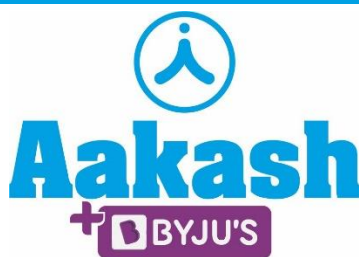


30/01/2024

Morning



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## Answers & Solutions

Time : 3 hrs.

M.M. : 300

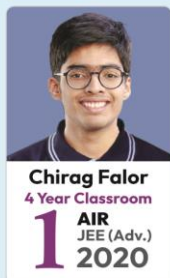
for

## JEE (Main)-2024 (Online) Phase-1

(Mathematics, Physics and Chemistry)

### IMPORTANT INSTRUCTIONS:

- (1) The test is of **3 hours** duration.
- (2) This test paper consists of 90 questions. Each subject (MPC) has 30 questions. The maximum marks are 300.
- (3) This question paper contains **Three Parts**. **Part-A** is Mathematics, **Part-B** is Physics and **Part-C** is Chemistry. Each part has only two sections: **Section-A** and **Section-B**.
- (4) **Section - A** : Attempt all questions.
- (5) **Section - B** : Attempt any 05 questions out of 10 Questions.
- (6) **Section - A (01 – 20)** contains 20 multiple choice questions which have **only one correct answer**. Each question carries **+4 marks** for correct answer and **–1 mark** for wrong answer.
- (7) **Section - B (21 – 30)** contains 10 **Numerical value** based questions. The answer to each question should be rounded off to the **nearest integer**. Each question carries **+4 marks** for correct answer and **–1 mark** for wrong answer.



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**MATHEMATICS**

**SECTION - A**

**Multiple Choice Questions:** This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

**Choose the correct answer:**

1. If  $f(x) = \begin{vmatrix} 2\cos^4 x & 2\sin^4 x & 3 + \sin^2 2x \\ 3 + 2\cos^4 x & 2\sin^4 x & \sin^2 2x \\ 2\cos^4 x & 3 + 2\sin^4 x & \sin^2 2x \end{vmatrix}$ , then

$\frac{1}{5} f'(0)$  is equal to:

- (1) 1  
(2) 2  
(3) 6  
(4) 0

**Answer (4)**

**Sol.**

$$f(x) = \begin{vmatrix} 2\cos^4 x & 2\sin^4 x & 3 + \sin^2 2x \\ 3 + 2\cos^4 x & 2\sin^4 x & \sin^2 2x \\ 2\cos^4 x & 3 + 2\sin^4 x & \sin^2 2x \end{vmatrix}$$

$$f'(x) = \begin{vmatrix} 8\cos^3 x(-\sin x) & 2\sin^4 x & 3 + \sin^2 2x \\ 8\cos^3 x(-\sin x) & 2\sin^4 x & \sin^2 2x \\ 8\cos^3 x(-\sin x) & 3 + 2\sin^4 x & \sin^2 2x \end{vmatrix}$$

$$+ \begin{vmatrix} 2\cos^4 x & 8\sin^3 x \cos x & 3 + \sin^2 2x \\ 3 + 2\cos^4 x & 8\sin^3 x \cos x & \sin^2 2x \\ 2\cos^4 x & 8\sin^3 x \cos x & \sin^2 2x \end{vmatrix}$$

$$+ \begin{vmatrix} 2\cos^4 x & 2\sin^4 x & 4\sin 2x \cos 2x \\ 3 + 2\cos^4 x & 2\sin^4 x & 4\sin 2x \cos 2x \\ 2\cos^4 x & 3 + 2\sin^4 x & 4\sin 2x \cos 2x \end{vmatrix}$$

$$f'(0) = \begin{vmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{vmatrix} + \begin{vmatrix} 2 & 0 & 0 \\ 5 & 0 & 0 \\ 2 & 0 & 0 \end{vmatrix} + \begin{vmatrix} 2 & 0 & 0 \\ 5 & 0 & 0 \\ 2 & 0 & 0 \end{vmatrix}$$

$$f(0) = 0$$

$$\therefore \frac{1}{5} f'(0) = 0$$

2. Let  $f: \left[-\frac{\pi}{2}, \frac{\pi}{2}\right] \rightarrow \mathbb{R}$  be a differentiable function

such that  $f(0) = \frac{1}{2}$ . If the  $\lim_{x \rightarrow 0} \frac{x \int_0^x f(t) dt}{e^{x^2} - 1} = \alpha$ , then

$8\alpha^2$  is equal to :

- (1) 1 (2) 16  
(3) 4 (4) 2

**Answer (4)**

**Sol.**  $\lim_{x \rightarrow 0} \frac{x \int_0^x f(t) dt}{e^{x^2} - 1} = \alpha$  and  $f(0) = \frac{1}{2}$

$$\begin{aligned} & \lim_{x \rightarrow 0} \frac{\int_0^x f(t) dt + x f(x)}{e^{x^2} (2x)} \\ &= \lim_{x \rightarrow 0} \frac{\int_0^x f(t) dt}{e^{x^2} (2x)} + \lim_{x \rightarrow 0} \frac{f(x)}{e^{x^2} (2)} \\ &= \lim_{x \rightarrow 0} \frac{f(x)}{2(e^{x^2} + x e^{x^2} (2x))} + \frac{1}{4} \\ &= \frac{1}{2} \end{aligned}$$

$$\therefore \alpha = \frac{1}{2}$$

$$\therefore 8\alpha^2 = 8 \times \frac{1}{4} = 2$$



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3. If  $2\sin^3x + \sin 2x \cos x + 4\sin x - 4 = 0$  has exactly 3 solutions in the interval  $\left[0, \frac{n\pi}{2}\right]$ ,  $n \in \mathbb{N}$ , then the roots of the equation  $x^2 + nx + (n-3) = 0$  belong to:

- (1)  $(-\infty, 0)$  (2)  $\mathbb{Z}$   
 (3)  $\left(-\frac{\sqrt{17}}{2}, \frac{\sqrt{17}}{2}\right)$  (4)  $(0, \infty)$

**Answer (1)**

**Sol.**  $2\sin^3x + \sin 2x \cos x + 4\sin x - 4 = 0$

$$2\sin^3x + 2\sin x \cos^2x + 4\sin x - 4 = 0$$

$$\Rightarrow \sin^3x + \sin x (1 - \sin^2x) + 2\sin x - 2 = 0$$

$$\Rightarrow \sin^3x + \sin x - \sin^3x + 2\sin x - 2 = 0$$

$$\Rightarrow 3\sin x - 2 = 0$$

$$\Rightarrow \sin x = \frac{2}{3}$$

$\therefore$  It has exactly three solution in the interval

$$\left[0, \frac{n\pi}{2}\right], n \in \mathbb{N}$$

$$\Rightarrow n = 9$$

$$\Rightarrow x^2 + 9x + 6 = 0$$

$$\Rightarrow x = \frac{-9 \pm \sqrt{81-24}}{2}$$

$$\Rightarrow x = \frac{-9 \pm \sqrt{57}}{2}$$

$$\Rightarrow \text{Roots belongs in the interval } (-\infty, 0)$$

4. If the domain of the function

$$f(x) = \cos^{-1}\left(\frac{2-|x|}{4}\right) + \{\log_e\{3-x\}\}^{-1} \text{ is } [-\alpha, \beta) -$$

$\{\gamma\}$ , then  $\alpha + \beta + \gamma$  is equal to

- (1) 8 (2) 12  
 (3) 9 (4) 11

**Answer (4)**

**Sol.**  $f(x) = \cos^{-1}\left(\frac{2-|x|}{4}\right) + \{\log_e(3-x)\}^{-1}$

$$-1 \leq \frac{2-|x|}{4} \leq 1$$

$$\Rightarrow -4 \leq 2-|x| \leq 4$$

$$\Rightarrow -4 \leq |x| - 2 \leq 4$$

$$\Rightarrow -2 \leq |x| \leq 6$$

$$|x| \leq 6$$

$$\Rightarrow x \in [-6, 6] \quad \dots(1)$$

$$\text{also, } 3-x \neq 1$$

$$x \neq 2 \quad \dots(2)$$

$$\text{and } 3-x > 0$$

$$\Rightarrow x < 3 \quad \dots(3)$$

From (1), (2) and (3)

$$\Rightarrow x \in [-6, 3) - \{2\}$$

$$\Rightarrow \alpha = 6, \beta = 3, \gamma = 2$$

$$\alpha + \beta + \gamma = 6 + 3 + 2 = 11$$

So, option (4) is correct

5. Let M denote the median of the following frequency distribution

Class	0-4	4-8	8-12	12-16	16-20
Frequency	3	9	10	8	6

Then 20M is equal to:

- (1) 52 (2) 104  
 (3) 208 (4) 416

**Answer (3)**

**Sol.**

$x_i$	$f_i$	$C.f$
0-4	3	3
4-8	9	12
8-12	10	22
12-16	8	30
16-20	6	36



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$$N = \sum f_i = 36$$

$$\left(\frac{N}{2}\right) = \frac{36}{2} = 18$$

So, we have median lies in the class 8-12

$$\therefore h = 8, f = 10, h = 4, C.f = 12$$

Here, we apply formula

$$M = l_1 + \frac{\frac{N}{2} - C.f}{f} \times h$$

$$= 8 + \frac{18 - 12}{10} \times 4$$

$$= 8 + \frac{12}{5} = \frac{52}{5}$$

$$\therefore 20M = 4 \times 52$$

$$= 208$$

6. If the circles  $(x+1)^2 + (y+2)^2 = r^2$  and  $x^2 + y^2 - 4x - 4y + 4 = 0$  intersect at exactly two distinct points, then

- (1)  $\frac{1}{2} < r < 7$   
(2)  $3 < r < 7$   
(3)  $5 < r < 9$   
(4)  $0 < r < 7$

**Answer (2)**

**Sol.**  $\therefore$  Circles intersect at two distinct points,

$$\Rightarrow |r_1 - r_2| < C_1 C_2 < r_1 + r_2$$

$$\Rightarrow |r - 2| < \sqrt{9+16} < r + 2$$

$$\Rightarrow |r - 2| < 5 \text{ and } r + 2 > 5$$

$$\therefore -5 < r - 2 < 5 \text{ and } r > 3$$

$$\Rightarrow -3 < r < 7 \text{ and } r > 3$$

$$\therefore 3 < r < 7$$

7. Two integers  $x$  and  $y$  are chosen with replacement from the set  $\{0, 1, 2, 3, \dots, 10\}$ . Then the probability that  $|x - y| > 5$ , is:

- (1)  $\frac{62}{121}$  (2)  $\frac{60}{121}$   
(3)  $\frac{30}{121}$  (4)  $\frac{31}{121}$

**Answer (3)**

**Sol.** If  $x = 0, y = 6, 7, 8, 9, 10$

If  $x = 1, y = 7, 8, 9, 10$

If  $x = 2, y = 8, 9, 10$

If  $x = 3, y = 9, 10$

If  $x = 4, y = 10$

If  $x = 5, y = \text{no possible value}$

$$\text{Total possible ways} = (5 + 4 + 3 + 2 + 1) \times 2$$

$$= 30$$

$$\text{Required probability} = \frac{30}{11 \times 11} = \frac{30}{121}$$

8. If the length of the minor axis of an ellipse is equal to half of the distance between the foci, then the eccentricity of the ellipse is:

- (1)  $\frac{1}{\sqrt{3}}$  (2)  $\frac{2}{\sqrt{5}}$   
(3)  $\frac{\sqrt{3}}{2}$  (4)  $\frac{\sqrt{5}}{3}$

**Answer (2)**

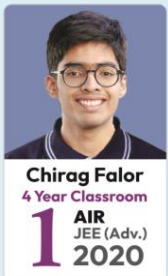
**Sol.**  $\therefore ae = 2b$

$$\therefore \frac{4b^2}{a^2} = e^2$$

$$\text{or } 4(1 - e^2) = e^2$$

$$\therefore 4 = 5e^2$$

$$\Rightarrow e = \frac{2}{\sqrt{5}}$$



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9. Let  $A(2, 3, 5)$  and  $C(-3, 4, -2)$  be opposite vertices of a parallelogram  $ABCD$ . If the diagonal  $\overrightarrow{BD} = \hat{i} + 2\hat{j} + 3\hat{k}$ , then the area of the parallelogram is equal to:

- (1)  $\frac{1}{2}\sqrt{306}$   
 (2)  $\frac{1}{2}\sqrt{474}$   
 (3)  $\frac{1}{2}\sqrt{586}$   
 (4)  $\frac{1}{2}\sqrt{410}$

**Answer (2)**

**Sol.** Given opposite vertices of parallelogram.

$$A(2, 3, 5) \text{ and } C(-3, 4, -2)$$

$$\therefore \overrightarrow{CA}(d_1) = 5\hat{i} - \hat{j} + 7\hat{k}$$

$$\text{Given } \overrightarrow{BD}(d_2) = \hat{i} + 2\hat{j} + 3\hat{k}$$

$\therefore$  As area of parallelogram

$$= \frac{1}{2} |\vec{d}_1 \times \vec{d}_2|$$

$$\text{Now, } \vec{d}_1 \times \vec{d}_2 = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 5 & -1 & 7 \\ 1 & 2 & 3 \end{vmatrix}$$

$$= \hat{i}(-3-14) - \hat{j}(15-7) + \hat{k}(10+1)$$

$$= -17\hat{i} - 8\hat{j} + 11\hat{k}$$

$$|\vec{d}_1 \times \vec{d}_2| = \sqrt{(-17)^2 + (-8)^2 + (11)^2}$$

$$= \sqrt{289 + 64 + 121}$$

$$= \sqrt{474}$$

$$\therefore \frac{1}{2} |\vec{d}_1 \times \vec{d}_2| = \frac{1}{2} \sqrt{474}$$

10. The value of  $\lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{n^3}{(n^2 + k^2)(n^2 + 3k^2)}$  is:

- (1)  $\frac{\pi}{8(2\sqrt{3} + 3)}$  (2)  $\frac{(2\sqrt{3} + 3)\pi}{24}$   
 (3)  $\frac{13\pi}{8(4\sqrt{3} + 3)}$  (4)  $\frac{13(2\sqrt{3} - 3)\pi}{8}$

**Answer (3)**

$$\text{Sol. } \lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{n^3}{n^4 \left(1 + \frac{k^2}{n^2}\right) \left(1 + \frac{3k^2}{n^2}\right)}$$

$$\lim_{n \rightarrow \infty} \frac{1}{n} \sum_{k=1}^n \frac{1}{\left(1 + \frac{k^2}{n^2}\right) \left(1 + \frac{3k^2}{n^2}\right)}$$

$$= \int_0^1 \frac{dx}{3(1+x^2) \left(\frac{1}{3} + x^2\right)}$$

$$= \frac{1}{3} \times \frac{3}{2} \int_0^1 \frac{1(x^2-1) - \left(x^2 + \frac{1}{3}\right)}{(1+x^2) \left(\frac{1}{3} + x^2\right)} dx$$

$$= \frac{1}{2} \int_0^1 \left[ \frac{1}{x^2 + \left(\frac{1}{\sqrt{3}}\right)^2} - \frac{1}{1+x^2} \right] dx$$

$$= \frac{1}{2} \left[ \sqrt{3} \tan^{-1}(\sqrt{3}x) \right]_0^1 - \frac{1}{2} \left[ \tan^{-1} x \right]_0^1$$

$$= \frac{\sqrt{3}}{2} \left( \frac{\pi}{3} \right) - \frac{1}{2} \left( \frac{\pi}{4} \right)$$

$$= \frac{\pi}{2\sqrt{3}} - \frac{\pi}{8}$$

$$= \frac{\pi}{2} \left( \frac{1}{\sqrt{3}} - \frac{1}{4} \right)$$



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$$= \frac{\pi}{2} \left( \frac{4-\sqrt{3}}{4\sqrt{3}} \right) \left( \frac{4+\sqrt{3}}{4+\sqrt{3}} \right)$$

$$= \frac{\pi}{2} \left( \frac{16-3}{4\sqrt{3}(4+\sqrt{3})} \right)$$

$$= \frac{13\pi}{8(4\sqrt{3}+3)}$$

Option (3) is correct

11. Let  $S_n$  denote the sum of first  $n$  terms of an arithmetic progression. If  $S_{20} = 790$  and  $S_{10} = 145$ , then  $S_{14} - S_5$  is :

- (1) 410 (2) 390  
(3) 405 (4) 395

**Answer (4)**

**Sol.** Given,  $S_{20} = 790$  and  $S_{10} = 145$

$$S_{20} = 790 = 10[2a + (19)d]$$

$$\Rightarrow 79 = 2a + 19d \quad \dots(1)$$

$$\text{and } S_{10} = 145 = 5[2a + 9d]$$

$$\Rightarrow 29 = 2a + 9d \quad \dots(2)$$

Subtract equation (2) from equation (1)

$$\Rightarrow 50 = 10d$$

$$d = 5$$

Put it in equation (2)

$$29 = 2a + 45$$

$$= -16 = 2a$$

$$\Rightarrow a = -8$$

$$S_{15} = \frac{15}{2}[2(-8) + (14)5]$$

$$= \frac{15}{2}[-16 + 70]$$

$$= 27 \cdot 15$$

$$= 405$$

$$S_5 = \frac{5}{2}[2(-8) + 4 \times 5]$$

$$= \frac{5}{2}[-16 + 20]$$

$$= 10$$

$$S_{15} - S_5 = 395$$

12. Consider the system of linear equation  $x + y + z = 4\mu$ ,  $x + 2y + 2\lambda z = 10\mu$ ,  $x + 3y + 4\lambda^2 z = \mu^2 + 15$ , where  $\lambda, \mu \in \mathbb{R}$ . Which one of the following statements is **NOT** correct?

- (1) The system has infinite number of solutions if  $\lambda = \frac{1}{2}$  and  $\mu = 15$   
(2) The system is consistent if  $\lambda \neq \frac{1}{2}$   
(3) The system is inconsistent if  $\lambda = \frac{1}{2}$  and  $\mu \neq 1$   
(4) The system has unique solution if  $\lambda \neq \frac{1}{2}$  and  $\mu \neq 1, 15$

**Answer (3)**

**Sol.** Given system of equation is

$$x + y + z = 4\mu$$

$$x + 2y + 2\lambda z = 10\mu$$

$$x + 3y + 4\lambda^2 z = \mu^2 + 15$$

$$\Delta = \begin{vmatrix} 1 & 1 & 1 \\ 1 & 2 & 2\lambda \\ 1 & 3 & 4\lambda^2 \end{vmatrix} = (2\lambda - 1)^2$$

If  $\lambda \neq \frac{1}{2}$  the system is consistent and has a unique solution.

If  $\lambda = \frac{1}{2}$  the system reduces to

$$x + y + z = 4\mu \quad \dots(i)$$

$$x + 2y + z = 10\mu \quad \dots(ii)$$

$$x + 3y + z = \mu^2 + 15 \quad \dots(iii)$$



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From (i) and (ii)  $y = 6\mu$  and  $x + z = -2\mu$ .

Putting in (iii) gives  $-2\mu + 18\mu = \mu^2 + 15$ .

$$\Rightarrow (\mu - 1)(\mu - 15) = 0.$$

Hence for  $\lambda = \frac{1}{2}$  and  $u = 1$  or  $15$  we have consistent system with infinite number of solution.

13. Let  $g: \mathbb{R} \rightarrow \mathbb{R}$  be a non constant twice differentiable function such that  $g'\left(\frac{1}{2}\right) = g'\left(\frac{3}{2}\right)$ . If a real valued function  $f$  is defined as  $f(x) = \frac{1}{2}[g(x) + g(2-x)]$ , then

(1)  $f'(x) = 0$  for exactly one  $x$  in  $(0, 1)$

(2)  $f'\left(\frac{3}{2}\right) + f'\left(\frac{1}{2}\right) = 1$

(3)  $f'(x) = 0$  for atleast two  $x$  in  $(0, 2)$

(4)  $f'(x) = 0$  for no  $x$  in  $(0, 1)$

**Answer (3)**

**Sol.**  $f(x) = \frac{1}{2}[g(x) + g(2-x)]$

$$f'(x) = \frac{1}{2}[g'(x) - g'(2-x)]$$

Put  $x = \frac{1}{2}$

$$f'\left(\frac{1}{2}\right) = \frac{1}{2}[g'(1/2) - g'(3/2)]$$

$$= 0 \text{ [Given]}$$

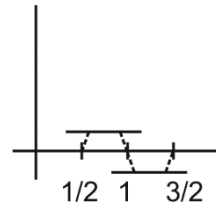
$$f'(3/2) = 1/2[g'(3/2) - g'(1/2)]$$

$$= 0$$

$$f'(1) = 1/2[g'(1) - g'(1)]$$

$$= 0$$

So curve  $f(x)$  will be like



So  $f''(x) = 0$ , atleast for 2 values of  $x$  in  $(0, 2)$

14. Let  $y = y(x)$  be the solution of the differential equation  $\sec x \, dy + \{2(1-x)\tan x + x(2-x)\}dx = 0$  such that  $y(0) = 2$ . Then  $y(2)$  is equal to :

(1)  $2\{\sin(2) + 1\}$  (2) 1

(3)  $2\{1 - \sin(2)\}$  (4) 2

**Answer (4)**

**Sol.** Given differential equation can be written as

$$dy = (2(x-1)\sin x + x(x-2)\cos x)dx.$$

Integrating both sides.

$$\Rightarrow y = \int (2(x-1)\sin x + (x^2 - 2x) \cdot \cos x)dx$$

$$y(x) = 2(-(x-1)\cos x + \sin x) + (x^2 - 2x)\sin x + 2(x-1)\cos x - \sin x + c$$

$$y(x) = (x^2 - 2x)\sin x + c$$

$$y(0) = 2 \Rightarrow c = 2$$

$$\text{Hence, } y(x) = (x^2 - 2x)\sin x + 2$$

$$y(2) = 2$$

15. A line passing through the point  $A(9, 0)$  makes angle of  $30^\circ$  with the positive direction of  $x$ -axis. If this line is rotated about  $A$  through an angle of  $15^\circ$  in the clockwise direction, then its equation in the new position is :

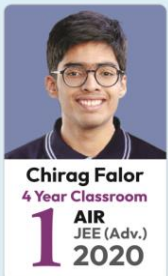
(1)  $\frac{y}{\sqrt{3}-2} + x = 9$  (2)  $\frac{x}{\sqrt{3}-2} + y = 9$

(3)  $\frac{y}{\sqrt{3}+2} + x = 9$  (4)  $\frac{x}{\sqrt{3}+2} + y = 9$

**Answer (1)**

**Sol.** Inclination of line in new position  $= 15^\circ$ .

$$\Rightarrow \text{Slope} = \tan 15^\circ = 2 - \sqrt{3}.$$



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Required equation

$$y - 0 = (2 - \sqrt{3})(x - 9).$$

$$\Rightarrow x + \frac{y}{\sqrt{3} - 2} = 9$$

16. If  $z = x + iy$ ,  $xy \neq 0$ , satisfies the equation

$$z^2 + i\bar{z} = 0, \text{ then } |z^2| \text{ is equal to :}$$

- (1) 4 (2) 9  
(3) 1 (4)  $\frac{1}{4}$

**Answer (3)**

**Sol.**  $z = x + iy$ ,  $x \neq 0$ ,  $y \neq 0 \Rightarrow |z| \neq 0$

$$z^2 + i\bar{z} = 0$$

$$\Rightarrow z^2 = -i\bar{z}$$

$$\Rightarrow |z^2| = |-i\bar{z}| = |-i| |\bar{z}|$$

$$\Rightarrow |z|^2 = |z| \Rightarrow |z| (|z| - 1) = 0$$

$$\Rightarrow |z| = 1$$

17. Let  $\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$  and  $\vec{b} = b_1\hat{i} + b_2\hat{j} + b_3\hat{k}$  be

two vectors such that  $|\vec{a}| = 1$ ,  $\vec{a} \cdot \vec{b} = 2$  and  $|\vec{b}| = 4$ . If

$$\vec{c} = 2(\vec{a} \times \vec{b}) - 3\vec{b}, \text{ then the angle between } \vec{b} \text{ and}$$

$\vec{c}$  is equal to :

- (1)  $\cos^{-1}\left(\frac{2}{3}\right)$  (2)  $\cos^{-1}\left(\frac{2}{\sqrt{3}}\right)$   
(3)  $\cos^{-1}\left(-\frac{\sqrt{3}}{2}\right)$  (4)  $\cos^{-1}\left(-\frac{1}{\sqrt{3}}\right)$

**Answer (3)**

**Sol.**  $|\vec{a}|^2 |\vec{b}|^2 = |\vec{a} \cdot \vec{b}|^2 + |\vec{a} \times \vec{b}|^2$

$$\Rightarrow |\vec{a} \times \vec{b}|^2 = 16 - 4 = 12$$

$$\vec{c} = 2\vec{a} \times \vec{b} - 3\vec{b}$$

$$\vec{b} \cdot \vec{c} = 2[\vec{a} \cdot \vec{b}] - 3|\vec{b}|^2$$

$$= 0 - 3(16) = -48$$

$$\vec{c} \cdot \vec{c} = (2\vec{a} \times \vec{b} - 3\vec{b}) \cdot (2\vec{a} \times \vec{b} - 3\vec{b})$$

$$= (4(\vec{a} \times \vec{b}) \cdot (\vec{a} \times \vec{b}) + 9|\vec{b}|^2 - 6[\vec{a} \cdot \vec{b}])$$

$$|\vec{c}|^2 = (4|\vec{a} \times \vec{b}|^2 + 9 \times 16)$$

$$= (48 + 144) = 192$$

Let angle between  $\vec{b}$  and  $\vec{c}$  is  $\theta$ .

$$\Rightarrow \vec{b} \cdot \vec{c} = |\vec{b}| |\vec{c}| \cos \theta = -48$$

$$\Rightarrow (4)\sqrt{192} \cos \theta = -48$$

$$\Rightarrow \cos \theta = \frac{-48}{4 \times \sqrt{192}} = -\sqrt{\frac{48 \times 48}{16 \times 192}}$$

$$= -\sqrt{\frac{3}{4}} = -\frac{\sqrt{3}}{2}$$

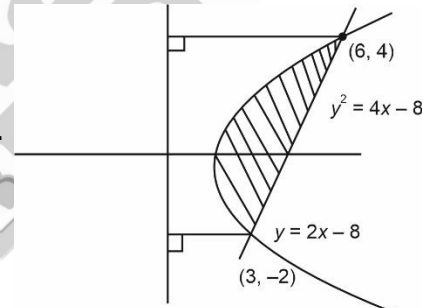
$$\theta = \cos^{-1}\left(-\frac{\sqrt{3}}{2}\right)$$

18. The area (in square units) of the region bounded by the parabola  $y^2 = 4(x - 2)$  and the line  $y = 2x - 8$ , is :

- (1) 7 (2) 9  
(3) 6 (4) 8

**Answer (2)**

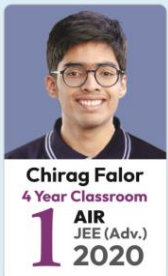
**Sol.**



Area along y-axis

$$\int_{-2}^4 \left[ \left( \frac{y+8}{2} \right) - \left( \frac{y^2+8}{4} \right) \right] dy$$

$$= \frac{y^2}{4} + 4y - \frac{y^3}{12} - 2y \Big|_{-2}^4$$



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$$\Rightarrow \left(4 + 16 - \frac{16}{3} - 8\right) - \left(1 - 8 + \frac{8}{12} + 4\right)$$

$$\Rightarrow \left(12 - \frac{16}{3}\right) - \left(\frac{8}{12} - 3\right) = 15 - \left(\frac{64 + 8}{12}\right)$$

$$= 15 - 6 = 9 \text{ sq. unit}$$

19. The maximum area of a triangle whose one vertex is at (0, 0) and the other two vertices lie on the curve  $y = -2x^2 + 54$  at points (x, y) and (-x, y) where  $y > 0$ , is :

- (1) 122                      (2) 92  
(3) 88                      (4) 108

**Answer (4)**

**Sol.** Area of triangle

$$= \frac{1}{2} \begin{vmatrix} 0 & 0 & 1 \\ x & y & 1 \\ -x & y & 1 \end{vmatrix}$$

$$= \frac{1}{2} |2xy| = |xy| \quad y > 0$$

$$\Rightarrow -2x^2 + 54 > 0$$

$$\Rightarrow x^2 - 27 < 0$$

$$\Rightarrow x \in (-3\sqrt{3}, 3\sqrt{3})$$

$$\text{Area} = |x(-2x^2 + 54)|, \quad x \in (-3\sqrt{3}, 3\sqrt{3})$$

$$= |-2x^3 + 54x|$$

$$\frac{dA}{dx} = -6x^2 + 54$$

$$\Rightarrow \frac{dA}{dx} \text{ is zero at } x = 3 \text{ or } -3$$

$$\Rightarrow \frac{d^2A}{dx^2} = -12x$$

$$\text{at } x = 3 \quad \frac{d^2A}{dx^2} < 0$$

$$\Rightarrow \text{Maxima at } x = 3$$

$$\Rightarrow \text{Area} = |3(-2 \times 9 + 54)| = |36 \times 3| = 108$$

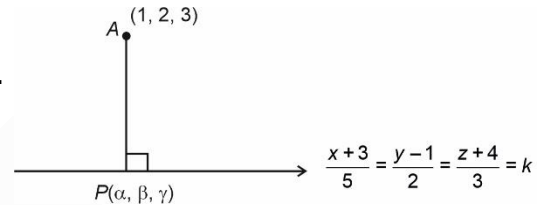
20. Let  $(\alpha, \beta, \gamma)$  be the foot of perpendicular from the point (1, 2, 3) on the line  $\frac{x+3}{5} = \frac{y-1}{2} = \frac{z+4}{3}$ .

Then  $19(\alpha + \beta + \gamma)$  is equal to :

- (1) 101  
(2) 100  
(3) 102  
(4) 99

**Answer (1)**

**Sol.**



$$\Rightarrow \alpha = 5k - 3$$

$$\beta = 2k + 1$$

$$\gamma = 3k - 4$$

$$\alpha + \beta + \gamma = 10k - 6$$

$AP \perp$  to the line

$$\Rightarrow (5\hat{i} + 2\hat{j} + 3\hat{k}) \cdot ((\alpha - 1)\hat{i} + (\beta - 2)\hat{j} + (\gamma - 3)\hat{k}) = 0$$

$$\Rightarrow 5(\alpha - 1) + 2(\beta - 2) + 3(\gamma - 3) = 0$$

$$\Rightarrow 5\alpha + 2\beta + 3\gamma - 5 - 4 - 9 = 0$$

$$5(5k - 3) + 2(2k + 1) + 3(3k - 4) = 18$$

$$\Rightarrow k(25 + 4 + 9) - 15 + 2 - 12 - 18 = 0$$

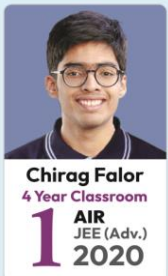
$$\Rightarrow 38k = 43$$

$$\alpha + \beta + \gamma = \left(10 \times \frac{43}{38} - 6\right) = \frac{5 \times 43}{19} - 6$$

$$19(\alpha + \beta + \gamma) = 5 \times 43 - 19 \times 6 = 215 - 114 = 101$$

### SECTION - B

**Numerical Value Type Questions:** This section contains 10 Numerical based questions. Attempt any 5 questions out of 10. The answer to each question should be rounded-off to the nearest integer.



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21. A group of 40 students appeared in an examination of 3 subjects – Mathematics, Physics and Chemistry. It was found that all students passed in atleast one of the subjects, 20 students passed in Mathematics, 25 students passed in Physics, 16 students passed in Chemistry, atmost 11 students passed in both Mathematics and Physics, atmost 15 students passed in both Physics and Chemistry, atmost 15 students passed in both Mathematics and Chemistry. The maximum number of students passed in all the three subjects is \_\_\_\_\_.

**Answer (11)**

**Sol.**  $n(M) = 20$

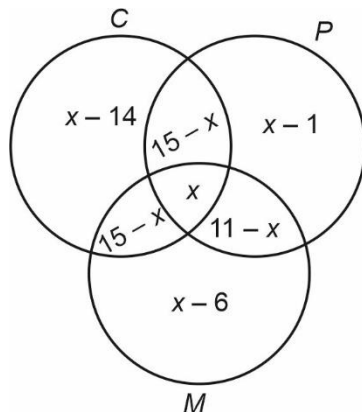
$$n(P) = 25$$

$$n(C) = 16$$

$$n(M \cap P) = 11$$

$$n(P \cap C) = 15$$

$$n(M \cap C) = 15$$



$$n(C \cup P \cup M) \leq n(U) = 40.$$

$$n(C) + n(P) + n(M) - n(C \cap M) - n(P \cap M) - n(C \cap P) + n(C \cap P \cap M) \leq 40$$

$$20 + 25 + 16 - 11 - 15 - 15 + x \leq 40$$

$$x \leq 20$$

$$\text{But } 11 - x \geq 0 \text{ and } 15 - x \geq 0$$

$$\Rightarrow x \geq 11$$

22. The value of  $9 \int_0^9 \left[ \sqrt{\frac{10x}{x+1}} \right] dx$ , where  $[t]$  denotes the greatest integer less than or equal to  $t$ , is \_\_\_\_\_.

**Answer (155)**

**Sol.**  $9 \int_0^9 \left[ \sqrt{\frac{10x}{x+1}} \right] dx$

Let  $I = \int_0^9 \left[ \sqrt{\frac{10x}{x+1}} \right] dx$

$$\frac{10x}{x+1} = 1 \Rightarrow x = \frac{1}{9}$$

$$\frac{10x}{x+1} = 4 \Rightarrow x = \frac{2}{3}$$

$$\frac{10x}{x+1} = 9 \Rightarrow x = 9$$

$$I = \int_0^{1/9} 0 dx + \int_{1/9}^{2/3} 1 dx + \int_{2/3}^9 2 dx$$

$$= 0 + [x]_{1/9}^{2/3} + [2x]_{2/3}^9$$

$$I = \frac{2}{3} - \frac{1}{9} + 18 - \frac{4}{3}$$

$$\Rightarrow I = \frac{155}{9}$$

$$\Rightarrow 9I = 155$$

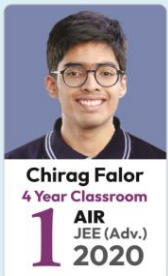
23. Number of integral terms in the expansion of

$$\left\{ 7 \left( \frac{1}{2} \right) + 11 \left( \frac{1}{6} \right) \right\}^{824} \text{ is equal to } \underline{\hspace{2cm}}.$$

**Answer (138)**

**Sol.**  $\left( 7^{\frac{1}{2}} + 11^{\frac{1}{6}} \right)^{824}$

Number of integral term



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$$T_{r+1} = {}^{824}C_r \left(7^{\frac{1}{2}}\right)^{824-r} \left(11^{\frac{1}{6}}\right)^r$$

$\Rightarrow r$  must be multiple of 6

$\Rightarrow r = 0, 6, 12, \dots, 822$

$\Rightarrow 138$  term

24. Let  $A = \{1, 2, 3, \dots, 7\}$  and let  $P(A)$  denote the power set of  $A$ . If the number of functions  $f: A \rightarrow P(A)$  such that  $a \in f(a), \forall a \in A$  is  $m^n$ ,  $m$  and  $n \in \mathbb{N}$  and  $m$  is least, then  $m + n$  is equal to \_\_\_\_\_.

**Answer (44)**

**Sol.**  $n(P(A)) = 2^7$

$a \in f(a)$

$\Rightarrow f(a)$  will have  $(2^6)$  different subsets having  $a$  in them as choice

$\Rightarrow (2^6)^7 = 2^{42}$  function

$m^n = 2^{42}$

$\Rightarrow m + n = 44$

25. Let  $\alpha = 1^2 + 4^2 + 8^2 + 13^2 + 19^2 + 26^2 + \dots$  up to 10 terms and  $\beta = \sum_{n=1}^{10} n^4$ . If  $4\alpha - \beta = 55k + 40$ , then  $k$  is equal to \_\_\_\_\_.

**Answer (353)**

**Sol.**  $\alpha = 1^2 + 4^2 + 8^2 + 13^2 + 19^2 + 26^2 + \dots$

$$T_n = \left(\frac{n^2 + 3n - 2}{2}\right)^2$$

$$\sum T_n = \alpha = \sum_{n=1}^{10} \left(\frac{n^2 + 3n - 2}{2}\right)^2$$

$$4\alpha = \sum_{n=1}^{10} (n^2 + 3n - 2)^2$$

$$\beta = \sum_{n=1}^{10} n^4$$

$$4\alpha - \beta = \sum_{n=1}^{10} (9n^2 + 4 + 6n^3 - 12n - 4n^2)$$

$$= \sum_{n=1}^{10} (6n^3 + 5n^2 - 12n + 4)$$

$$= 6 \sum_{n=1}^{10} n^3 + 5 \sum_{n=1}^{10} n^2 - 12 \sum_{n=1}^{10} n + 4 \sum_{n=1}^{10} 1$$

$$= 6 \times \left(\frac{10 \times 11}{2}\right)^2 + 5 \left(\frac{10 \times 11 \times 21}{6}\right) - 12 \left(\frac{10 \times 11}{2}\right) + 4 \times 10$$

$$= 19455 = 55k + 40$$

$$\Rightarrow k = 353$$

26. If  $d_1$  is the shortest distance between the lines  $x + 1 = 2y = -12z$ ,  $x = y + 2 = 6z - 6$  and  $d_2$  is the shortest distance between the lines

$$\frac{x-1}{2} = \frac{y+8}{-7} = \frac{z-4}{5}, \frac{x-1}{2} = \frac{y-2}{1} = \frac{z-6}{-3}, \text{ then}$$

the value of  $\frac{32\sqrt{3}d_1}{d_2}$  is :

**Answer (16)**

**Sol.**  $\frac{x+1}{-12} = \frac{y}{-6} = \frac{z}{1}, \frac{x}{6} = \frac{y+2}{6} = \frac{z-1}{1}$

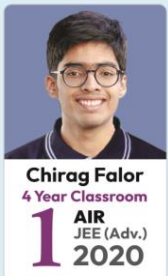
$$A_1(-1, 0, 0), A_2(0, -2, 1), \overrightarrow{A_1 A_2} = \hat{i} - 2\hat{j} + \hat{k}$$

$$\vec{n}_1 = (-12\hat{i} - 6\hat{j} + \hat{k}), \vec{n}_2 = 6\hat{i} + 6\hat{j} + \hat{k}$$

$$\vec{n}_1 \times \vec{n}_2 = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ -12 & -6 & 1 \\ 6 & 6 & 1 \end{vmatrix} = 6(-2\hat{i} + 3\hat{j} - 6\hat{k})$$

$$\Rightarrow |\vec{n}_1 \times \vec{n}_2| = 42$$

$$d_1 = \frac{|\overrightarrow{A_1 A_2} \cdot (\vec{n}_1 \times \vec{n}_2)|}{|\vec{n}_1 \times \vec{n}_2|} = \frac{|6(-2-6-6)|}{7 \times 6} = 2$$



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$$\therefore \frac{x-1}{2} = \frac{y+8}{-7} = \frac{z-4}{5}, \frac{x-1}{2} = \frac{y-2}{1} = \frac{z-6}{-3}$$

$$A_3 = (1, -8, 4), A_4 = (1, 2, 6), \overrightarrow{A_3 A_4} = 10\hat{j} + 2\hat{k}$$

$$\vec{n}_3 \times \vec{n}_4 = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & -7 & 5 \\ 2 & 1 & -3 \end{vmatrix} = 16\hat{i} + 16\hat{j} + 16\hat{k}$$

$$\Rightarrow |\vec{n}_3 \times \vec{n}_4| = 16\sqrt{3}$$

$$d_2 = \frac{|\overrightarrow{A_3 A_4} \cdot (\vec{n}_3 \times \vec{n}_4)|}{|\vec{n}_3 \times \vec{n}_4|} = \frac{16(10+2)}{16\sqrt{3}} = \frac{12}{\sqrt{3}}$$

$$\Rightarrow \frac{32\sqrt{3} d_1}{d_2} = \frac{32\sqrt{3} \times 12 \times \sqrt{3}}{12 \times 6} = 16$$

27. If the function  $f(x) = \begin{cases} \frac{1}{|x|}, & |x| \geq 2 \\ ax^2 + 2b, & |x| < 2 \end{cases}$  is differentiable on  $\mathbf{R}$ , then  $48(a + b)$  is equal to \_\_\_\_\_.

**Answer (15)**

$$\text{Sol. } f(x) = \begin{cases} \frac{1}{|x|}, & |x| \geq 2 \\ ax^2 + 2b, & |x| < 2 \end{cases}$$

$$f(x) = \begin{cases} -\frac{1}{x}, & x \leq -2 \\ ax^2 + 2b, & -2 < x < 2 \\ \frac{1}{x}, & x \geq 2 \end{cases}$$

$$\Rightarrow f'(x) = \begin{cases} \frac{1}{x^2}, & x \leq -2 \\ 2ax, & -2 < x < 2 \\ -\frac{1}{x^2}, & x \geq 2 \end{cases}$$

$$f(x) \text{ is continuous at } x = -2 \Rightarrow \frac{1}{2} = 4a + 2b$$

$$f(x) \text{ is continuous at } x = 2 \Rightarrow \frac{1}{2} = 4a + 2b$$

$$f(x) \text{ is differentiable at } x = -2 \Rightarrow \frac{1}{4} = -4a$$

$$f(x) \text{ is differentiable at } x = 2 \Rightarrow 4a = -\frac{1}{4}$$

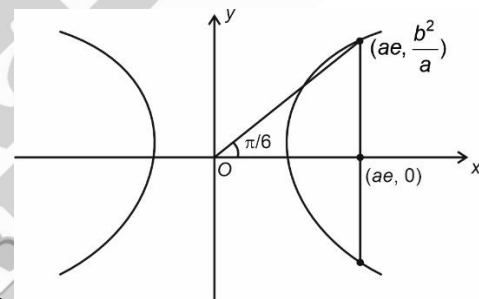
$$\Rightarrow a = -\frac{1}{16}, b = \frac{3}{8}$$

$$\Rightarrow 48(a + b) = -3 + 18 = 15$$

28. Let the latus rectum of the hyperbola  $\frac{x^2}{9} - \frac{y^2}{b^2} = 1$

subtend an angle of  $\frac{\pi}{3}$  at the centre of the hyperbola. If  $b^2$  is equal to  $\frac{l}{m}(1 + \sqrt{n})$ , where  $l$  and  $m$  are co-prime numbers, then  $l^2 + m^2 + n^2$  is equal to \_\_\_\_\_.

**Answer (182)**

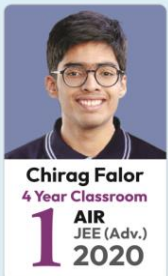


**Sol.**

$$\Rightarrow \tan \frac{\pi}{6} = \frac{b^2}{a^2 e}$$

$$\therefore \frac{b^2}{a^2} = (e^2 - 1)$$

$$\frac{1}{\sqrt{3}} = \frac{e^2 - 1}{e} \Rightarrow \sqrt{3}e^2 - e - \sqrt{3} = 0$$



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$$e = \frac{1 \pm \sqrt{1+12}}{2\sqrt{3}}, \because e > 1 \Rightarrow e = \frac{\sqrt{13}+1}{2\sqrt{3}}$$

$$\Rightarrow b^2 = 9 \left( \frac{13+1+2\sqrt{13}}{12} - 1 \right) = 9 \left( \frac{2+2\sqrt{13}}{12} \right)$$

$$\Rightarrow b^2 = 9 \left( \frac{1+\sqrt{13}}{6} \right)$$

$$b^2 = \frac{3}{2}(1+\sqrt{13})$$

$$\Rightarrow l = 3, m = 2, n = 13$$

$$\Rightarrow l^2 + m^2 + n^2 = 182$$

29. Let  $y = y(x)$  be the solution of the differential equation  $(1-x^2)dy = [xy + (x^3+2)\sqrt{3(1-x^2)}]dx$ ,  $-1 < x < 1$ ,  $y(0) = 0$ . If  $y\left(\frac{1}{2}\right) = \frac{m}{n}$ ,  $m$  and  $n$  are co-prime numbers, then  $m+n$  is equal to \_\_\_\_\_.

**Answer (97)**

**Sol.**  $\frac{dy}{dx} + \left(\frac{x}{x^2-1}\right)y = \frac{(x^3+2)\sqrt{3}}{\sqrt{1-x^2}}$

$$\text{I.F.} = e^{\int \frac{x}{x^2-1} dx} = e^{\frac{1}{2} \ln|x^2-1|} = \sqrt{1-x^2}$$

Solution of D.E.

$$y \cdot \sqrt{1-x^2} = \int \sqrt{3}(x^3+2) dx + C$$

$$y \cdot \sqrt{1-x^2} = \sqrt{3} \left( \frac{x^4}{4} + 2x \right) + C$$

$$\because y(0) = 0 \Rightarrow C = 0$$

$$y\sqrt{1-x^2} = \sqrt{3} \left( \frac{x^4}{4} + 2x \right)$$

$$\Rightarrow y\left(\frac{1}{2}\right) = \frac{\sqrt{3} \left( \frac{1}{64} + 1 \right)}{\frac{\sqrt{3}}{2}} = \frac{65}{32}$$

$$\Rightarrow m+n = 97$$

30. Let  $\alpha, \beta \in N$  be roots of the equation  $x^2 - 70x + \lambda = 0$ .

Where  $\frac{\lambda}{2}, \frac{\lambda}{3} \notin N$ . If  $\lambda$  assumes the minimum

possible value, then  $\frac{(\sqrt{\alpha-1} + \sqrt{\beta-1})(\lambda+35)}{|\alpha-\beta|}$  is equal to :

**Answer (60)**

**Sol.**  $x^2 - 70x + \lambda = 0$

$$\alpha + \beta = 70, \alpha\beta = \lambda$$

$$\because \frac{\lambda}{2}, \frac{\lambda}{3} \notin N, \alpha, \beta \in N$$

$$\Rightarrow \lambda \text{ is not divisible by 2 or 3}$$

$$\Rightarrow \alpha, \beta \text{ not divisible by 2 or 3}$$

$$\lambda = \alpha(70-\alpha) \Rightarrow \frac{d\lambda}{d\alpha} = 70-2\alpha$$

$$\lambda \text{ is increasing when } \alpha \leq 35$$

$$\Rightarrow \lambda \text{ is minimum when } \alpha = 5 \text{ or } \alpha = 65$$

$$\because \text{When } \alpha = 1, \beta = 69 \text{ (divisible by 3) not possible}$$

$$\alpha \neq 2, \alpha \neq 3, \alpha \neq 4$$

$$\Rightarrow \alpha = 5, \beta = 65$$

$$\Rightarrow \frac{(\sqrt{\alpha-1} + \sqrt{\beta-1})(\lambda+35)}{|\alpha-\beta|} = \frac{(2+8) \cdot (5 \times 65 + 35)}{60}$$

$$= 60$$



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## PHYSICS

### SECTION - A

**Multiple Choice Questions:** This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

**Choose the correct answer :**

31. The electrostatic potential due to an electric dipole at a distance ' $r$ ' varies as :

- (1)  $\frac{1}{r^3}$                       (2)  $\frac{1}{r^2}$   
(3)  $r$                         (4)  $\frac{1}{r}$

**Answer (2)**

**Sol.** For dipole

$$V = \frac{kP}{r^2}$$

$$\Rightarrow V \propto \frac{1}{r^2}$$

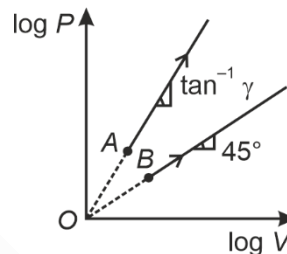
32. The work function of a substance is 3.0 eV. The longest wavelength of light that can cause the emission of photoelectrons from this substance is approximately;

- (1) 414 nm  
(2) 400 nm  
(3) 215 nm  
(4) 200 nm

**Answer (1)**

**Sol.**  $\lambda_{th} = \frac{hc}{\phi_0} = \frac{1240}{3} \text{ nm}$   
 $= 414 \text{ nm}$

33. Two thermodynamical processes are shown in the figure. The molar heat capacity for process A and B are  $C_A$  and  $C_B$ . The molar heat capacity at constant pressure and constant volume are represented by  $C_P$  and  $C_V$  respectively. Choose the correct statement.



- (1)  $C_A > C_P > C_V$                       (2)  $C_B = \infty, C_A = 0$   
(3)  $C_A = 0$  and  $C_B = \infty$                       (4)  $C_P > C_V > C_A = C_B$

**Answer (None)**

**Sol.**  $PV^{-x} = \text{const}$

where  $x$  is slope

For A,  $x = 1, C_A = C_V + \frac{R}{2}$

For B,  $x = \gamma, C_B = C_V + \frac{R}{\gamma + 1}$

None of the options are matching.

34. The diffraction pattern of a light of wavelength 400 nm diffracting from a slit of width 0.2 mm is focused on the focal plane of a convex lens of focal length 100 cm. The width of the 1<sup>st</sup> secondary

- (1) 0.2 mm                      (2) 2 mm  
(3) 0.02 mm                      (4) 2 cm

**Answer (2)**



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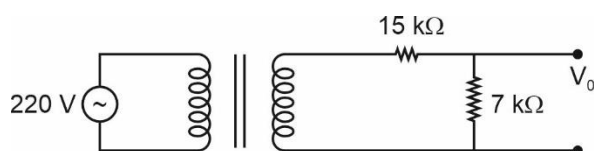
**Sol.** Angular width  $= \frac{\lambda}{a}$

$$\therefore \text{Width} = \frac{\lambda f}{a}$$

$$= \frac{400 \times 10^{-9} \times 1}{0.2 \times 10^{-3}}$$

$$= 2 \text{ mm}$$

35. Primary coil of a transformer is connected to 220 V ac. Primary and secondary turns of the transforms are 100 and 10 respectively. Secondary coil of transformer is connected to two series resistances shown in figure. The output voltage ( $V_0$ ) is :



- (1) 15 V                      (2) 22 V  
(3) 44 V                      (4) 7 V

**Answer (4)**

**Sol.**  $\frac{E_2}{E_1} = \frac{N_2}{N_1}$

$$\therefore E_2 = 22 \text{ V}$$

$$\therefore V_0 = 22 - \left( \frac{15}{22} \right) 22$$

$$= 7 \text{ V}$$

36. The ratio of the magnitude of the kinetic energy to the potential energy of an electron in the 5<sup>th</sup> excited state of a hydrogen atom is :

- (1) 4                      (2) 1  
(3)  $\frac{1}{4}$                       (4)  $\frac{1}{2}$

**Answer (4)**

**Sol.**  $\therefore KE = \frac{1}{2}(-PE)$

$$KE : PE = 1 : -2$$

37. A particle of mass  $m$  is projected with a velocity ' $u$ ' making an angle of  $30^\circ$  with the horizontal. The magnitude of angular momentum of the projectile about the point of projection when the particle is at its maximum height  $h$  is :

- (1) Zero                      (2)  $\frac{mu^3}{\sqrt{2}g}$   
(3)  $\frac{\sqrt{3}}{16} \frac{mu^3}{g}$                       (4)  $\frac{\sqrt{3}}{2} \frac{mu^2}{g}$

**Answer (3)**

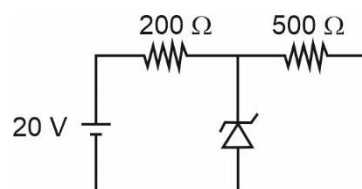
**Sol.**  $L = (mu \cos \theta)H$

$$H = \frac{u^2 \sin^2 \theta}{2g}$$

$$L = \frac{mu^3}{2g} \sin^2 \theta \cos \theta$$

$$= \frac{\sqrt{3}}{16} \frac{mu^3}{g}$$

38. A Zener diode of breakdown voltage 10 V is used as a voltage regulator as shown in the figure. The current through the Zener diode is:



- (1) 30 mA                      (2) 20 mA  
(3) 50 mA                      (4) 0

**Answer (1)**



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**Sol.**  $i_{500} = \frac{10}{500} = 20 \text{ mA}$

$i_{200} = \frac{10}{200} = 50 \text{ mA}$

$\therefore i_z = 30 \text{ mA}$

39. Match **List-I** with **List-II**.

	List-I		List-II
(A)	Coefficient of viscosity	(I)	$[ML^2T^{-2}]$
(B)	Surface tension	(II)	$[ML^2T^{-1}]$
(C)	Angular momentum	(III)	$[ML^{-1}T^{-1}]$
(D)	Rotational kinetic energy	(IV)	$[ML^0T^{-2}]$

Choose the **correct** answer from the options given below:

- (1) (A)-(I), (B)-(II), (C)-(III), (D)-(IV)  
 (2) (A)-(III), (B)-(IV), (C)-(II), (D)-(I)  
 (3) (A)-(IV), (B)-(III), (C)-(II), (D)-(I)  
 (4) (A)-(II), (B)-(I), (C)-(IV), (D)-(III)

**Answer (2)**

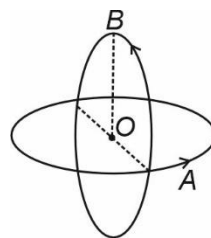
**Sol.**  $[\eta] = [ML^{-1}T^{-1}]$

$[S] = [MT^{-2}]$

$[L] = [ML^2T^{-1}]$

$[KE] = [ML^2T^{-2}]$

40. Two insulated circular loop A and B of radius 'a' carrying a current of 'I' in the anti clockwise direction as shown in the figure. The magnitude of the magnetic induction at the centre will be:



- (1)  $\frac{\sqrt{2}\mu_0 I}{a}$  (2)  $\frac{\mu_0 I}{2a}$   
 (3)  $\frac{\mu_0 I}{\sqrt{2}a}$  (4)  $\frac{2\mu_0 I}{a}$

**Answer (3)**

**Sol.**  $B_1$  &  $B_2$  are perpendicular

$\therefore B_{eq} = \frac{\sqrt{2}\mu_0 I}{2a} = \frac{\mu_0 I}{\sqrt{2}a}$

41. A series L.R circuit connected with an ac source  $E = (25 \sin 1000 t) \text{ V}$  has a power factor of  $\frac{1}{\sqrt{2}}$ . If the source of emf is changed to  $E = (20 \sin 2000 t) \text{ V}$ , the new power factor of the circuit will be:

- (1)  $\frac{1}{\sqrt{7}}$   
 (2)  $\frac{1}{\sqrt{2}}$   
 (3)  $\frac{1}{\sqrt{5}}$   
 (4)  $\frac{1}{\sqrt{3}}$

**Answer (3)**



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**Sol.** For LR circuit

$$\cos \phi = \frac{R}{\sqrt{(x_L)^2 + R^2}} = \frac{1}{\sqrt{2}}$$

$$R = x_L$$

When  $w' = 2w$

$$x'_L = 2x_L$$

$$\therefore \cos \phi' = \frac{R}{\sqrt{4x_L^2 + R^2}} = \frac{1}{\sqrt{5}}$$

42. A spherical body of mass 100 g is dropped from a height of 10 m from the ground. After hitting the ground, the body rebounds to a height of 5 m. The impulse of force imparted by the ground to the body is given by: (given,  $g = 9.8 \text{ m/s}^2$ )

- (1) 43.2 kg ms<sup>-1</sup>      (2) 23.9 kg ms<sup>-1</sup>  
 (3) 2.39 kg ms<sup>-1</sup>      (4) 4.32 kg ms<sup>-1</sup>

**Answer (3)**

**Sol.**  $V_1 = \sqrt{2gh_1}$

$$V_2 = \sqrt{2gh_2}$$

$$\Delta V = (V_1 + V_2)$$

$$\therefore I = m \Delta V$$

$$= 0.1 \times \sqrt{2g} (\sqrt{h_1} + \sqrt{h_2})$$

$$= 2.39 \text{ kg m/s}$$

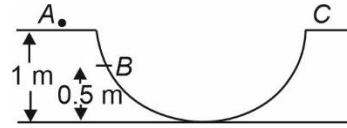
43. Young's modulus of material of a wire length 'L' and cross-sectional area A is Y. If the length of the wire is doubled and cross-sectional area is halved then Young's modulus will be:

- (1) Y      (2) 2Y  
 (3)  $\frac{Y}{4}$       (4) 4Y

**Answer (1)**

**Sol.** Young's modulus is a property of material, it is independent of dimension.

44. A particle is placed at the point A of a frictionless track ABC as shown in figure. It is gently pushed towards right. The speed of the particle when it reaches the point B is: (Take  $g = 10 \text{ m/s}^2$ )



- (1)  $2\sqrt{10} \text{ m/s}$       (2) 10 m/s  
 (3)  $\sqrt{10} \text{ m/s}$       (4) 20 m/s

**Answer (3)**

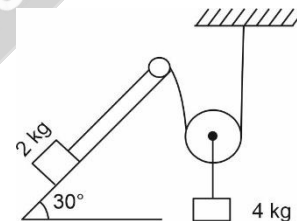
**Sol.** By conservation of mechanical energy

$$\frac{1}{2}mv^2 = mg(\Delta h)$$

$$V = \sqrt{20 \times 0.5}$$

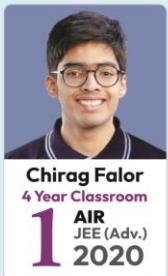
$$= \sqrt{10} \text{ m/s}$$

45. All surfaces shown in figure are assumed to be frictionless and all the pulleys and the string are light. The acceleration of the block of mass 2 kg is:



- (1) g      (2)  $\frac{g}{2}$   
 (3)  $\frac{g}{4}$       (4)  $\frac{g}{3}$

**Answer (4)**



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**Sol.**  $4g - 2T = 4\left(\frac{a}{2}\right)$

$\Rightarrow T = (2g - a)$

Now,

$T - 2g \sin 30^\circ = 2a$

$\Rightarrow a = \frac{g}{3}$

46. At which temperature the r.m.s. velocity of a hydrogen molecule equal to that of an oxygen molecule at  $47^\circ\text{C}$ ?

- (1) 80 K
- (2) 20 K
- (3) 4 K
- (4)  $-73$  K

**Answer (2)**

**Sol.**  $V_{\text{rms}} = \sqrt{\frac{3RT}{M}}$

$\therefore \frac{T}{2} = \frac{(273 + 47)}{32}$

$\Rightarrow T = 20 \text{ K}$

47. The gravitational potential at a point above the surface of earth is  $-5.12 \times 10^7 \text{ J/kg}$  and the acceleration due to gravity at that point is  $6.4 \text{ m/s}^2$ . Assume that the mean radius of earth to be 6400 km. The height of this point above the earth's surface is:

- (1) 540 km
- (2) 1200 km
- (3) 1600 km
- (4) 1000 km

**Answer (3)**

**Sol.**  $V = \frac{-GM}{r}$

and  $g = \frac{GM}{r^2}$

$\Rightarrow r = \frac{-V}{g} = \frac{5.12 \times 10^7}{6.4} = 8000 \text{ km}$

$\Rightarrow h = r - 6400 = 1600 \text{ km}$

48. The electric field of an electromagnetic wave in free space is represented at  $\vec{E} = E_0 \cos(\omega t - kz) \hat{i}$ . The corresponding magnetic induction vector will be:

- (1)  $\vec{B} = E_0 C \cos(\omega t + kz) \hat{j}$
- (2)  $\vec{B} = E_0 C \cos(\omega t - kz) \hat{j}$
- (3)  $\vec{B} = \frac{E_0}{C} \cos(\omega t - kz) \hat{j}$
- (4)  $\vec{B} = \frac{E_0}{C} \cos(\omega t + kz) \hat{j}$

**Answer (3)**

**Sol.**  $\vec{E} \times \vec{B}$  is along  $+z$  axis

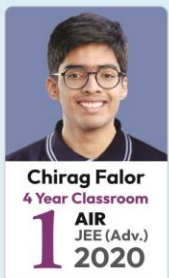
and  $B = \frac{E_0}{C}$

$\therefore \vec{B} = \frac{E_0}{C} \cos(\omega t - kz) \hat{j}$

49. An electric toaster has resistance of  $60 \Omega$  at room temperature ( $27^\circ\text{C}$ ). The toaster is connected to a 220 V supply. If the current flowing through it reaches 2.75 A, the temperature attained by toaster is around: (if  $\alpha = 2 \times 10^{-4}/^\circ\text{C}$ )

- (1)  $1667^\circ\text{C}$
- (2)  $694^\circ\text{C}$
- (3)  $1235^\circ\text{C}$
- (4)  $1694^\circ\text{C}$

**Answer (4)**



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**Sol.**  $R = \frac{V}{I} = \frac{220}{2.75} = 80 \Omega$

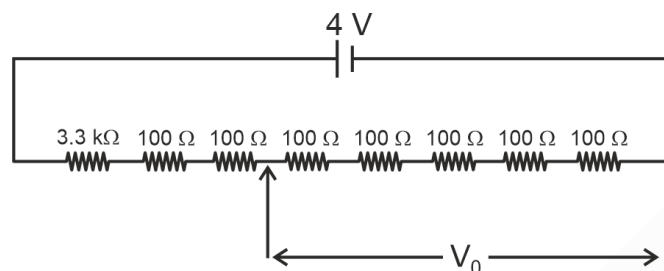
and,  $R = R_0(1 + \alpha \Delta T)$

$\Rightarrow 80 = 60(1 + 2 \times 10^{-4} \Delta T)$

$\Rightarrow \Delta T = 1667^\circ\text{C}$

$\therefore T = 27 + \Delta T = 1694^\circ\text{C}$

50. A potential divider circuit is shown in figure. The output voltage  $V_0$  is:



(1) 2 mV

(2) 0.5 V

(3) 4 V

(4) 12 mV

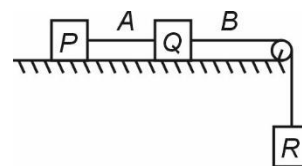
**Answer (2)**

**Sol.**  $V_{\text{out}} = \frac{5 \times 100}{4000} \times 4$   
 $= 0.5 \text{ V}$

### SECTION - B

**Numerical Value Type Questions:** This section contains 10 Numerical based questions. Attempt any 5 questions out of 10. The answer to each question should be rounded-off to the nearest integer.

51. Each of three blocks  $P$ ,  $Q$  and  $R$  shown in figure has a mass of 3 kg. Each of the wires  $A$  and  $B$  has cross-sectional area  $0.005 \text{ cm}^2$  and Young's modulus  $2 \times 10^{11} \text{ N m}^{-2}$ . Neglecting friction, the longitudinal strain on wire  $B$  is  $\underline{\hspace{2cm}} \times 10^{-4}$ . (Take  $g = 10 \text{ m/s}^2$ )



**Answer (2)**

**Sol.**  $a = \frac{3g}{9} = \frac{g}{3} \text{ m/s}^2$

$T_A = ma = g$

$T_B - T_A = ma$

$T_B = 2g = 20 \text{ N}$

$\left(\frac{\Delta L}{L}\right) = \frac{(T_B)}{AY} = \frac{20}{0.005 \times 10^{-4} \times 2 \times 10^{11}}$   
 $= 2 \times 10^{-4}$

52. The distance between object and its two times magnified real image as produced by a convex lens is 45 cm. The focal length of the lens used is  $\underline{\hspace{2cm}}$  cm.

**Answer (10)**

**Sol.**  $m = -2$

$v = -2u$

$v - u = 45$

$u = -15, v = 30$

$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$

$\frac{1}{f} = \frac{1}{30} - \frac{1}{-15}$

$f = 10 \text{ cm}$



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53. A capacitor of capacitance  $C$  and potential  $V$  has energy  $E$ . It is connected to another capacitor of capacitance  $2C$  and potential  $2V$ . Then the loss of energy is  $\frac{x}{3}E$ , where  $x$  is \_\_\_\_\_.

**Answer (2)**

**Sol.**  $V_{eq} = \frac{Q_1 + Q_2}{3C} = \frac{5V}{3}$

$$E = \frac{1}{2}CV^2$$

$$E' = \frac{1}{2} \times 3C \times \left(\frac{5V}{3}\right)^2 = \frac{25}{6}CV^2$$

$$E_{Loss} = \frac{1}{2}CV^2 + 4CV^2 - \frac{25}{6}CV^2$$

$$= \frac{1}{3}CV^2$$

$$\therefore E_{Loss} = \frac{2E}{3}$$

54. In a closed organ pipe, the frequency of fundamental note is 30 Hz. A certain amount of water is now poured in the organ pipe so that the fundamental frequency is increased to 110 Hz. If the organ pipe has a cross-sectional area of  $2 \text{ cm}^2$ , the amount of water poured in the organ tube is \_\_\_\_\_ g. (Take speed of sound in air is 330 m/s)

**Answer (400)**

**Sol.**  $f = \frac{V}{4l}$

$$l_1 = \frac{V}{4f_1} = \frac{11}{4} \text{ m}$$

$$l_2 = \frac{V}{4f_2} = \frac{3}{4} \text{ m}$$

$$l_1 - l_2 = 2 \text{ m}$$

$$m = V\rho = 2 \times 2 \times 10^{-4} \times 1000$$

$$= 0.4 \text{ kg}$$

55. A electron of hydrogen atom on an excited state is having energy  $E_n = -0.85 \text{ eV}$ . The maximum number of allowed transitions to lower energy level is \_\_\_\_\_.

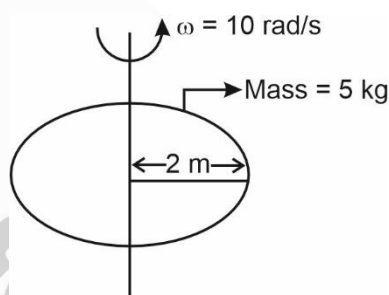
**Answer (6)**

**Sol.**  $E_n = \frac{-13.6}{n^2} = -0.85$

$$n = 4$$

$$\therefore \text{No. of transitions} = \frac{4 \times 3}{2} = 6$$

56.



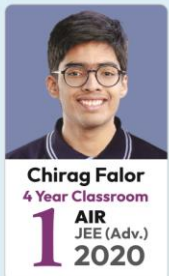
Consider a Disc of mass 5 kg, radius 2 m, rotating with angular velocity of 10 rad/s about an axis perpendicular to the plane of rotation. An identical disc is kept gently over the rotating disc along the same axis. The energy dissipated so that both the discs continue to rotate together without slipping is \_\_\_\_\_ J.

**Answer (250)**

**Sol.** By conservation of angular momentum

$$I\omega = 2I\omega'$$

$$\omega' = \frac{\omega}{2}$$



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$$E_{\text{loss}} = \frac{1}{2} I \omega^2 - \frac{1}{2} \times 2I \times \frac{\omega^2}{4} = \frac{I \omega^2}{4}$$

$$I = \frac{MR^2}{2} = 10 \text{ kg m}^2$$

$$\therefore E_{\text{loss}} = \frac{10}{4} \times 100 = 250 \text{ J}$$

57. The horizontal component of earth's magnetic field at a place is  $3.5 \times 10^{-5} \text{ T}$ . A very long straight conductor carrying current of  $\sqrt{2} \text{ A}$  in the direction from South east to North west is placed. The force per unit length experienced by the conductor is \_\_\_\_\_  $\times 10^{-6} \text{ N/m}$ .

**Answer (35)**

**Sol.**  $F = BIl \sin 45^\circ$

$$= 3.5 \times 10^{-5} \times \sqrt{2} \times 1 \times \frac{1}{\sqrt{2}}$$

$$= 35 \times 10^{-6} \text{ N}$$

58. The displacement and the increase in the velocity of a moving particle in the time interval of  $t$  to  $(t+1)$  s are 125 m and 50 m/s, respectively. The distance travelled by the particle in  $(t+2)^{\text{th}}$  s is \_\_\_\_\_ m.

**Answer (175)**

**Sol.**  $S_n = u + a \left( n - \frac{1}{2} \right)$

$$S_{t+1} = u + a \left( t + 1 - \frac{1}{2} \right)$$

$$a = 50 \text{ m/s}^2$$

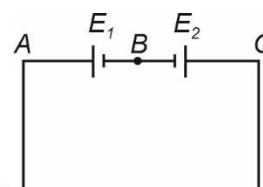
$$125 = u + 50 \left( t + \frac{1}{2} \right)$$

$$S_{t+2} = u + a \left( t + 2 - \frac{1}{2} \right)$$

$$= u + 50 \left( t + \frac{3}{2} \right)$$

$$= 100 + 75 = 175 \text{ m}$$

59. Two cells are connected in opposition as shown. Cell  $E_1$  is of 8 V emf and  $2 \Omega$  internal resistance; the cell  $E_2$  is 2 V emf and  $4 \Omega$  internal resistance. The terminal potential difference of cell  $E_2$  is \_\_\_\_\_ V.



**Answer (6)**

**Sol.**  $i = \frac{E_1 - E_2}{r_1 + r_2} = 1 \text{ A}$

$$\therefore V_2 = E_2 + ir_2 = 2 + 4 = 6 \text{ V}$$

60. A ceiling fan having 3 blades of length 80 cm each is rotating with an angular velocity of 1200 rpm. The magnetic field of earth in that region is 0.5 G and angle of dip is  $30^\circ$ . The emf induced across the blades is  $N\pi \times 10^{-5} \text{ V}$ . The value of  $N$  is \_\_\_\_\_.

**Answer (32)**

**Sol.**  $B_v = B \sin 30^\circ = \frac{0.5}{2} \times 10^{-4} \text{ T}$

$$E = \frac{(B_v) \omega l^2}{2}$$

$$= \frac{0.5}{4} \times 10^{-4} \times 40\pi \times 0.64 = 32\pi \times 10^{-5} \text{ V}$$



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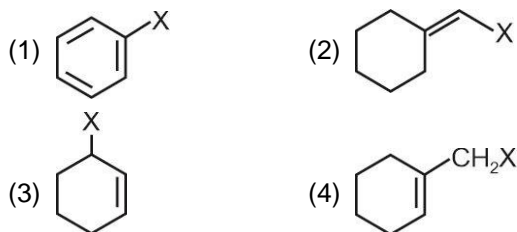
## CHEMISTRY

### SECTION - A

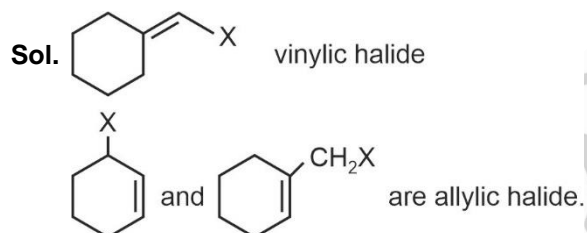
**Multiple Choice Questions:** This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

**Choose the correct answer :**

61. Example of vinylic halide is



**Answer (2)**



62. Given below are two statements.

**Statement (I) :** The gas liberated on warming a salt with dil  $\text{H}_2\text{SO}_4$ , turns a piece of paper dipped in lead acetate into black, it is a confirmatory test for sulphide ion.

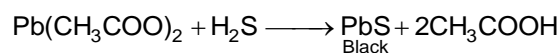
**Statement (II) :** In statement-I the colour of paper turns black because of formation of lead sulphite.

In the light of the above statements, choose the most appropriate answer from the options given below

- (1) Both **Statement I** and **Statement II** are false
- (2) **Statement I** is true but **Statement II** is false
- (3) Both **Statement I** and **Statement II** are true
- (4) **Statement I** is false but **Statement II** is true

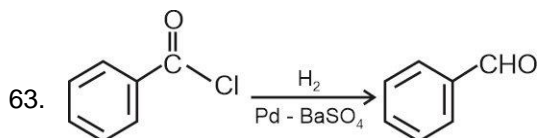
**Answer (2)**

**Sol.**  $\text{H}_2\text{S}$  turns  $\text{Pb}(\text{CH}_3\text{COO})_2$  black.



Statement-I is true.

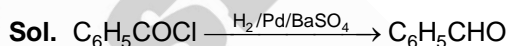
Statement-II is false.



This reduction reaction is known as

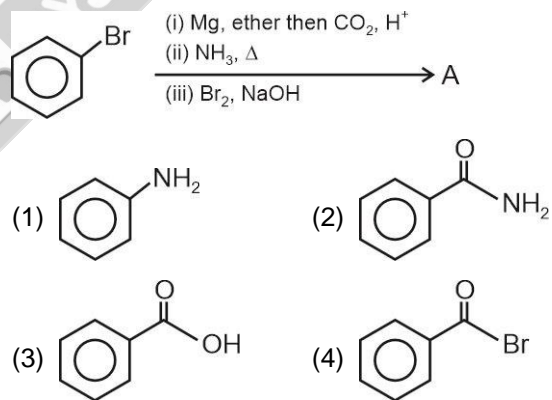
- (1) Etard reduction
- (2) Wolff-Kishner reduction
- (3) Stephen reduction
- (4) Rosenmund reduction

**Answer (4)**



Rosenmund's reduction convert acid halides to aldehydes.

64. The final product A, formed in the following multistep reaction sequence is



**Answer (1)**

  
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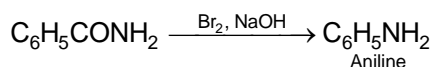
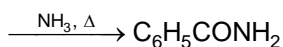
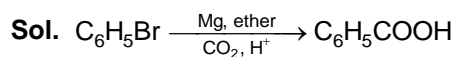
  
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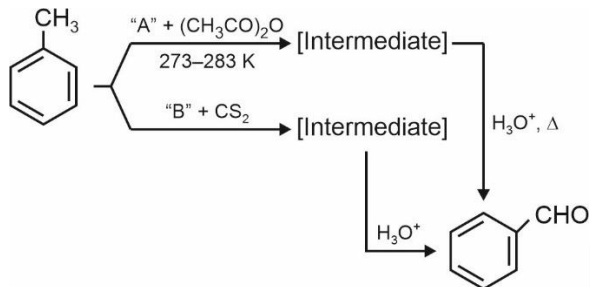
  
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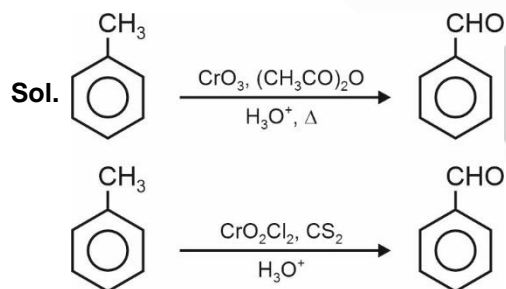


65. In the given reactions, identify the reagent A and reagent B.



- (1) A-CrO<sub>2</sub>Cl<sub>2</sub>, B-CrO<sub>3</sub>
- (2) A-CrO<sub>3</sub>, B-CrO<sub>2</sub>Cl<sub>2</sub>
- (3) A-CrO<sub>2</sub>Cl<sub>2</sub>, B-CrO<sub>2</sub>Cl<sub>2</sub>
- (4) A-CrO<sub>3</sub>, B-CrO<sub>3</sub>

**Answer (2)**



A = CrO<sub>3</sub>

B = CrO<sub>2</sub>Cl<sub>2</sub>

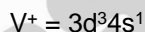
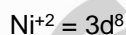
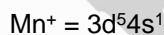
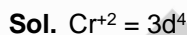
66. Match List-I with List-II.

	List-I Species		List-II Electronic distribution
(A)	Cr <sup>+2</sup>	(I)	3d <sup>8</sup>
(B)	Mn <sup>+</sup>	(II)	3d <sup>3</sup> 4s <sup>1</sup>
(C)	Ni <sup>+2</sup>	(III)	3d <sup>4</sup>
(D)	V <sup>+</sup>	(IV)	3d <sup>5</sup> 4s <sup>1</sup>

Choose the **correct** answer from the options given below

- (1) (A)-(II), (B)-(I), (C)-(IV), (D)-(III)
- (2) (A)-(III), (B)-(IV), (C)-(I), (D)-(II)
- (3) (A)-(IV), (B)-(III), (C)-(I), (D)-(II)
- (4) (A)-(I), (B)-(II), (C)-(III), (D)-(IV)

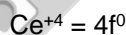
**Answer (2)**



67. Diamagnetic Lanthanoid ions are

- (1) Nd<sup>3+</sup> & Ce<sup>4+</sup>
- (2) La<sup>3+</sup> & Ce<sup>4+</sup>
- (3) Nd<sup>3+</sup> & Eu<sup>3+</sup>
- (4) Lu<sup>3+</sup> & Eu<sup>3+</sup>

**Answer (2)**




Diamagnetic

68. Sugar which does not give reddish brown precipitate with Fehling's reagent, is

- (1) Maltose
- (2) Glucose
- (3) Lactose
- (4) Sucrose

**Answer (4)**

Sol. Aldehyde (carbonyl) group is not free in sucrose.



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69. Match List-I with List-II.

	List-I Molecule		List-II Shape
(A)	BrF <sub>5</sub>	(I)	T-shape
(B)	H <sub>2</sub> O	(II)	See saw
(C)	ClF <sub>3</sub>	(III)	Bent
(D)	SF <sub>4</sub>	(IV)	Square pyramidal

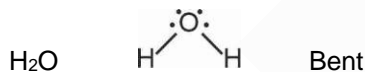
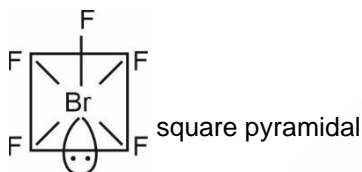
Choose the **correct** answer from the options given below

- (1) (A)-(I), (B)-(II), (C)-(IV), (D)-(III)  
 (2) (A)-(II), (B)-(I), (C)-(III), (D)-(IV)  
 (3) (A)-(III), (B)-(IV), (C)-(I), (D)-(II)  
 (4) (A)-(IV), (B)-(III), (C)-(I), (D)-(II)

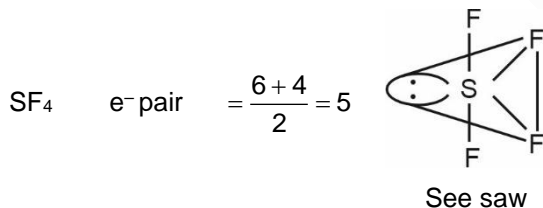
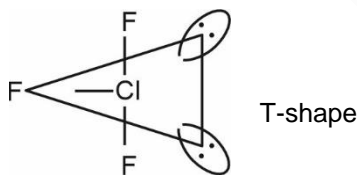
**Answer (4)**

**Sol.** BrF<sub>5</sub>

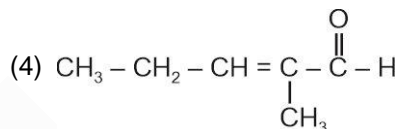
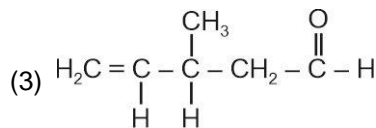
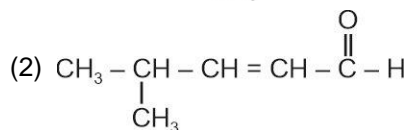
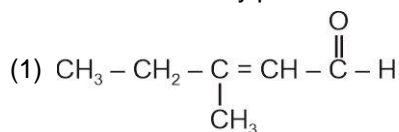
$$\text{Electron pair} = \frac{7+5}{2} = 6$$



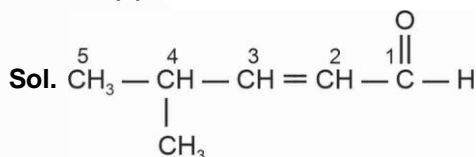
ClF<sub>3</sub>       $e^- \text{ pair} = \frac{7+3}{2} = 5$



70. Structure of 4-Methylpent-2-enal is

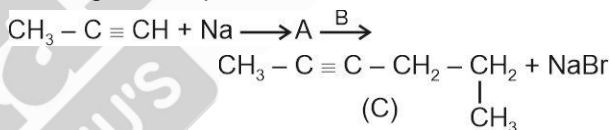


**Answer (2)**



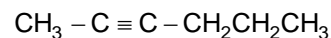
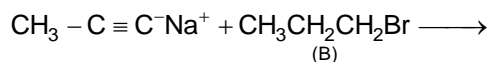
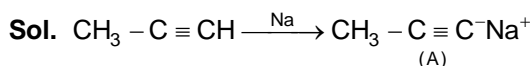
4-Methylpent-2-enal

71. Compound A formed in the following reaction reacts with B gives the product C. Find out A and B.



- (1) A =  $\text{CH}_3 - \text{C} \equiv \text{C}^- \text{Na}^+$ , B =  $\text{CH}_3 - \text{CH}_2 - \text{CH}_2 - \text{Br}$   
 (2) A =  $\text{CH}_3 - \text{C} \equiv \text{C}^- \text{Na}^+$ , B =  $\text{CH}_3 - \text{CH}_2 - \text{CH}_3$   
 (3) A =  $\text{CH}_3 - \text{CH}_2 - \text{CH}_3$ , B =  $\text{CH}_3 - \text{C} \equiv \text{CH}$   
 (4) A =  $\text{CH}_3 - \text{CH} = \text{CH}_2$ , B =  $\text{CH}_3 - \text{CH}_2 - \text{CH}_2 - \text{Br}$

**Answer (1)**



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72. Choose the correct statements from the following :

- (A) Ethane-1, 2-diamine is a chelating ligand.
- (B) Metallic aluminium is produced by electrolysis of aluminium oxide in presence of cryolite.
- (C) Cyanide ion is used as ligand for leaching of silver.
- (D) Phosphine act as a ligand in Wilkinson catalyst.
- (E) The stability constants of  $\text{Ca}^{2+}$  and  $\text{Mg}^{2+}$  are similar with EDTA complexes.

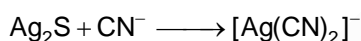
Choose the correct answer from the options given below :

- (1) (C), (D), (E) only      (2) (A), (B), (C) only
- (3) (A), (D), (E) only      (4) (B), (C), (E) only

**Answer (2)**

**Sol.** (A)  $\text{H}_2\text{N} - \text{CH}_2 - \text{CH}_2 - \text{NH}_2$  is a chelating ligand.

- (B) Aluminium is extracted by electrolysis of  $\text{Al}_2\text{O}_3$  in the presence of cryolite.
- (C) Cyanide ion form complex with silver



(A), (B) and (C) are true.

73. Given below are two statements.

**Statement (I) :** The orbitals having same energy are called as degenerate orbitals.

**Statement (II) :** In hydrogen atom, 3p and 3d orbitals are not degenerate orbitals.

In the light of the above statements, choose the most appropriate answer from the options given below :

- (1) Both **Statement I** and **Statement II** are true
- (2) Both **Statement I** and **Statement II** are false
- (3) **Statement I** is true but **Statement II** is false
- (4) **Statement I** is false but **Statement II** is true

**Answer (3)**

**Sol.** In hydrogen 3s, 3p and 3d orbitals have same energy.

74. Given below are two statements : one is labelled as **Assertion (A)** and the other is labelled as **Reason (R)**.

**Assertion (A) :**  $\text{CH}_2 = \text{CH} - \text{CH}_2 - \text{Cl}$  is an example of allyl halide.

**Reason (R) :** Allyl halides are the compounds in which the halogen atom is attached to  $\text{sp}^2$  hybridised carbon atom.

In the light of the above statements, choose the **most appropriate** answer from the options given below :

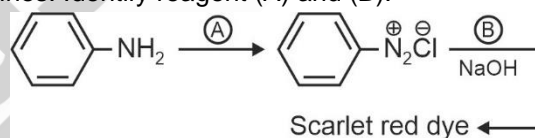
- (1) Both **(A)** and **(R)** are true and **(R)** is the correct explanation of **(A)**
- (2) **(A)** is false but **(R)** is true
- (3) **(A)** is true but **(R)** is false
- (4) Both **(A)** and **(R)** are true but **(R)** is not the correct explanation of **(A)**

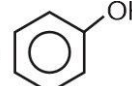
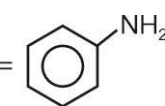
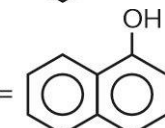

**Answer (3)**

**Sol.**  $\text{CH}_2 = \text{CH} - \text{CH}_2^{\text{sp}^3} - \text{Cl}$  is allyl halide.

Halogen is attached to  $\text{sp}^3$  hybridised carbon in allyl halide.

75. Following is a confirmatory test for aromatic primary amines. Identify reagent (A) and (B).



- (1)  $\text{A} = \text{HNO}_3/\text{H}_2\text{SO}_4$ ;  $\text{B} =$  
- (2)  $\text{A} = \text{NaNO}_2 + \text{HCl}, 0 - 5^\circ\text{C}$ ;  $\text{B} =$  
- (3)  $\text{A} = \text{NaNO}_2 + \text{HCl}, 0 - 5^\circ\text{C}$ ;  $\text{B} =$  
- (4)  $\text{A} = \text{NaNO}_2 + \text{HCl}, 0 - 5^\circ\text{C}$ ;  $\text{B} =$  

**Answer (4)**



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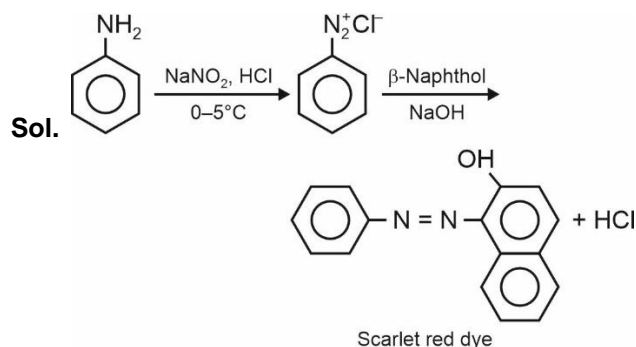
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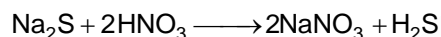
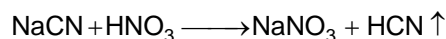
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76. The Lassaigne's extract is boiled with dil.  $\text{HNO}_3$  before testing for halogens because,
- (1) Silver halides are soluble in  $\text{HNO}_3$
  - (2)  $\text{Ag}_2\text{S}$  is soluble in  $\text{HNO}_3$
  - (3)  $\text{Na}_2\text{S}$  and  $\text{NaCN}$  are decomposed by  $\text{HNO}_3$
  - (4)  $\text{AgCN}$  is soluble in  $\text{HNO}_3$

**Answer (3)**

**Sol.** The Lassaigne's extract is boiled with dil.  $\text{HNO}_3$  because it decomposes  $\text{Na}_2\text{S}$  and  $\text{NaCN}$ , if formed



77. Given below are two statements : one is labelled as **Assertion (A)** and the other is labelled as **Reason (R)**.

**Assertion (A) :** There is a considerable increase in covalent radius from N to P. However from As to Bi only a small increase in covalent radius is observed.

**Reason (R) :** Covalent and ionic radii in a particular oxidation state increases down the group.

In the light of the above statements, choose the **most appropriate** answer from the options given below :

- (1) Both **(A)** and **(R)** are true and **(R)** is not the correct explanation of **(A)**
- (2) **(A)** is true but **(R)** is false
- (3) Both **(A)** and **(R)** are true but **(R)** is the correct explanation of **(A)**
- (4) **(A)** is false but **(R)** is true

**Answer (1)**

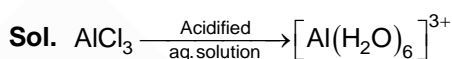
**Sol.** There is considerable increase in covalent radius from N to P. However from As to Bi increment in covalent radii is very small due to presence of *d* and *f* orbital electron results in increase in effective nuclear charge.

Covalent and ionic radius at particular oxidation state generally increases down the group, due to increase in shell number.

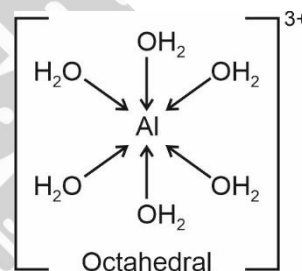
78. Aluminium chloride in acidified aqueous solution forms an ion having geometry

- (1) Octahedral
- (2) Tetrahedral
- (3) Square planar
- (4) Trigonal bipyramidal

**Answer (1)**



Hybridisation of  $\text{Al}^{3+}$  in  $[\text{Al}(\text{H}_2\text{O})_6]^{3+}$  is  $sp^3d^2$  and geometry is octahedral.



79. What happens to freezing point of benzene when small quantity of naphthalene is added to benzene?

- (1) First decreases and then increases
- (2) Increases
- (3) Decreases
- (4) Remains unchanged

**Answer (3)**

**Sol.** When small quantity of naphthalene is added to benzene freezing point decreases due to decrease in vapour pressure of solution.

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80. Which of the following molecule/species is most stable?



**Answer (1)**

**Sol.** The compound cyclopropenium ion is most stable, because it is an aromatic compound



⇒ Aromatic



⇒ Anti aromatic



⇒ Anti aromatic



⇒ Non aromatic

### SECTION - B

**Numerical Value Type Questions:** This section contains 10 Numerical based questions. Attempt any 5 questions out of 10. The answer to each question should be rounded-off to the nearest integer.

81. On a thin layer chromatographic plate, an organic compound moved by 3.5 cm, while the solvent moved by 5 cm. The retardation factor of the organic compound is \_\_\_\_\_  $\times 10^{-1}$ .

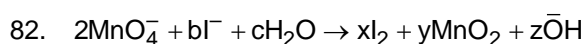
**Answer (7)**

**Sol.** Retardation factor =  $\frac{\text{Distance travelled by solute}}{\text{Distance travelled by solvent}}$

$$R_f = \frac{3.5}{5} = 0.7$$

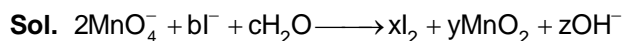
$$= 7 \times 10^{-1}$$

$$\text{Ans} = 7$$

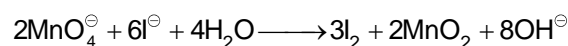


If the above equation is balanced with integer coefficients, the value of z is \_\_\_\_\_.

**Answer (8)**



Balanced chemical reaction is



$$z = 8$$

83. 0.05 cm thick coating of silver is deposited on a plate of 0.05 m<sup>2</sup> area. The number of silver atoms deposited on plate are \_\_\_\_\_  $\times 10^{23}$ . (At mass Ag = 108, d = 7.9 g cm<sup>-3</sup>)

**Answer (11)**

**Sol.** Given density of silver coating = 7.9 g/cm<sup>3</sup>

$$\begin{aligned} \text{Volume of silver coating} &= 0.05 \times 10^4 \text{ cm}^2 \times 0.05 \text{ cm} \\ &= 25 \text{ cm}^3 \end{aligned}$$

$$d = \frac{\text{Mass of silver coating}}{\text{Volume of silver coating}}$$

$$7.9 = \frac{\text{Mass of silver coating}}{25 \text{ cm}^3}$$

$$\begin{aligned} \text{Mass of silver coating} &= 7.9 \times 25 \text{ g} \\ &= 197.5 \text{ g} \end{aligned}$$

$$\text{Moles of silver coating} = \frac{197.5}{108} = 1.83 \text{ mol}$$

$$\begin{aligned} \text{Atoms of silver} &= 1.83 \times 6.022 \times 10^{23} \\ &= 11.02 \times 10^{23} \end{aligned}$$

$$\text{Ans} = 11$$



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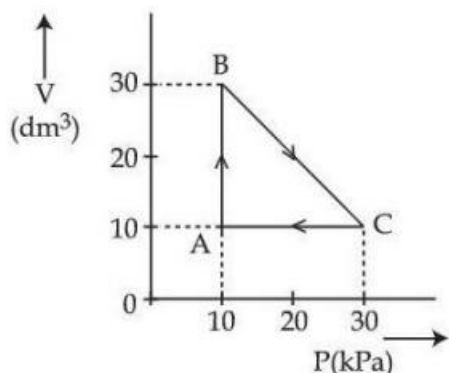
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84.



An ideal gas undergoes a cyclic transformation starting from the point A and coming back to the same point by tracing the path  $A \rightarrow B \rightarrow C \rightarrow A$  as shown in the diagram above. The total work done in the process is \_\_\_\_\_ J.

**Answer (200)**

**Sol.** Work done = Area under curve

$$\text{Work done} = \frac{1}{2} \times AC \times AB$$

$$1 \text{ dm}^3 = 0.001 \text{ m}^3$$

$$AB = 20 \text{ dm}^3 = 0.02 \text{ m}^3$$

$$1 \text{ kPa} = 1000 \text{ Nm}^{-2}$$

$$20 \text{ kPa} = 20000 \text{ Nm}^{-2}$$

$$\begin{aligned} \text{Work done} &= \frac{1}{2} \times 0.02 \times 20000 \text{ J} \\ &= 200 \text{ J} \end{aligned}$$

85. The mass of sodium acetate ( $\text{CH}_3\text{COONa}$ ) required to prepare 250 mL of 0.35 M aqueous solution is \_\_\_\_\_ g. (Molar mass of  $\text{CH}_3\text{COONa}$  is 82.02 g  $\text{mol}^{-1}$ )

**Answer (7)**

**Sol.** Given volume of solution = 250 mL

$$\text{Molarity of solution of } \text{CH}_3\text{COONa} = 0.35 \text{ M}$$

$$\text{Molarity} = \frac{\text{Moles of } \text{CH}_3\text{COONa}}{\text{Volume of solution (in mL)}} \times 1000$$

$$0.35 = \frac{\text{Moles of } \text{CH}_3\text{COONa}}{250} \times 1000$$

$$\text{Moles of } \text{CH}_3\text{COONa} = \frac{0.35 \times 250}{1000}$$

$$= 0.0875 \text{ mol}$$

$$\begin{aligned} \text{Mass of } \text{CH}_3\text{COONa} &= 0.0875 \times 82.02 \text{ g} \\ &= 7.18 \text{ g} \end{aligned}$$

86. If IUPAC name of an element is "Unununnium" then the element belongs to  $n^{\text{th}}$  group of Periodic table. The value of  $n$  is \_\_\_\_\_.

**Answer (11)**

**Sol.** IUPAC name given is Unununnium

$$\text{un} = 1$$

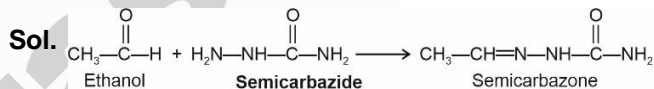
$$\text{un} = 1$$

$$\text{un} = 1$$

Atomic number is 111 belongs to group  $11^{\text{th}}$ .

87. The compound formed by the reaction of ethanal with semicarbazide contains \_\_\_\_\_ number of nitrogen atoms.

**Answer (3)**



When ethanal reacts with semicarbazide, semicarbazone is formed via condensation, number of nitrogen atoms present in product is 3.

88. The total number of molecular orbitals from 2s and 2p atomic orbitals of a diatomic molecule is \_\_\_\_\_.

**Answer (8)**

**Sol.** 2s – 2s combine to form two molecular orbitals  $\sigma_{2s}$  and  $\sigma_{2s}^*$

2p – 2p combine to form 6 molecular orbital

$$\sigma_{2p_z}, \sigma_{2p_z}^*, \pi_{2p_x}, \pi_{2p_y}, \pi_{2p_x}^*, \pi_{2p_y}^*$$

Total molecular orbitals formed are 6 + 2

$$= 8$$

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89. The rate of First order reaction is  $0.04 \text{ mol L}^{-1} \text{ s}^{-1}$  at 10 minutes and  $0.03 \text{ mol L}^{-1} \text{ s}^{-1}$  at 20 minutes after initiation. Half life of the reaction is \_\_\_\_\_ minutes. (Given  $\log 2 = 0.3010$ ,  $\log 3 = 0.4771$ )

**Answer (24)**

**Sol.** Rate of first order reaction =  $0.04 \text{ mol L}^{-1} \text{ s}^{-1}$  at time = 10 min

Rate of first order reaction =  $0.03 \text{ mol L}^{-1} \text{ s}^{-1}$  at time = 20 min

$$r_1 = 0.04 \text{ mol L}^{-1} \text{ s}^{-1}$$

$$r_2 = 0.03 \text{ mol L}^{-1} \text{ s}^{-1}$$

$$t_1 = 10 \text{ min}$$

$$t_2 = 20 \text{ min}$$

$$k = \frac{2.303}{t_2 - t_1} \log \frac{r_1}{r_2}$$

$$k = \frac{2.303}{10} \log \frac{0.04}{0.03}$$

$$k = 0.02876 \text{ min}^{-1}$$

$$t_{\frac{1}{2}} = \frac{0.693}{k} = \frac{0.693}{0.02876} = 24.09$$

$\approx 24 \text{ min}$

90. The pH at which  $\text{Mg}(\text{OH})_2$  [ $K_{sp} = 1 \times 10^{-11}$ ] begins to precipitate from a solution containing  $0.10 \text{ M}$   $\text{Mg}^{2+}$  ions is \_\_\_\_\_.

**Answer (9)**

**Sol.**  $\text{Mg}(\text{OH})_2(\text{s}) \rightleftharpoons \text{Mg}^{+2}(\text{aq}) + 2\text{OH}^{-}(\text{aq})$

At limiting condition, for precipitation to be start  $K_{sp} = Q_{sp}$

$$K_{sp} = [\text{Mg}^{+2}] [\text{OH}^{-}]^2$$

$$1 \times 10^{-11} = [0.1] [\text{OH}^{-}]^2$$

$$[\text{OH}^{-}] = \frac{10^{-11}}{0.1}$$

$$10^{-10} = [\text{OH}^{-}]^2$$

$$[\text{OH}^{-}] = 10^{-5} \text{ M}$$

$$\text{pOH} = -\log [\text{OH}^{-}]$$

$$= 5$$

$$\text{pH} = 14 - 5$$

$$= 9$$



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