(\pi)} tf'(t) dt = [tf(t)]_{f^{-1}(0)}^{f^{-1}(\pi)} - \int_{f^{-1}(0)}^{f^{-1}(\pi)} f(t) dt$$

$$f^{-1}(0) = 0$$

$$f^{-1}(\pi) = \pi$$

$$= \pi^2 - \int_0^\pi (t + \sin t) dt$$

$$= \pi^2 - \left( \frac{t^2}{2} - \cos t \right)_0^\pi = \pi^2 - \frac{\pi^2}{2} - 2 = \frac{\pi^2}{2} - 2$$

Therefore,  $k = 2$ .

30. Answer (04)

$$\text{Hint : } f(x) = [x] + |1 - x|, -1 \leq x \leq 3$$

$$\text{Sol. : } f(x) = [x] + |1 - x|, -1 \leq x \leq 3$$

$$= -x \text{ if } -1 \leq x < 0$$

$$= 1 - x \text{ if } 0 \leq x < 1 = x \text{ if } 1 \leq x < 2$$

$$= x + 1 \text{ if } 2 \leq x < 3$$

$$= 5 \text{ if } x = 3$$

Clearly  $f$  is not continuous at  $x = 0, 1, 2$  and  $3$

31. Answer (03)

$$\text{Hint : } f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$\text{Sol. : } f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$\therefore f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$= \lim_{h \rightarrow 0} \frac{f\left(\frac{3x+3h}{3}\right) - f\left(\frac{3x+0}{3}\right)}{h}$$

$$= \lim_{h \rightarrow \infty} \frac{2 + f(3x) + f(3h) - 2 + f(3x) + f(0)}{3h} = \lim_{h \rightarrow \infty} \frac{f(3h) - f(0)}{3h} = f'(0)$$

$$\Rightarrow f'(2) = f'(0) = 2$$

$$(\because f'(2) = 2)$$

$$\Rightarrow f'(x) = 2 \Rightarrow f(x) = 2x + c$$

Put  $x = y = 0$  in

$$f\left(\frac{x+y}{3}\right) = \frac{2 + f(x) + f(y)}{3}$$

$$\Rightarrow f(0) = 2$$

Now, from equation (i),  $f(0) = 0 + c = 2$

$$\therefore c = 2$$

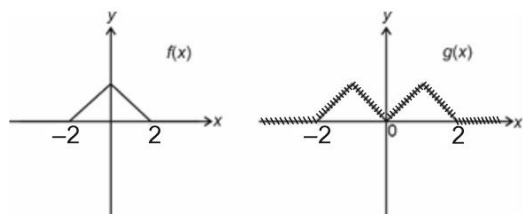
From equation (i),  $f(x) = 2x + 2$

So, function  $g(x) = |2x| - 1$ , hence the points of non differentiability of  $g(x)$  are  $x = \pm(1/2), 0$ .

32. Answer (05)

**Hint :** Plot the graph

**Sol. :**



33. Answer (B)

**Hint :** On differentiating a polynomial of  $n^{\text{th}}$  degree, we get another polynomial of  $(n - 1)$  degrees.

**Sol.:** On differentiating a polynomial of  $n^{\text{th}}$  degree, we get another polynomial of  $(n - 1)$  degrees.

So,

$$f(x) = \{f'(x)\}^2 \Rightarrow n = 2(n - 1) \Rightarrow n = 2$$

34. Answer (D)

**Hint :** Let  $f(x) = ax^2 + bx + c$

$$\Rightarrow f'(0) = b > 0$$

**Sol. :** Let  $f(x) = ax^2 + bx + c$

$$\Rightarrow f'(0) = b > 0$$

$$\text{Also, } f(x) = (f'(x))^2$$

$$\Rightarrow ax^2 + bx + c = 4a^2x^2 + 4abx + b^2 \forall x$$

Thus,  $a = 4a^2$ ,  $b = 4ab$  and  $c = b^2$

From which, we get  $a = \frac{1}{4}$ , since  $(b \neq 0)$

Again,

$$\int_0^1 f(x) dx = \frac{19}{12}$$

$$\Rightarrow \frac{a}{3} + \frac{b}{2} + c = \frac{19}{12}$$

$$\text{Therefore, } \frac{b}{2} + b^2 = \frac{3}{2}$$

$$\Rightarrow b = 1$$

(since,  $b > 0$ ) and so  $c = 1$

Therefore,

$$f'(0) = b = 1$$

35. Answer (B)

**Hint :** Putting  $x = 9$ ,  $y = 0$  in the given equation of curve, we have

$$0 = 3a + 9b - \frac{1}{2} = \frac{a}{2 \times 3} + b$$

**Sol. :** Putting  $x = 9$ ,  $y = 0$  in the given equation of curve, we have

$$0 = 3a + 9b - \frac{1}{2} = \frac{a}{2 \times 3} + b$$

$$\Rightarrow a = -3b \quad \dots(1)$$

$$\frac{dy}{dx} = \frac{a}{2\sqrt{x}} + b$$

$$\left. \frac{dy}{dx} \right|_{(9,0)} = \frac{a}{6} + b = -\frac{1}{2} \quad \dots(2)$$

Using Eqs. (1) and (2), we get

$$b = -1 \text{ and } a = 3$$

Therefore,

$$y = 3\sqrt{x} - x$$

Point (1, 2) lies on curve as well as it is point of intersection of family of lines.

$$\frac{dy}{dx} = \frac{3}{2\sqrt{x}} - 1$$

$$\frac{dy}{dx} \text{ at } (1, 2) \text{ is } \frac{1}{2}$$

$$y - 2 = \frac{1}{2}(x - 1)$$

$$\Rightarrow x - 2y + 3 = 0$$

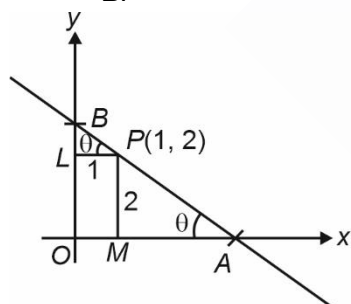
36. Answer (B)

**Hint :**  $AB = AP + BP = 2\operatorname{cosec}\theta + \sec\theta$

$$\text{Sol. : } \sin\theta = \frac{2}{PA}$$

$$PA = 2 \operatorname{cosec}\theta$$

$$\cos\theta = \frac{1}{BP}$$



$$BP = \sec\theta$$

$$AB = AP + BP = 2\operatorname{cosec}\theta + \sec\theta$$

$$\text{Therefore, minimum value of } AB = (2^{2/3} + 1)^{3/2}$$

### PART - III (PHYSICS)

37. Answer (A, C)

**Hint :** Apply lens maker's formula.

$$\text{Sol. } \frac{1}{f} = (1.5 - 1) \left( \frac{2}{30} \right) = \frac{1}{30}$$

$$\therefore f = 30 \text{ cm}$$

Image will be at  $2f$  and is real.

38. Answer (A, C, D)

**Hint :** If  $\theta = 90^\circ$ , three images are formed.

**Sol. :** If  $\theta = 90^\circ$ , three images are formed.

39. Answer (B, D)

**Hint :** Before  $t = 0$ ,  $i = \frac{V}{R}$

Just after  $t = 0$ ,  $i = \frac{V}{R}$

**Sol. :** Before  $t = 0$ ,  $i = \frac{V}{R}$

40. Answer (A, C, D)

**Hint :**  $\Delta V_{PQ} = Blv$

**Sol. :**  $\Delta V = Blv$ ,  $R_{eq} = 2R$

$$i_{PQ} = \frac{Blv}{2R}$$

$$i_{R_1} = i_{R_2} = \frac{Blv}{4R}$$

41. Answer (A, D)

**Hint :**  $I_{rms} = \sqrt{\frac{T_0 \int_0^{T_0} I_0^2 dt}{T_0}}$  and  $I_{avg} = \frac{\int I dt}{\int dt}$

$$\text{Sol. : } I_{rms} = \sqrt{\frac{T_0 \int_0^{T_0} I_0^2 dt}{T_0}} = I_0$$

$I_{avg} = I_0$  for half cycle as current remains constant.

42. Answer (B, C, D)

**Hint :** Circuit is in resonance.

**Sol. :**  $\Delta V$  across LC combination = 0

Circuit is in resonance.

43. Answer (00)

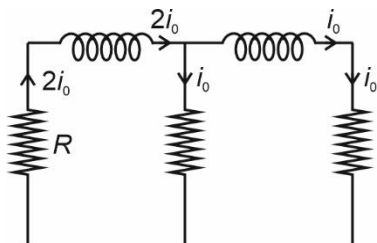
**Hint :** Find direction of induced electric field on OA.

**Solution :** There is no emf induced in BA and CD, since induced electric field is normal to AB and CD.

44. Answer (02)

**Hint :** Use the behaviour of the inductor concept.

**Solution :** After S is opened, current through inductor wouldn't change suddenly.



$$\begin{aligned}\text{Required sum} &= 2i_0 + i_0 + i_0 \\ &= 4i_0\end{aligned}$$

45. Answer (12)

**Hint :** Find equivalent focal length of the system.

$$\text{Solution : } \frac{1}{F} = 2\left(\frac{1}{f_{\text{lens}}}\right) + \left(\frac{1}{f_m}\right)$$

$$= 2\left[(1.5 - 1)\left(\frac{1}{12} - \frac{1}{\infty}\right)\right] + \left(\frac{1}{\infty}\right)$$

$$\Rightarrow f = 12 \text{ cm}$$

46. Answer (10)

**Hint :** Apply lens maker's formula

$$\text{Sol. : } R = 10 \text{ cm}$$

$$-\frac{1}{20} = \left[ \frac{1.5}{1 + 0.1t} - 1 \right] \frac{2}{10}$$

$$\frac{3}{4} = \frac{1.5}{1 + 0.1t}$$

$$t = 10 \text{ s}$$

47. Answer (02)

$$\text{Hint : } \varepsilon = -L \frac{di}{dt}$$

**Sol. :**

$$\varepsilon = -L \frac{di}{dt} = Bv\ell$$

$$iB\ell = -\frac{mdv}{dt}$$

$$B\ell \frac{di}{dt} = m \frac{d^2v}{dt^2}$$

$$\frac{B^2 \ell^2 v}{L} = -m \frac{d^2v}{dt^2}$$

$$m \frac{d^2v}{dt^2} + \frac{B^2 \ell^2}{L} v = 0$$

$$v = v_0 \cos(\omega t)$$

$$\omega = \frac{B\ell}{\sqrt{mL}}$$

$$v = v_0 \cos \left[ \frac{B\ell}{\sqrt{mL}} \times \frac{\pi \sqrt{mL}}{4B\ell} \right]$$

$$= \frac{v_0}{\sqrt{2}}$$

$$\Rightarrow \frac{1}{2} Li^2 = \frac{1}{2} m \left[ v_0^2 - \frac{v_0^2}{2} \right]$$

$$\Rightarrow i = \sqrt{\frac{mv_0^2}{2L}}$$

48. Answer (04)

$$\text{Hint : } \mu_1 \sin i = \mu_2 \sin r$$

**Sol. :**

$$\delta = 2i - 2r + \pi - 2r$$

$$= [\pi + 2i - 4r]$$

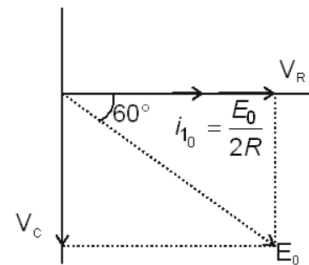
$$\frac{\sin i}{\sin r} = \sqrt{3}, \delta \text{ is minimum at } \theta = \sin^{-1}\left(\frac{1}{3}\right)$$

49. Answer (03)

**Hint :** Draw phasor diagram

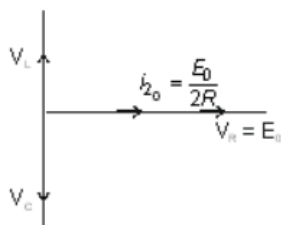
**Sol. :**

For branch containing R & C

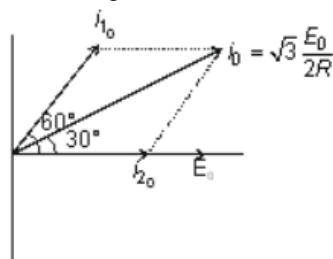


For branch containing L, C & R





Combining both

 $i_0$  leads  $E_0$  by  $\pi/6$ 

$$z = \frac{E_0}{i_0} = \frac{2R}{\sqrt{3}}$$

$$i_1 = \frac{E_0}{2R} \sin\left(\omega t + \frac{\pi}{3}\right)$$

$$i_2 = \frac{E_0}{2R} \sin \omega t$$

50. Answer (12)

$$\text{Hint : } C = \frac{E_0}{B}$$

$$\begin{aligned} \text{Solution : } E_0 &= CB_0 = (3 \times 10^8) (4 \times 10^{-6}) \text{ V/m} \\ &= 1200 \text{ V/m} \end{aligned}$$

51. Answer (B)

52. Answer (B)

**Hints and Solutions of Q. Nos. 51 & 52****Hint:**

In LC oscillation, total energy is constant.

**Solution:**

$$V_L = 0$$

$$V_C = V_{2C} = V_0$$

$$\frac{1}{2} L I_1^2 + \frac{1}{2} (3C) V_0^2 = \frac{1}{2} (2C) 4V_0^2 + \frac{1}{2} C V_0^2$$

$$I_1 = V_0 \sqrt{\frac{6C}{L}}$$

$$t_0 = \frac{T}{4} = \frac{1}{4} \times \frac{2\pi}{\omega}$$

$$= \frac{\pi}{2} \sqrt{\frac{2LC}{3}}$$

53. Answer (C)

**Hint :** Use spherical refraction concept**Sol., :**

$$\frac{2}{V} + \frac{1}{x} = \frac{2-1}{R}$$

$$\left[ \frac{2}{V} = \frac{1}{R} - \frac{1}{x} \right]$$

54. Answer (D)

**Hint :** Use spherical refraction concept**Sol. :**  $V = +4R$ 

Image is inverted and magnified

$$\text{First refraction : } \frac{2}{v} - \frac{1}{-2R} = \frac{2-1}{R}$$

$$\Rightarrow v = 4R$$

$$\Rightarrow m_1 = \frac{\frac{v}{\mu_2}}{\frac{u}{\mu_1}} = -1$$

For second refraction,

$$m_2 = +1$$

$$\Rightarrow m_{\text{net}} = -1$$

 $\Rightarrow$  Inverted and of same size.