



# Aakash

Medical | IIT-JEE | Foundations

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MM : 180

AIATS For One Year JEE(Advanced)-2026 (XII Studying)\_Test-2A\_Paper-2\_ONLINE

Time : 180 Min.

**CHEMISTRY****Section-I**

1. (B)
2. (A)
3. (C)
4. (C)

5. (A,C,D)
6. (A,C,D)
7. (B,D)

**Section-II****Section-III**

8. (18)
9. (3)
10. (2)
11. (0)
12. (5)
13. (6)

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**Section-IV**

14. (00.00)
15. (01.00)
16. (01.00)
17. (09.00)

**MATHEMATICS****Section-I**

18. (D)
19. (C)
20. (A)

21. (B)

**Section-II**

22. (A,B,C,D)

23. (B,C)

24. (A,D)

**Section-III**

25. (B)

26. (0)

27. (2)

28. (0)

29. (2)

30. (2)

**Section-IV**

31. (63.00)

32. (02.00)

33. (01.00)

34. (00.00)



PHYSICS

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**Section-I**

35. (D)

36. (D)

37. (C)

38. (A)

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**Section-II**

39. (A,B,C)

40. (A,C)

41. (A,C)

**Section-III**

42. (16)

43. (6)

44. (0)

45. (15)

46. (10)

47. (52)

Section-IV

- 48. (00.75)
- 49. (06.00)
- 50. (90.00)
- 51. (67.50)



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## Hints and Solutions

## CHEMISTRY

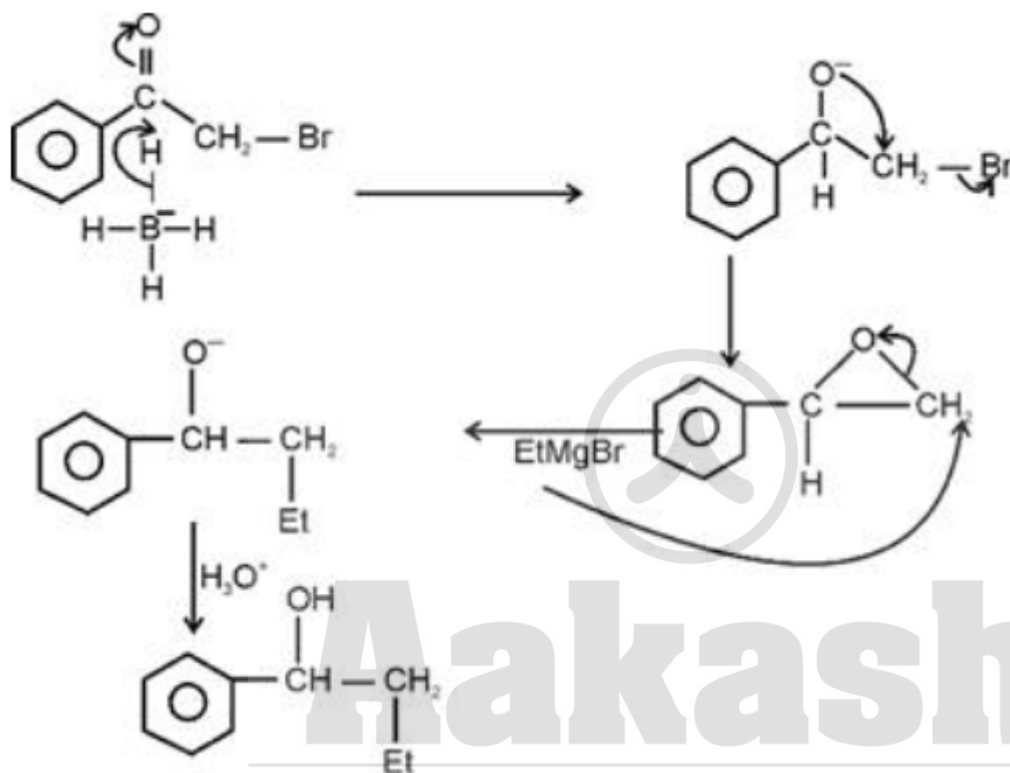
## Section-I

(1) Answer : (B)

Hint:

Ring opening of less hindered C-atom

Solution:

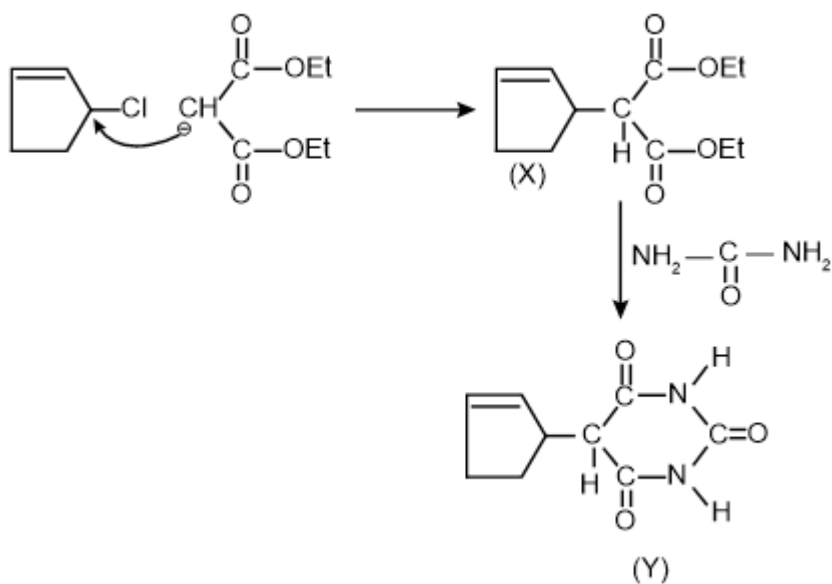


(2) Answer : (A)

Hint:

It is  $\text{S}_{\text{N}}2$  reaction

Solution:



(3) Answer : (C)

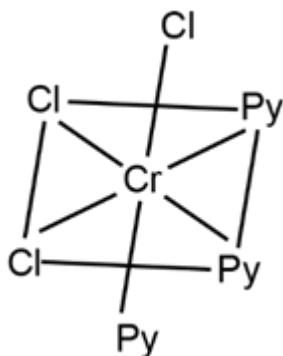
**Hint:**

$\text{Ni}(\text{dmg})_2$  is square planar.

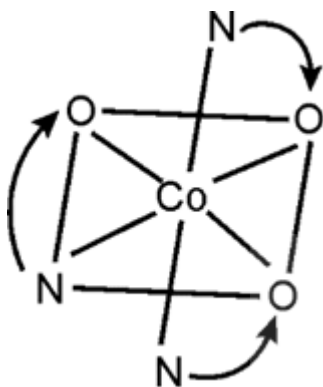
**Solution:**

$\text{Ni}(\text{dmg})_2$  is square planar.  $[\text{Ni}(\text{dmg})_2]$  is a square planar complex

So no optical isomerism.



Fac- $[\text{CrCl}_3(\text{Py})_3]$  has plane of symmetry



trans  $[\text{Co}(\text{gly})_3]$  has chirality-exists as d-l pair

$\Rightarrow [\text{Zn}(\text{en})(\text{gly})]\text{Cl}$  is tetrahedral complex lacking chirality

(4) Answer : (C)

**Hint:**

Symmetrical molecules have compact packing and hence higher melting point.

**Solution:**

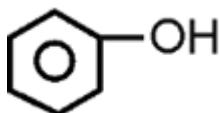
Compound	M. pt.
Phenol	43°C
Catechol	105°C
Resorcinol	110°C
Quinol	170°C

**Section-II**

(5) Answer : (A,C,D)

**Hint:**

Phenol is most acidic.

**Solution:**

does not react with HCl, but it is soluble in NaOH. It decolorises  $\text{Br}_2$  water.

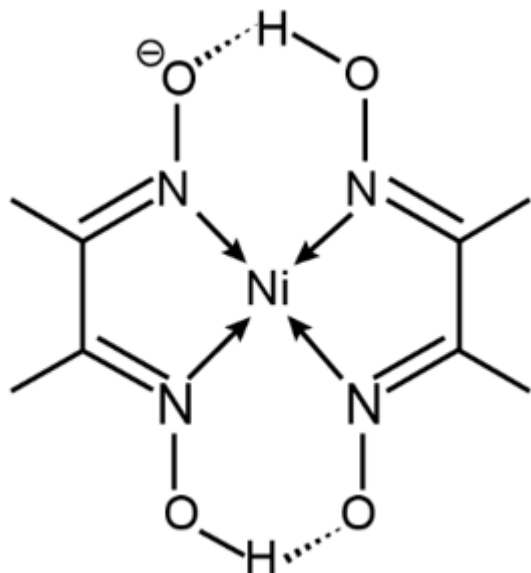
(6) Answer : (A,C,D)

**Hint:**

CFSE depends on metal and ligands both

**Solution:**

As one moves from Ni  $\rightarrow$  Pd  $\rightarrow$  Pt, keeping the ligand same,  $\Delta_0$  (crystal field splitting energy increases)



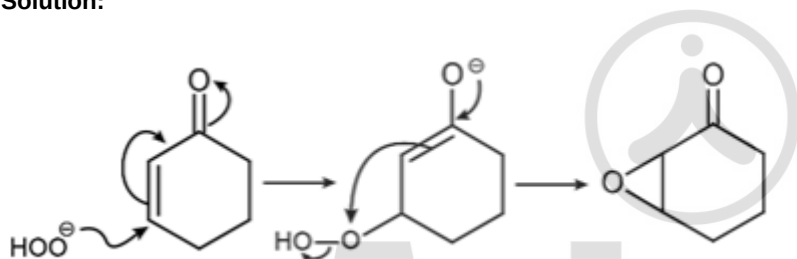
dmg is stronger ligand than en – one of the reason is formation of rings due to intramolecular H-boding.

(7) Answer : (B,D)

Hint:

1, 4-addition.

Solution:



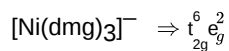
$\Rightarrow \text{H}_2\text{O}_2 \text{ H}_2\text{O}$   
 $\text{pK}_a = 11.6 \text{ pK}_a = 15.4$

(8) Answer : 18

Hint:

$sp^3d^2$  hybridised

Solution:



$$k = 6$$

$$l = 2$$

$$\text{So, } \frac{4 \times 6^2}{2^3} = 18$$

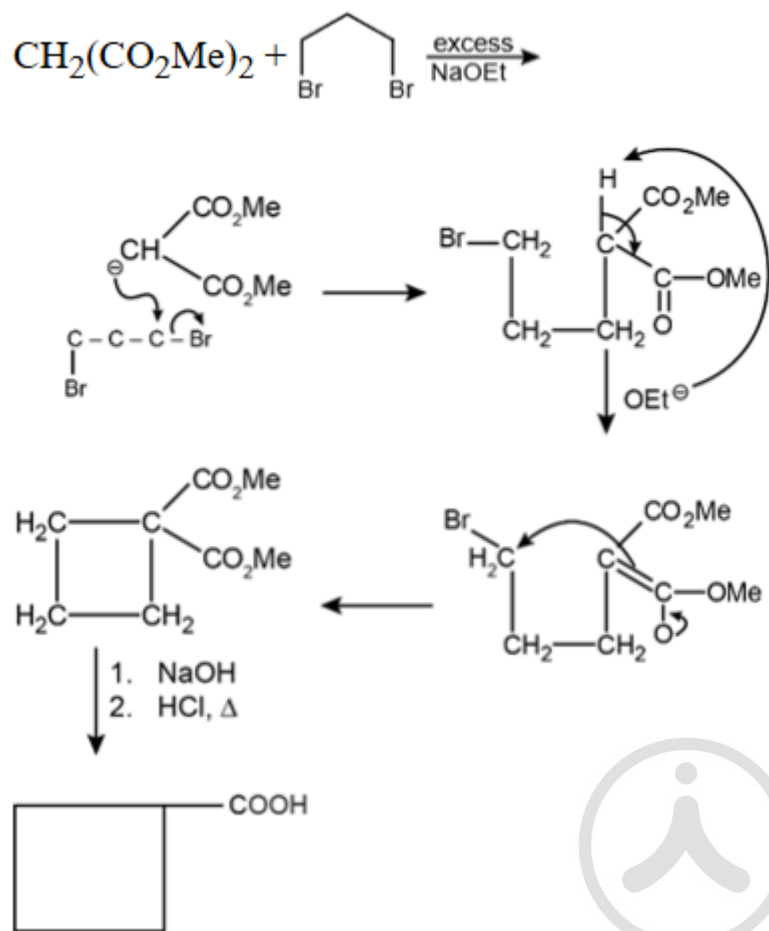
(9) Answer : 3

Hint:

$\text{CH}_2(\text{CO}_2\text{Me})_2$  contains acidic H.

Solution:

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Number of  $sp^3$  hybridised C = 4 = x

Degree of unsaturation = 2 = y

So,  $x + y = 6$

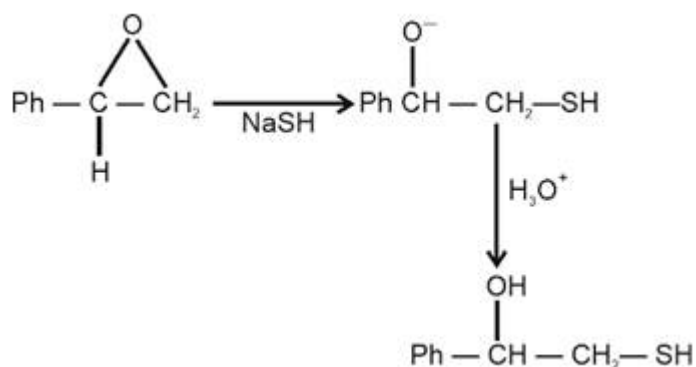
So,  $1 + \frac{x}{y} = 1 + \frac{4}{2} = 3$

(10) Answer : 2

Hint:

Ring opening takes place at less hindered C-atom.

Solution:

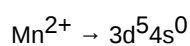
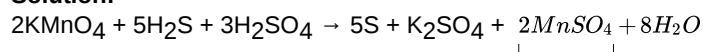


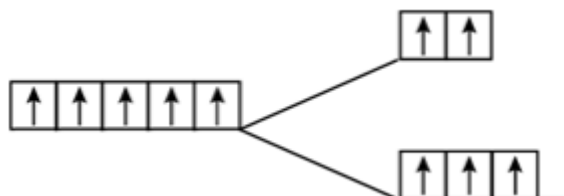
(11) Answer : 0

Hint:

It is  $t_{2g}^3 e_g^2$  complex.

Solution:





$$\text{CFSE} = -3 \times 0.4\Delta_0 + 2 \times 0.6\Delta_0$$

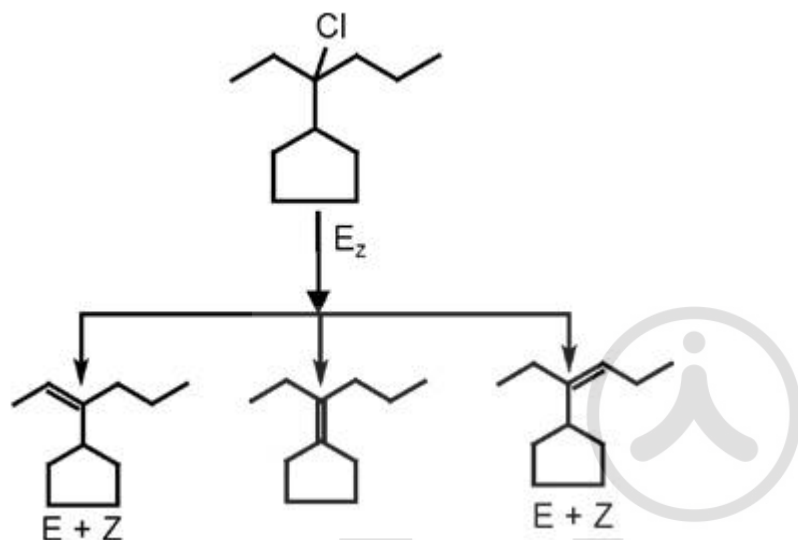
$$= 0$$

(12) Answer : 5

Hint:

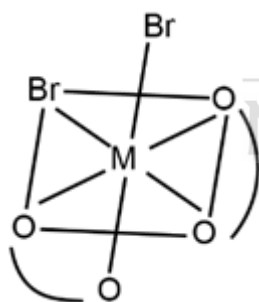
5 isomers are formed.

Solution:



(13) Answer : 6

Solution:

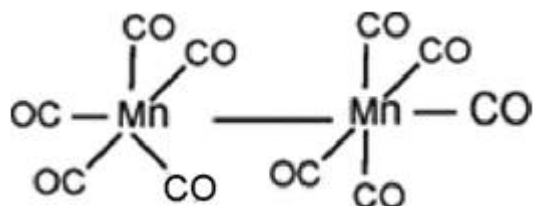


For each of two Br-atoms 3 such angles are possible.

#### Section-IV

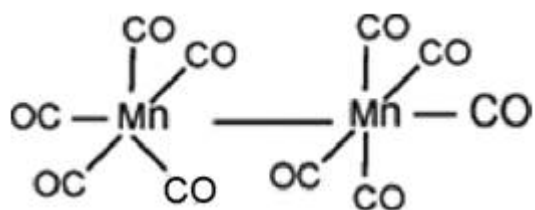
(14) Answer : 00.00

Solution:



(15) Answer : 01.00

Solution:



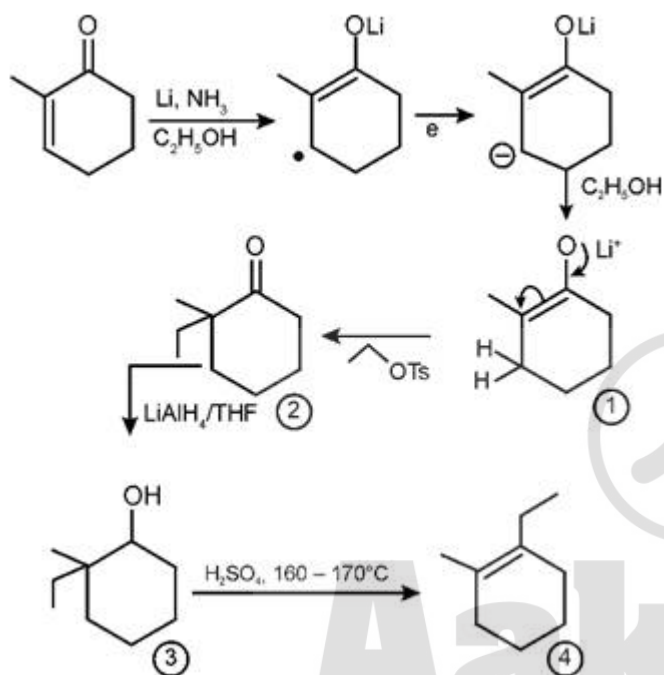
Number of M – M bond = 1.

(16) Answer : 01.00

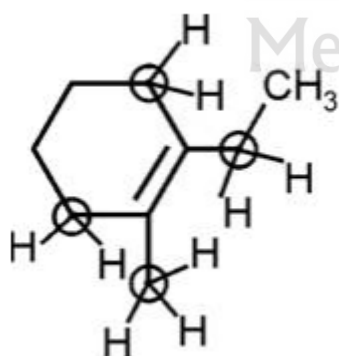
**Hint:**

nucleophilic addition

**Solution:**



Double bond equivalent of (3) is 1. Hyperconjugative hydrogen atoms in (4) is (9)

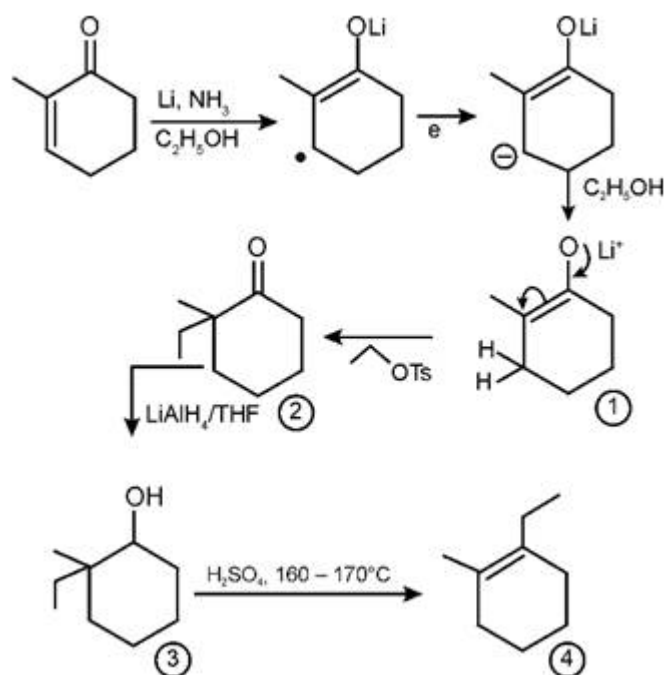


(17) Answer : 09.00

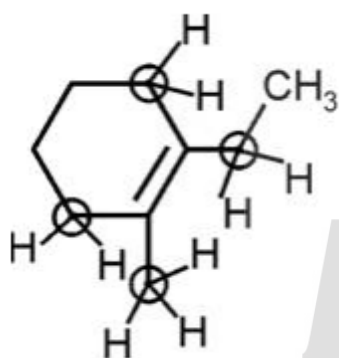
**Hint:**

Nucleophilic addition

**Solution:**



Double bond equivalent of (3) is 1 Hyperconjugative hydrogen atoms in (4) is (9)



  
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MATHEMATICS

Section-I

(18) Answer : (D)

Hint:

Let  $x + 1 = t$

Solution:

Let  $x + 1 = t$

$dx = dt$

$$= \int_1^e \frac{e^{\frac{(t-1)^2 + 2(t-1) - 1}{2}}}{t} dt + \int_1^e x \log x e^{\frac{x^2-2}{2}} dx$$

$$= \int_1^e \frac{e^{\frac{x^2-2}{2}}}{x} dx + \int_1^e x \log x e^{\frac{x^2-2}{2}} dx$$

$$= e^{\frac{x^2-2}{2}} \int_1^e \frac{dx}{x} + \int_1^e \left( \frac{d}{dx} \left( e^{\frac{x^2-2}{2}} \right) \int_1^e \frac{1}{x} dx \right) dx +$$

$$\begin{aligned}
 & \int_1^e x \log x e^{\frac{x^2-2}{2}} dx \\
 &= \left[ e^{\frac{x^2-2}{2}} \log |x| \right]_1^e - \int_1^e e^{\frac{x^2-2}{2}} \cdot x \log x \\
 &+ \int_1^e x \log x e^{\frac{x^2-2}{2}} \\
 &= e^{\frac{e^2-2}{2}} \log e \\
 &= e^{\frac{e^2-2}{2}} = (\sqrt{e})^{e^2-2}
 \end{aligned}$$

(19) Answer : (C)

Hint:

$$f(x) = \tan \frac{x}{2} + 4$$

Solution:

$$\int \frac{dx}{1 + \cos x} = \int \frac{dx}{2\cos^2 \frac{x}{2}} = \int \frac{1}{2} \sec^2 \frac{x}{2} dx$$

$$f(x) = \int \frac{1}{2} \sec^2 \frac{x}{2} dx$$

$$= \tan \frac{x}{2} + C$$

$$f(0) = 4$$

$$\Rightarrow C = 4$$

$$\therefore f(x) = \tan \frac{x}{2} + 4$$

$$f\left(\frac{\pi}{2}\right) = \tan\left(\frac{\pi}{4}\right) + 4 = 1 + 4 = 5$$

(20) Answer : (A)

Hint:

$$h'(x) = f'(x) - g'(1-x) \geq 0$$

Solution:

$$h'(x) = f'(x) - g'(1-x) \geq 0$$

$$\Rightarrow f'(x) - f''(x) \geq 0$$

$$\Rightarrow \frac{d}{dx} (e^{-x} f'(x)) \leq 0$$

$$\Rightarrow e^{-x} f'(x) \text{ is decreasing function}$$

$$\Rightarrow e^{-x} f'(x) \leq e^{-0} f'(0) \text{ for } x \geq 0$$

$$\Rightarrow f'(x) \leq 0 \quad \forall x \geq 0.$$

$$\therefore g'(1-x) \leq 0 \quad \forall x \geq 0$$

(21) Answer : (B)

Hint:

$$\text{write, } 3x^2 + 4x - 1 = 4x^2 + 4x - x^2 - 1$$

Solution:

$$\int \frac{3x^2 + 4x - 1}{(x^2 + 1)\sqrt{x+1}} dx = \int \frac{4x^2 + 4x - x^2 - 1}{(x^2 + 1)^2 \sqrt{x+1}} dx$$

$$= 4 \int \frac{x(x+1)dx}{(x^2+1)^2 \sqrt{x+1}} - \int \frac{dx}{(x^2+1)\sqrt{x+1}}$$

$$= 4 \int \frac{x(x+1)dx}{(x^2+1)^2 \sqrt{x+1}} - \frac{2\sqrt{x+1}}{x^2+1}$$

$$= \frac{-2\sqrt{x+1}}{x^2+1} + C$$

## Section-II

(22) Answer : (A,B,C,D)

Hint:

$$\frac{dy}{dx} = \frac{1}{3x^{2/3}} [4x-1]$$

Solution:

$$y = x^{1/3} (x-1)$$

$$\frac{dy}{dx} = \frac{4}{3}x^{\frac{1}{3}} - \frac{1}{3} \cdot \frac{1}{x^{2/3}} = \frac{1}{3x^{2/3}} [4x - 1]$$

Hence function is increasing for  $x > \frac{1}{4}$  and decreasing for  $x < \frac{1}{4}$ .

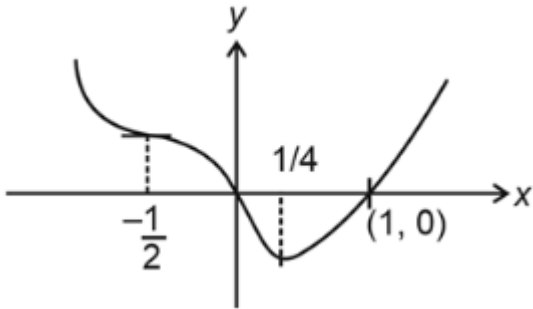
$\therefore x = \frac{1}{4}$  is the point of minima.

$f'(0)$  does not exist as  $f(x)$  is a vertical tangent here.

$$f''(x) = \frac{4}{9} \cdot \frac{1}{x^{2/3}} + \frac{1}{3} \cdot \frac{2}{3} \cdot \frac{1}{x^{5/3}}$$

$$= \frac{2}{9x^{2/3}} \left[ 2 + \frac{1}{x} \right] = \frac{2}{9x^{2/3}} \left[ \frac{2x+1}{x} \right]$$

$f''(x) = 0$  at  $x = -\frac{1}{2}$  (inflection point)



(23) Answer : (B,C)

Hint:

$$\Rightarrow e^{-f(x)} f'(x) - e^{-g(x)} g'(x) = 0$$

Solution:

$$f'(x) = (e^{f(x)-g(x)}) g'(x) \quad \forall x \in \mathbb{R}$$

$$\Rightarrow e^{-f(x)} f'(x) - e^{-g(x)} g'(x) = 0$$

$$\Rightarrow \int (e^{-f(x)} f'(x) - e^{-g(x)} g'(x)) dx = C$$

$$\Rightarrow -e^{-f(x)} + e^{-g(x)} = C$$

$$\Rightarrow -e^{-f(1)} + e^{-g(1)} = -e^{-f(2)} + e^{-g(2)}$$

$$\Rightarrow -\frac{1}{e} + e^{-g(1)} = -e^{-f(2)} + \frac{1}{e}$$

$$\Rightarrow e^{-f(2)} + e^{-g(1)} = \frac{2}{e}$$

$$\therefore e^{-f(2)} < \frac{2}{e} \text{ \& } e^{-g(1)} < \frac{2}{e}$$

$$\Rightarrow -f(2) < \ln 2 - 1 \text{ \& } -g(1) < \ln 2 - 1$$

$$\Rightarrow f(2) > 1 - \ln 2 \text{ \& } g(1) > 1 - \ln 2$$

(24) Answer : (A,D)

Hint:

$$I_n + I_{n-2} = \frac{1}{n-1}$$

Solution:

$$I_n = \int_0^{\pi/4} \tan^n x \, dx, \text{ when } n \text{ is even}$$

$$I_n = \frac{\tan^{n-1} x}{n-1} \Big|_0^{\pi/4} - I_{n-2}$$

$$\Rightarrow I_n + I_{n-2} = \frac{1}{n-1}$$

$$I_4 = \frac{\tan^3 x}{3} \Big|_0^{\pi/4} - (\tan x - x) \Big|_0^{\pi/4}$$

$$= \frac{1}{3} - \left(1 - \frac{\pi}{4}\right) = \frac{\pi}{4} - \frac{2}{3}$$

### Section-III

(25) Answer : B

Hint:

$$f(x) = \cos x$$

Solution:

$$f(x) = \lim_{\theta \rightarrow 0} \frac{(\cos(x+4\theta) + \cos x) - 4(\cos(x+3\theta) + \cos(x+\theta)) + 6\cos(x+2\theta)}{\theta^4}$$

$$= \lim_{\theta \rightarrow 0} \frac{2\cos(x+2\theta) \cdot \cos 2\theta - 8\cos(x+2\theta) \cdot \cos \theta + 6\cos(x+2\theta)}{\theta^4}$$

$$= \lim_{\theta \rightarrow 0} \frac{2\cos(x+2\theta) \cdot ((\cos 2\theta) - 4\cos \theta + 3)}{\theta^4}$$

$$= \lim_{\theta \rightarrow 0} \frac{2\cos(x+2\theta) (2\cos^2 \theta - 4\cos \theta + 2)}{\theta^4}$$

$$\lim_{\theta \rightarrow 0} 4\cos(x+2\theta) \frac{(1-\cos \theta)^2}{\theta^4} = \cos x$$

Maximum value of  $f(x) = 1$  and minimum value of  $f(x) = -1$   
 $\therefore$  Difference =  $1 - (-1) = 2$

(26) Answer : 0

Hint:

$$x = \frac{1}{t} \Rightarrow dx = \frac{-dt}{t^2}$$

Solution:

$$I = \int_{\frac{1}{5}}^5 \frac{1}{x} \left\{ \frac{x}{4x^2-2x+9} \right\} dx + \int_{\frac{1}{5}}^5 \frac{1}{x} \left\{ \frac{-x}{9x^2-2x+4} \right\} dx$$

$$\underbrace{\hspace{10em}}_{I_1} \quad \underbrace{\hspace{10em}}_{I_2}$$

$$I_2 = \int_{1/5}^5 \frac{1}{x} \left\{ \frac{-x}{9x^2-2x+4} \right\} dx$$

Putting  $x = \frac{1}{t} \Rightarrow dx = \frac{-dt}{t^2}$

$$I_2 = \int_{1/5}^5 t \left\{ \frac{-1/t}{9/t^2 - 2/t + 4} \right\} \frac{dt}{t^2} = \int_{1/5}^5 \frac{1}{t} \left\{ \frac{-t}{4t^2 - 2t + 9} \right\} dt$$

Now,  $I_2 = -I_1$

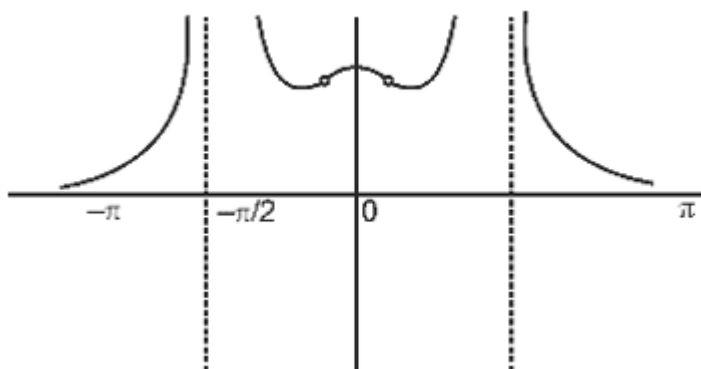
(27) Answer : 2

Hint:

Draw the graph

Solution:

Function is not differentiable in  $(-\pi, \pi)$  at exactly 2 points



(28) Answer : 0

Hint:

$$g' \left( \frac{x^2}{2} \right) - f'(6 - x^2) > 0 \text{ when } x < -2 \text{ or } x > 2$$

Solution:

$$g(x) = 2f \left( \frac{x^2}{2} \right) + f(6 - x^2)$$

$$\Rightarrow g'(x) = 2f' \left( \frac{x^2}{2} \right) x - 2xf'(6 - x^2)$$

$$\Rightarrow g'(x) = 2x \left( f' \left( \frac{x^2}{2} \right) - f'(6 - x^2) \right)$$

$$f' \left( \frac{x^2}{2} \right) > f'(6 - x^2) \quad \left( \text{if } \frac{x^2}{2} > 6 - x^2 \right)$$

$\therefore f'(x)$  is increasing

$$\frac{x^2}{2} > 6 - x^2 \Rightarrow x^2 > 4$$

$$\Rightarrow f' \left( \frac{x^2}{2} \right) - f'(6 - x^2) > 0 \quad \text{when } x < -2 \text{ or } x > 2$$

$$\Rightarrow g'(x) > 0 \quad \text{when } x \in (-2, 0) \cup (2, \infty)$$

$$\Rightarrow [a + b + c] = 0$$

(29) Answer : 2

Hint:

$$\text{Put } 1 + \cot^5 x = t$$

Solution:

$$I = \int \frac{\cos^4 x \, dx}{\sin^3 x (\sin^5 x + \cos^5 x)^{3/5}}$$

$$= \int \frac{\cos^4 x \, dx}{\sin^6 x (1 + \cot^5 x)^{3/5}} \quad \{ \text{put } 1 + \cot^5 x = t \}$$

$$= -\frac{1}{5} \int \frac{dt}{t^{3/5}}$$

$$= -\frac{1}{2} (1 + \cot^5 x)^{2/5} + C$$

$$\therefore AB = 5 \times \frac{2}{5} = 2$$

(30) Answer : 2

Hint:

$$\sin 3\theta = 3\sin\theta - 4\sin^3\theta = \sin\theta(1 + 2\cos 2\theta)$$

Solution:

$$\sin 3\theta = 3\sin\theta - 4\sin^3\theta = \sin\theta(1 + 2\cos 2\theta)$$

$$\Rightarrow \sin x = \sin \frac{x}{3} \left( 1 + 2\cos \frac{2x}{3} \right)$$

$$\sin \frac{x}{3} = \sin \left( \frac{x}{3^2} \right) \left( 1 + 2\cos \frac{2x}{3^2} \right) \quad \& \text{ So on multiplying all}$$

$$\sin x = \sin \left( \frac{x}{3^n} \right) \prod_{r=1}^n \left( 1 + 2\cos \frac{2x}{3^r} \right)$$

$$\Rightarrow \frac{\sin x}{x} = \lim_{n \rightarrow \infty} \frac{\sin \left( \frac{x}{3^n} \right)}{\left( \frac{x}{3^n} \right)} \cdot \prod_{r=1}^n \frac{\left( 1 + 2\cos \frac{2x}{3^r} \right)}{3}$$

$$\Rightarrow f(x) = \frac{\sin x}{x}$$

Thus  $|xf(x)| = |\sin x|$  is not differentiable at 2 points in  $(0, 3\pi)$

#### Section-IV

(31) Answer : 63.00

Hint:

$$\int_0^6 (x^2 + [x]) d(|3-x|) = \int_0^3 (x^2 + [x]) d(3-x) + \int_3^6 (x^2 + [x]) d(x-3)$$

Solution:

$$\int_0^6 (x^2 + [x]) d(|3-x|) = \int_0^3 (x^2 + [x]) d(3-x)$$

$$+ \int_3^6 (x^2 + [x]) d(x-3)$$

$$\begin{aligned}
 &= - \int_0^3 (x^2 + [x]) dx + \int_3^6 (x^2 + [x]) dx \\
 &\Rightarrow \int_0^6 (x^2 + [x]) d|3-x| = \\
 &= - \int_0^3 x^2 dx + \int_3^6 x^2 dx - \int_0^3 [x] dx + \int_3^6 [x] dx \\
 &= \left[ \frac{-x^3}{3} \right]_0^3 + \left[ \frac{x^3}{3} \right]_3^6 - \int_0^3 [x] dx + \int_3^6 [x] dx \\
 &= -9 + (72 - 9) + 3 + 12 \\
 &= 63
 \end{aligned}$$

(32) Answer : 02.00

Hint:

$$\int_{-2}^3 [|x|] dx = \int_{-2}^0 [-x] d(-x) + \int_0^3 [x] dx$$

Solution:

$$\begin{aligned}
 \int_{-2}^3 [|x|] dx &= \int_{-2}^0 [-x] d(-x) + \int_0^3 [x] dx \\
 &= - \int_{-2}^{-1} [-x] dx + \int_{-1}^0 [-x] dx + \int_0^3 [x] dx \\
 &= -1 + 3 = 2
 \end{aligned}$$

(33) Answer : 01.00

Hint:

$$f(x) \leq 0 \text{ and } F'(x) = f(x)$$

Solution:

$$f(x) \leq 0 \text{ and } F'(x) = f(x)$$

$$\Rightarrow f(x) \geq CF(x) \Rightarrow \frac{d}{dx} (e^{-Cx} \cdot F(x)) \geq 0$$

$$\Rightarrow e^{-Cx} F(x) \text{ is an increasing function}$$

$$\Rightarrow e^{-Cx} F(x) \geq e^{-(0)} F(0)$$

$$\Rightarrow F(x) \geq 0 \Rightarrow f(x) \geq 0$$

$$\Rightarrow f(x) = 0$$

$$\text{Also, } \frac{d}{dx} (e^{-x} g(x)) < 0$$

$$\Rightarrow e^{-x} g(x) \text{ is a decreasing function}$$

$$\Rightarrow e^{-x} g(x) < e^{-(0)} g(0)$$

$$\Rightarrow g(x) < 0 \text{ (as } g(0) = 0)$$

$$\therefore f(x) = g(x) \text{ has one solution } x = 0$$

(34) Answer : 00.00

Hint:

$$x^2 - x - 6 = (x - 2)(x + 3)$$

Solution:

$$|x^2 + x - 6| = f(x) + g(x)$$

$$x^2 + x - 6 = (x - 2)(x + 3)$$

Roots of this quadratic equation are  $x = 2$  and  $x = -3$ .

$$\text{For } 0 \leq x < 2, |x^2 + x - 6| = 6 - x^2 - x$$

$$x \geq 2, |x^2 + x - 6| = x^2 + x - 6$$

$$\therefore g(x) \leq 0 \text{ \& } g(0) = 0$$

$$\therefore f(x) + g(x) \leq g(x) \quad \forall x \geq 0$$

$$\text{For } 0 \leq x < 2$$

$$6 - x^2 - x \geq 0$$

This is positive, while  $f(x) + g(x) \leq 0$ .

No solution

For  $x \geq 2$

$$x^2 + x - 6 \geq 0$$

This is also positive, while  $f(x) + g(x) \leq 0$

No solution

PHYSICS

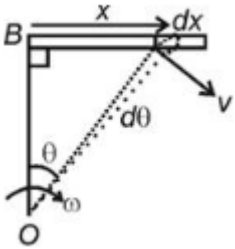
Section-I

(35) Answer : (D)

Hint:

$$E = Bvl$$

Solution:



$$\text{emf} = \int (d\vec{x} \times \vec{v}) \cdot \vec{B}$$

$$(d\vec{x} \times \vec{v}) = \omega r dx \sin \theta$$

$$(d\vec{x} \times \vec{v}) \cdot \vec{B} = B\omega (r \sin \theta) dx = B\omega x dx$$

$$E = \omega B \int_0^l x dx = \frac{B\omega l^2}{2}$$

(36) Answer : (D)

Hint:

$$I_0 = \frac{V}{\sqrt{R^2 + \left(\frac{1}{\omega_0 C}\right)^2}}$$

Solution:

$$\frac{I_0}{2} = \frac{v}{\sqrt{R^2 + \left(\frac{3}{\omega_0 C}\right)^2}}$$

$$4 \left( R^2 + \frac{1}{C^2 \omega^2} \right) = R^2 + \frac{9}{C^2 \omega^2}$$

$$\frac{1}{C^2 \omega^2} = \frac{3}{5} R^2$$

$$\frac{1}{\omega C R} = \sqrt{\frac{3}{5}}$$

$$\omega C R = \sqrt{\frac{5}{3}}$$

(37) Answer : (C)

Hint:

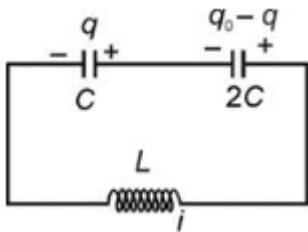
Oscillation

Solution:

$$\frac{q_0 - 2}{2C} - \frac{L di}{dt} - \frac{q}{C} = 0$$

$$q = \frac{q_0}{3}$$





$$\frac{1}{2}Li^2 + \frac{\left(\frac{2q_0}{3}\right)^2}{2 \times 2C} + \frac{\left(\frac{q_0}{3}\right)^2}{2C} = \frac{q_0^2}{2 \times 2C}$$

$$i = \frac{q_0}{\sqrt{6LC}}$$

(38) Answer : (A)

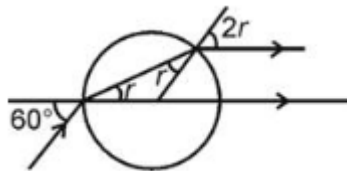
Hint:

$$\mu_1 \sin i = \mu_2 \sin r$$

Solution:

At  $\mu = \mu_{\min}$

Emergent ray must parallel to x-axis



$$1 \sin 60^\circ = \mu \sin r$$

$$\mu \sin r = 1 \sin 2r$$

$$\sin 2r = \sin 60^\circ$$

$$r = 30^\circ$$

$$\mu = \sqrt{3}$$



Section-II

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(39) Answer : (A,B,C)

Hint:

$$\frac{L di}{dt} + \frac{q}{C} = V$$

Solution:

$$\frac{L di}{dt} + \frac{q}{C} = V$$

$$\frac{L d^2 i}{dt^2} = \frac{i}{C}$$

$$i = i_0 \sin(\omega t) \quad \omega = \frac{1}{\sqrt{LC}}$$

$$q = \frac{i_0}{\omega} (1 - \cos \omega t)$$

$$q_{\max} \Rightarrow V q_{\max} = \frac{q_{\max}^2}{2C}$$

$$q_{\max} = 2CV$$

$$i_0 = q_0 \omega$$

$$i_0 = 2CV \cdot \frac{1}{\sqrt{LC}} = 2V \sqrt{\frac{C}{L}}$$

(40) Answer : (A,C)

Hint:

$$\theta_C = 30^\circ$$

Solution:

$$\theta_C = 30^\circ$$

$$\sin 30^\circ = \frac{\mu_1}{\mu_2}$$

$$\frac{\mu_1}{\mu_2} = \frac{1}{2}$$

$$\delta_{\max} = 180 - 2\theta_C$$

$$= 120^\circ$$

(41) Answer : (A,C)

Hint:

$$\frac{I}{C} = \frac{1}{2} \epsilon_0 E_0^2$$

**Solution:**

$$\frac{I}{C} = \frac{1}{2} \varepsilon_0 E_0^2$$

$$\frac{1 \times 10^3 \times 2}{6\pi \times 3 \times 10^8 \varepsilon_0} = E_0^2$$

$$\frac{4\pi \times 10^3 \times 2 \times 9 \times 10^9}{6\pi \times 3 \times 10^8} = E_0^2$$

$$4 \times 10^4 = E_0^2$$

$$E_0 = 200 \text{ N/C}$$

$$\frac{E_0}{B_0} = C$$

$$B_0 = \frac{200}{3 \times 10^8} = \frac{2}{3} \times 10^{-6}$$

### Section-III

(42) Answer : 16

**Hint:**

$$\varepsilon = Bvl$$

**Solution:**

$$\varepsilon = Bvl$$

$$i = \frac{Bvl}{R}$$

$$F = Bil = \frac{B^2 l^2 v}{R}$$

$$- \frac{m dv}{dt} = \frac{B^2 l^2 v}{R}$$

$$\frac{m dv}{dt} \cdot \frac{ds}{dt} = \frac{-B^2 l^2 v}{R}$$

$$S = \frac{Rmv_0}{B^2 l^2} = 8$$

(43) Answer : 6

**Hint:**

$$\varphi_S = MiP$$

**Solution:**

$$\varphi_S = MiP$$

$$\varepsilon_S = \frac{d\varphi_S}{dt} = i_s R$$

$$\int \frac{d\varphi_S}{R} = \int i_s dt$$

$$\frac{\Delta\varphi_S}{R} = Q$$

$$\frac{4 \times 3}{2} = Q$$

$$Q = 6 \text{ C}$$

(44) Answer : 0

**Hint:**

$$\tau \rightarrow \infty$$

**Solution:**

$$X_C = \frac{1}{100 \times 200 \times 10^{-6}} = 50 \Omega$$

$$X_L = 0.5 \times 100 = 50 \Omega$$

$$Z = \infty$$

$$i = 0$$

(45) Answer : 15

**Hint:**

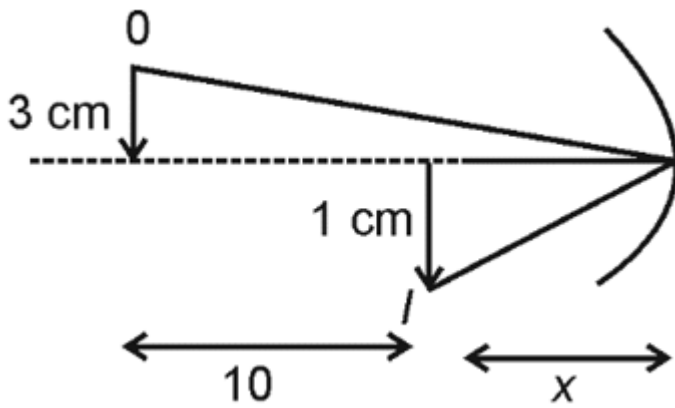
$$\frac{1}{v} + \frac{1}{v} = \frac{1}{f}$$

**Solution:**



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$$\frac{x}{1} = \frac{x+10}{3} \Rightarrow x = 5$$

$$\frac{1}{f} = \frac{1}{-5} + \frac{1}{-15} = \frac{-4}{15}$$

$$f = \frac{15}{4}$$

(46) Answer : 10

Hint:

$$\text{Total energy } E = \frac{1}{2}mv^2 + \frac{1}{2}kx^2 + \frac{q^2}{2C}$$

Solution:

$$\text{Total energy } E = \frac{1}{2}mv^2 + \frac{1}{2}kx^2 + \frac{q^2}{2C}$$

$$BvI = \frac{q}{C}$$

$$\frac{dv}{dt} = - \left( \frac{k}{m + B^2I^2C} \right) x$$

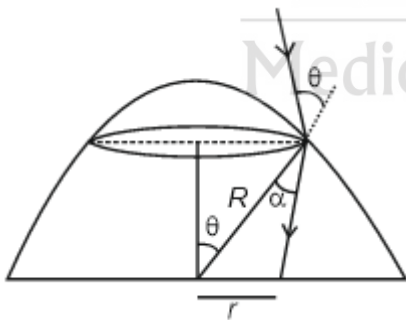
$$\tau = 2\pi \sqrt{\frac{m + B^2I^2C}{k}} = \frac{\pi}{10}$$

(47) Answer : 52

Hint:

$$\mu_1 \sin i = \mu_2 \sin r$$

Solution:



$$\sin \theta = \frac{3}{5} \Rightarrow \theta = 37^\circ$$

$$\sin \theta = \frac{3}{5} \sin \alpha \Rightarrow \sin \alpha = \frac{2}{5}$$

$$\frac{R}{\sin(180 - 53 - \alpha)} = \frac{r}{\sin \alpha}$$

$$r = \frac{2}{5} \frac{R}{\sin(104^\circ)}$$

$$r = \frac{2}{\sin(104^\circ)}$$

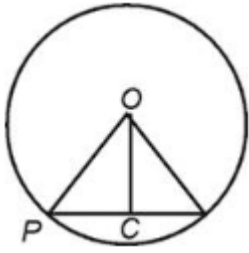
Section-IV

(48) Answer : 00.75

Hint:

$$\varepsilon = \frac{d\phi}{dt}$$

Solution:



Consider triangle  $PCO$ .

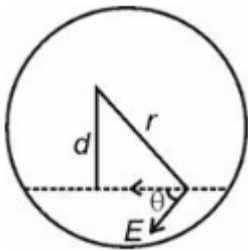
$$\begin{aligned} \epsilon &= \frac{d\phi}{dt} = \frac{1}{2} \cdot OC \cdot PC \cdot \frac{dB}{dt} \\ &= \frac{1}{2} \cdot \frac{\sqrt{3}}{2} R \cdot \frac{R}{2} \cdot 2 \\ &= \frac{\sqrt{3}}{4} R^2 \end{aligned}$$

(49) Answer : 06.00

Hint:

$$\epsilon = \frac{d\phi}{dt}$$

Solution:



$$E = \frac{r}{2} \frac{dB}{dt} = r$$

$$a = \frac{qE \cos \theta}{m}$$

$$a = \frac{q \cdot (r) \left(\frac{d}{r}\right)}{m}$$

$$a = \frac{qd}{m}$$

$$\frac{1}{2} \cdot \frac{qd}{m} t^2 = R$$

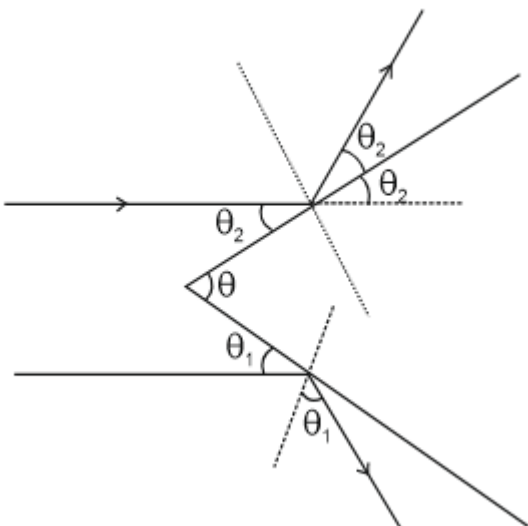
$$t = \sqrt{\frac{2m}{\sqrt{3}q}}$$

(50) Answer : 90.00

Hint:

$$\delta = i + \rho - A$$

Solution:



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$$\delta_1 = \left(\frac{\theta}{2}\right) \times 2$$

$$\text{So } \varphi = 2\delta_1 = 2\theta = 90^\circ$$

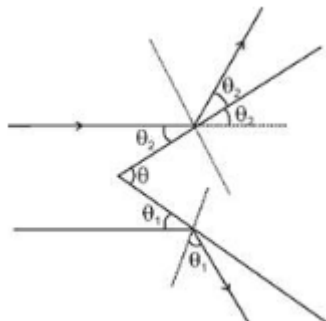
$$\text{And } i = 90 - 22.5 = 67.5^\circ$$

(51) Answer : 67.50

Hint:

$$\delta = i + \rho - A$$

Solution:



$$\delta_1 = (\theta_2) \times 2$$

$$\text{So } \varphi = 2\delta_1 = 2\theta = 90^\circ$$

$$\text{And } i = 90 - 22.5 = 67.5^\circ$$



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