



Aakash

Medical | IIT-JEE | Foundations

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MM : 180

AIATS For Two Year JEE(Advanced)-2027 (XI Studying-P1)_Test-4A_Paper-1_Online

Time : 180 Min.

PHYSICS

Section-I

1. (D)
2. (C)
3. (B)
4. (D)

Section-II

5. (A,C,D)
6. (A,C)
7. (B,C)

Section-III

8. (04.00)
9. (75.00)
10. (02.00)
11. (00.40)
12. (00.20)
13. (31.00)

Section-IV

14. (B)
15. (D)
16. (C)

CHEMISTRY

Section-I

17. (B)
18. (C)
19. (C)
20. (C)

Section-II

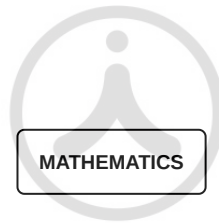
- 21. (A,B)
- 22. (A,B,C)
- 23. (A,D)

Section-III

- 24. (30.60)
- 25. (04.00)
- 26. (08.62)
- 27. (02.00)
- 28. (36.80)
- 29. (05.10)

Section-IV

- 30. (B)
- 31. (A)
- 32. (D)



Section-I

- 33. (A)
- 34. (A)
- 35. (C)
- 36. (D)

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Section-II

- 37. (B,C)
- 38. (A,C)
- 39. (A,C,D)

Section-III

- 40. (05.88)
- 41. (06.00)
- 42. (08.00)
- 43. (03.00)
- 44. (10.00)
- 45. (04.00)

Section-IV

- 46. (D)
- 47. (A)

48. (B)



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Hints and Solutions

PHYSICS

Section-I

(1) Answer : (D)

Hint:

$$v^2 = u^2 + 2ab$$

Solution:

$$a = \frac{2S}{t^2} = 1.5 \text{ m/s}^2 \quad V_{avg} = \frac{3}{2} = 1.5 \text{ m/s}^2$$

$$V_{max} = (1.5)2 = 3 \text{ m/s in } 2 \text{ sec.}$$

So absolute value of acceleration is at most 1.5 m/s^2 i.e. $\frac{3}{20}$ times of gravitational acceleration. so co-efficient of friction

$$\mu \leq \frac{3}{20}$$

(2) Answer : (C)

Hint:

$$\frac{dx}{dt} = v$$

Solution:

$$v = \alpha x + \beta, \quad \beta \leq \frac{\alpha}{2}$$

$$\frac{dx}{dt} = \alpha x + \beta, \quad \int \frac{dx}{\alpha x + \beta} = \int dt$$

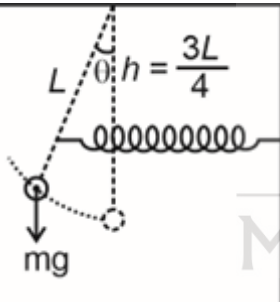
$$x = \frac{\beta}{\alpha} (e^{\alpha t} - 1)$$

(3) Answer : (B)

Hint:

$$\tau = I\alpha$$

Solution:



$$\tau = -[mg(L\sin\theta) + K(h\tan\theta)h]$$

for small angle $\sin\theta \approx \theta$

$$\tau = -(mgL + Kh^2)\theta = (mL^2)\alpha$$

$$\omega^2 = \frac{g}{L} + \frac{9K}{16m}$$

$$\omega = \sqrt{\frac{g}{L} + \frac{9K}{16m}}$$

(4) Answer : (D)

Hint:

$$B = -\frac{\Delta P}{\left(\frac{\Delta V}{V}\right)}$$

Solution:

$$\Delta V = V_0(3\alpha) \Delta T$$

$$\Delta P = B \left(\frac{\Delta V}{V}\right) = 3\alpha B \Delta T$$

$$= 5.28 \times 10^8 \text{ Pa.}$$

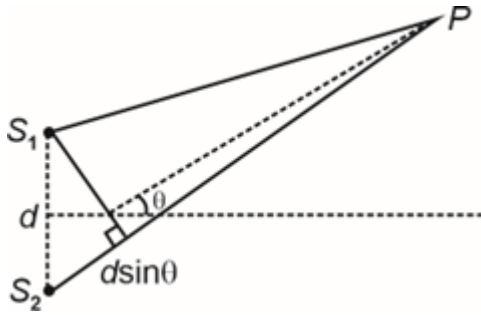
Section-II

(5) Answer : (A,C,D)

Hint:

$$\Delta x = d \sin \theta$$

Solution:



For 1st

$$\Delta x = \lambda = d \sin \theta_1$$

For 2nd

$$\Delta x = 2\lambda = d \sin \theta_2$$

$$\lambda = d(\sin \theta_2 - \sin \theta_1)$$

$$= 2(0.05) = 0.1 \text{ m}$$

$$f = \frac{340}{0.1} = 3400 \text{ m}$$

For smallest angle, destructive interference

$$\Delta x = d \sin \theta = \frac{\lambda}{2}$$

$$\theta = \sin^{-1} \left(\frac{\lambda}{2d} \right)$$

$$\theta = \sin^{-1} \left(\frac{1}{40} \right)$$

(6) Answer : (A,C)

Hint:

$$PV^{\gamma} = \text{const.}$$

$$W = \frac{P_1 V_1 - P_2 V_2}{\gamma - 1}$$

Solution:

$$W_{AB} = \frac{P_1 V_1 - P_2 \left(\frac{V_1}{V_2}\right)^{\gamma} V_2}{\left(\frac{2}{3}\right)}$$

$$W_{BC} = 0$$

$$W_{net} = -\frac{3}{2} P_0 V_0 \left[\left(\frac{V_0}{V}\right)^{\frac{2}{3}} - 1 \right]$$

$$\Delta Q_{AB} = 0$$

$$U_{AB} = -W_{AB} = \frac{3}{2} P_0 V_0 \left[\left(\frac{V_0}{V}\right)^{\frac{2}{3}} - 1 \right]$$

$$\Delta W_{BC} = 0$$

$$\Delta U_{BC} = Q_{BC} = Q$$

$$U = \frac{3}{2} P_0 V_0 \left[\left(\frac{V_0}{V}\right)^{\frac{2}{3}} - 1 \right] + Q$$

$$\Delta U = n C_V \Delta T$$

$$\Delta U = n C_V \Delta T = 2 \left(\frac{R}{\gamma - 1}\right) (T_e - T_A)$$

$$T_e = \frac{Q}{3R} + \frac{P_0 V_0}{2R} \left(\frac{V_0}{V}\right)^{\frac{2}{3}}$$

(7) Answer : (B,C)

Hint:

$$T_{\max} \text{ at } \theta = 45^\circ$$

Solution:

$$\lambda R g \int_0^{\pi/2} \cos \theta \cdot d\theta = \mu \lambda R g \int_0^{\pi/2} \sin \theta \cdot d\theta$$

$$\mu = 1$$

At the position of maximum tension in the rope

$$(\lambda R d\theta) \cos \theta = \mu (\lambda R d\theta \cdot \sin \theta)$$

$$\theta = 45^\circ$$

At any angle θ

$$dT = \lambda R d\theta \cos \theta - (\mu \lambda R \cdot d\theta) g \sin \theta$$



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$$\int_0^{T_{\max}} dT = \lambda Rg \int_0^{\pi/4} (\cos \theta - \sin \theta) d\theta$$

$$T_{\max} = \lambda Rg(\sqrt{2} - 1) = 4.1 \text{ N}$$

Section-III

(8) Answer : 04.00

Hint:

Equivalent thermal conductivity

Solution:

$$H = -K(2\pi rl) \frac{dT}{dr}$$

$$\int_{R_1}^{R_2} \frac{H dr}{2\pi rl} = -K \int_{T_1}^{T_2} dT$$

$$H_1 = H_2$$

$$n = 4$$

(9) Answer : 75.00

Hint:

$$W = \int F dy$$

Solution:

Work done by all forces = 0

$$\int_0^h mg(1 - 0.4y) \cdot dy = 0$$

$$mg \int_0^h (1 - 0.4y) \cdot dy = 0$$

$$mg(h - 0.2h^2) = 0$$

$$h = 5m$$

$$\text{work done by } F \Rightarrow W = \int_0^{\frac{h}{2}} F \cdot dy = \frac{15mg}{4}$$

$$= 75 \text{ J}$$

(10) Answer : 02.00

Hint:

F. B. D.

Solution:

$$N_2 \cos \theta_2 = mg$$

$$N_2 \sin \theta_2 = N_1$$

$$\tan \theta_2 = \frac{N_1}{mg}$$

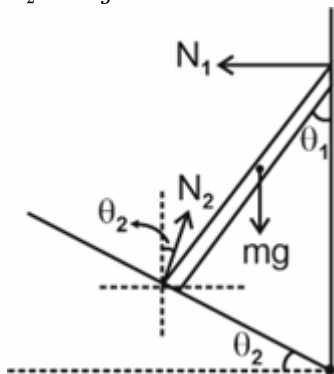
$$l N_1 \cos \theta_1 = \frac{l}{2} mg \sin \theta_1$$

$$\tan \theta_1 = \frac{2N_1}{mg}$$

$$\tan \theta_1 = 2 \tan \theta_2 = 2\sqrt{3}$$

$$N_1 = \sqrt{3}mg$$

$$N_2 = 2mg$$

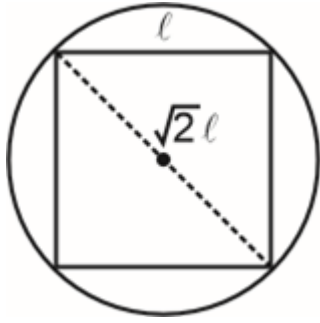


(11) Answer : 00.40

Hint:

$$l\alpha = fR$$

Solution:



M.I of each rod about centre of ring

$$I = \frac{2mr^2}{3}$$

$$I_{net} = \frac{8mr^2}{3}$$

$$\text{Now, } 4ma = 4mg \sin \theta - f \dots (i)$$

$$fR = I\alpha$$

$$f = \frac{Ia}{R^2}, f = \frac{8ma}{3} \dots (ii)$$

From (i) and (ii)

$$a = \frac{12g}{20\sqrt{2}}, f = \frac{8mg}{5\sqrt{2}}$$

$$f \leq \mu N$$

$$\mu \geq \frac{2}{5}$$

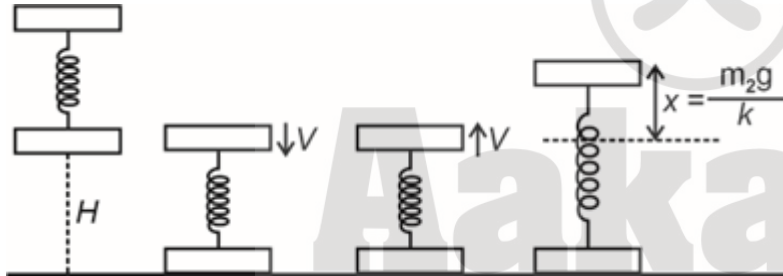
$$\mu_{min} = 0.4$$

(12) Answer : 00.20

Hint:

Conservation of energy

Solution:



$$\frac{1}{2}m_1V^2 = m_1gx + \frac{1}{2}Kx^2, V^2 = 2gH$$

and for the block M_2 to just lift off

$$x = \frac{m_2g}{K}$$

$$m_1gH = m_1g\left(\frac{m_2g}{K}\right) + \frac{1}{2}K\left(\frac{m_2g}{K}\right)^2$$

$$H = \frac{m_2g}{K} \left(\frac{2m_1 + m_2}{2m_1} \right)$$

$$H = 0.20 \text{ m}$$

(13) Answer : 31.00

Hint:

$$W = \int F dx$$

Solution:

$$\pi r^2 l \rho g = \pi r^2 l_{in} \rho_{\omega} g$$

$$l_{in} = \left(\frac{\rho}{\rho_{\omega}} \right) l = \frac{225}{1000} \times 40 = 9 \text{ cm}$$

net displacement = 40 - 9 = 31 cm

$$F_{net} = kx + \pi r^2 \rho g x$$

$$W = \int f_{net} dx = \int_0^{31} (kx + \pi r^2 \rho g x) dx$$

$$W = \left(\frac{\pi+5}{200} \right) (31)^2$$

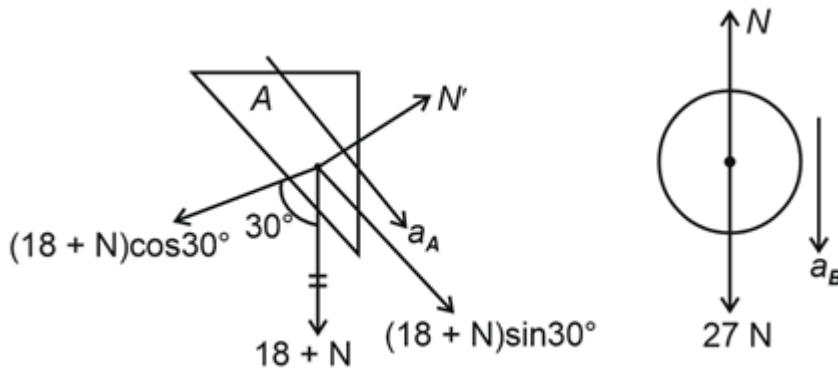
Section-IV

(14) Answer : (B)

Hint:

Draw F. B. D and analysis the motion

Solution:



$$(18 + N) \times \frac{1}{2} = 1.8 a_A \quad \left| \quad 27 - N = 2.7 a_B \quad \dots (ii) \right.$$

$$18 + N = 3.6 a_A \quad \dots (i)$$

From constraint relation $a_A = 2a_B \dots (iii)$

From equation (i), (ii) & (iii)

$$a_B = 4.545 \text{ m/s}^2$$

$$a_A = 9.09 \text{ m/s}^2$$

$$N = 14.72 \text{ N}$$

(15) Answer : (D)

Hint:

Apply conservation of volume and work energy theorem

Solution:

Let cross sectional area of cube = $A = a^2$

then cross sectional area of vessel = $2A = 2a^2$

height of a cube = $a = h$

$$k \cdot \frac{h}{4} = mg, \quad K = 4\rho g A$$

when liquid is filled and spring is relaxed

$$2\rho g x A = \rho g h A, \quad x = \frac{h}{2} \text{ (inside liquid)}$$

As external force pushes the block in the liquid,

liquid also rises from remaining area

Remaining area = $2A - A = A$

$$A_1 x_1 = A_2 x_2, \quad x_1 = x_2$$

$$x_1 + x_2 = \frac{h}{2}, \quad x_1 = x_2 = \frac{h}{4}$$

displacement of block $x_1 = \frac{h}{4}$

$$W_{mg} = \rho g h A \left(\frac{h}{4} \right) = \frac{\rho g h^2 A}{4} = \frac{\rho g a^4}{4}$$

$$W_{spring} = -\frac{1}{2} k x^2 = -\frac{\rho g A h^2}{8} = -\frac{\rho g a^4}{8}$$

When block displaced by x , it gets submerged by $2x$ in liquid

$$W_{upthrust} = -\int_0^{\frac{h}{4}} 2\rho A \left(\frac{h}{2} + 2x \right) g \cdot dx = -\frac{3}{8} \rho g A h^2 = -\frac{3\rho g a^4}{8}$$

$$W_{mg} + W_{spring} + W_{upthrust} \neq W_{ext} = \Delta K = 0$$

$$W_{ext} = \frac{\rho g A^2}{4} = \frac{\rho g a^4}{4}$$

(16) Answer : (C)

Hint:

$$v = \sqrt{\frac{T}{\mu}}$$

Solution:

$$4 \left(\frac{\lambda}{2} \right) = 2$$

$$\lambda = 1 \text{ m}$$

$$v = \sqrt{\frac{T}{\mu}} = \sqrt{\frac{T}{\rho s}}$$

$$\frac{T}{s} = y \left(\frac{\Delta l}{l} \right)$$

$$V = 400 \text{ m/s}$$

$$f = \frac{v}{\lambda} = 400 \text{ Hz}$$

$$y = A \sin(Kx) \cos(\omega t)$$

$$A = 3 \text{ mm}, K = \frac{2\pi}{\lambda} \text{ and } \omega = 2\pi f$$

$$y = (3 \text{ mm}) \sin(2\pi x) \cos(800 \pi t)$$

$$x = \frac{\partial y}{\partial t} = -\omega A \sin(Kx) \sin(\omega t)$$

$$dK = \frac{1}{2} (\mu dx) v^2 = \frac{1}{2} \left(\frac{m}{l} \right) v^2 - dx$$

$$K.E. = K = \frac{1}{2} \left(\frac{m}{l} \right) (\omega A)^2 \int_0^l \sin^2 Kx \cdot dx$$

$$K = \frac{1}{4} m \omega^2 A^2$$

$$= 1.44 \text{ J}$$

$$= 1440 \text{ mJ}$$

CHEMISTRY

Section-I

(17) Answer : (B)

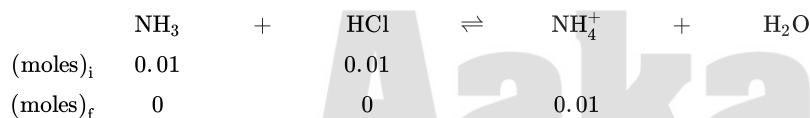
Solution:

Since Beaker X contains temporary hardness, it will get removed on heating & white precipitate of CaCO_3 will be observed

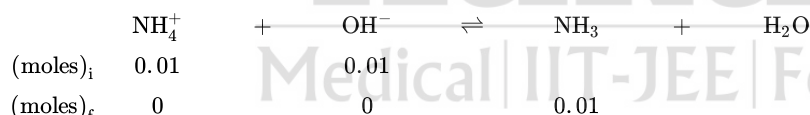


Beaker y has permanent hardness

(18) Answer : (C)

Solution:

After adding NaOH



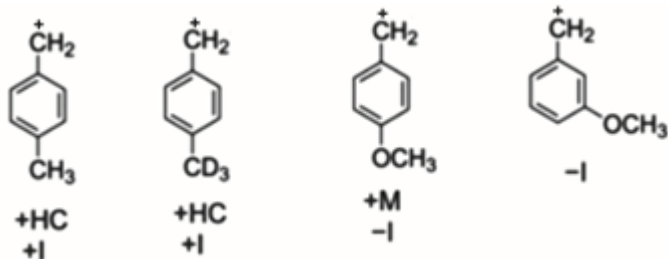
$$[\text{NH}_3]_f = \frac{0.01}{0.2} = 5 \times 10^{-2}$$

$$\text{pOH} = -\log \sqrt{5 \times 10^{-2} \times 1.8 \times 10^{-5}} = -\frac{1}{2} \log 9 \times 10^{-7}$$

$$\text{pOH} \approx 3$$

$$\text{pH} \approx 11$$

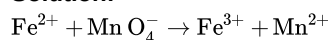
(19) Answer : (C)

Solution:

$$(+\text{HC})_{\text{H}} > (+\text{HC})_{\text{D}}$$

Stability order III > I > II > IV

(20) Answer : (C)

Solution:

$$\text{Meq of Fe}^{2+} = \text{meq KMnO}_4$$

$$\frac{0.25}{152+18x} \times 1000 \times 1 = 0.02 \times 9 \times 5$$

$$x \approx 7$$

Section-II

(21) Answer : (A,B)

Solution:

Chemical smog is a mixture of smog, fog and sulphur dioxide
Ozone, nitric oxide and acrolein are components of photochemical smog

(22) Answer : (A,B,C)

Solution:

For D_2O melting point, Boiling point & magnitude of ΔH_f is higher compared to H_2O

(23) Answer : (A,D)

Solution:

$$\Delta H_{T_2} = (\Delta C_P)_r (T_2 - T_1) + \Delta H_{T_1}$$

$$\Delta H_{500} = \frac{10(500-300)}{1000} - 40$$

$$= -38 \text{ kJ/mole}$$

$$\Delta H_{400} = \frac{10(400-300)}{1000} - 40$$

$$= -39 \text{ kJ/mole}$$

Section-III

(24) Answer : 30.60

Solution:

$$v_n = 2.2 \times 10^6 \times \frac{Z}{n}$$

$$1.65 \times 10^6 = 2.2 \times 10^6 \times \frac{Z}{4}$$

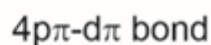
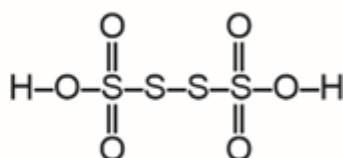
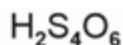
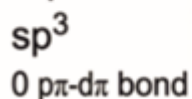
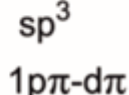
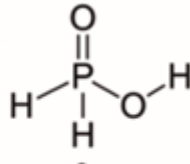
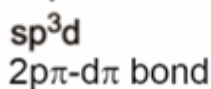
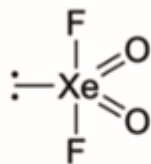
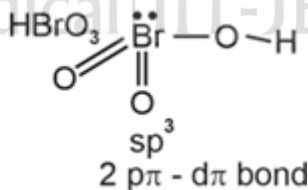
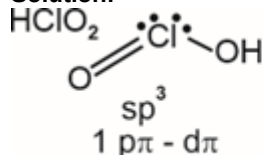
$$3 = Z$$

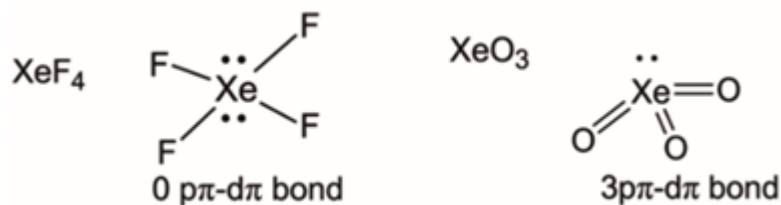
$$E_n = 13.6 \frac{Z^2}{n^2} = 13.6 \times \frac{3^2}{2^2}$$

$$= 30.6 \text{ eV}$$

(25) Answer : 04.00

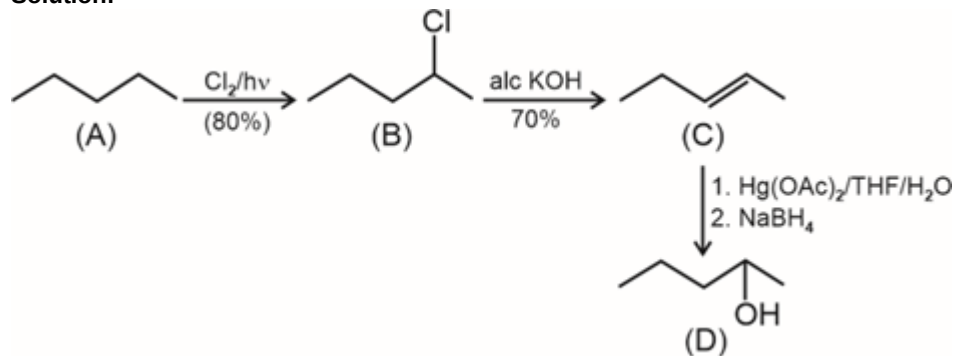
Solution:





(26) Answer : 08.62

Solution:



$$\text{moles of pentane} = \frac{25.2}{72} = 0.35$$

$$\begin{aligned} \text{mass of 3-pentanol formed} &= 0.35 \times 0.8 \times 0.7 \times 0.5 \times 88 \\ &= 8.624 \text{ g} \end{aligned}$$

(27) Answer : 02.00

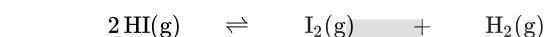
Solution:

$$\Delta G^\circ = -RT \ln K_{eq}$$

$$-3.5 \times 10^3 = 8.3 \times 300 \ln K_{eq}$$

$$1.4 = \ln K_{eq}$$

$$4 = K_{eq}$$



$$t = 0 \quad 5$$

$$t = t_{eq} \quad 5 - 2x$$

$$K_P = \frac{P_{\text{H}_2} P_{\text{I}_2}}{(P_{\text{HI}})^2}$$

$$4 = \frac{x^2}{(5-2x)^2}$$

$$2 = \frac{x}{5-2x}$$

$$10 - 4x = x$$

$$2 = x$$

(28) Answer : 36.80

Solution:

Each molecule of orthoboric acid will require

2 molecule of glycerol.

mass of glycerol required for 12.36 g H_3BO_3

$$= 2 \times \frac{12.36}{61.8} \times 92$$

$$= 36.8 \text{ g}$$

(29) Answer : 05.10

Solution:

$$\text{Al}_2\text{O}_3 \text{ in original sample} = \frac{6.12}{102} \times \frac{100}{75} \times \frac{100}{80} \times \frac{2}{2} \times 102$$

$$= 10.2 \text{ g}$$

$$\% \text{ purity} = \frac{10.2 \times 100}{200}$$

$$= 5.1\%$$

Section-IV

(30) Answer : (B)

Solution:(P) Electron density on Benzene ring $\propto +HC > +I$

(Q) Stability of enol decreases as extent of cross conjugation increases

(R) Stability of carbocation $\propto +HC > +Z$ (S) Stability of carbanion increases due to back bonding followed by extent of $-I$ **(31) Answer : (A)****Solution:**

	%	Moles	Moles ratio
C	73	6.08	6
(P) H	11.5	11.5	12
O	15.5	0.96	1

	%	Moles	Moles ratio
C	39%	3.25	3
(Q) H	8.6%	8.6	8
O	52.4%	3.27	3

	%	Moles	Moles ratio
C	54.5%	4.54	4
(R) H	9%	9	8
O	36.5	2.28	2

	%	Moles	Moles ratio
C	58.8	4.9	5
(S) H	9.8	9.8	10
O	31.4	1.96	2

(32) Answer : (D)**Solution:**Charles law, $\frac{V}{T} = \text{constant}$ Boyle's Law, $PV = \text{constant}$ Gay-Lussac's Law, $\frac{P}{T} = \frac{nR}{V}$

$$PT = \frac{nRT^2}{V}$$

$$y = x^2$$

Avogadro's Law, $\frac{V}{n} = \text{constant}$


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MATHEMATICS

Section-I**(33) Answer : (A)****Solution:**

$$y^2 = 12x + 2y + 23$$

$$y^2 - 2y + 1 = 12(x + 2)$$

$$(y - 1)^2 = 12(x + 2)$$

Vertex: $(-2, 1)$

$$a = 3$$

Focus: $(1, 1)$ Let equation of focal chord of the Parabola is $\frac{x}{p} + \frac{y}{q} = 1$

$$\Rightarrow \frac{x}{p} + \frac{y}{2} = 1$$

It passes through focus.

$$\frac{1}{p} + \frac{1}{2} = 1$$

$$\Rightarrow p = 2$$

Equation of focal chord is:

$$x + y = 2, m = -1 \Rightarrow \theta = \frac{3\pi}{4}$$

Length of focal chord : $4ac\sec^2\theta$

$$= 4 \times 3 \times \cos e c^2 \left(\frac{3\pi}{4} \right)$$

$$= 12 \times 2$$

$$= 24$$

(34) Answer : (A)

Solution:

$$3x - 2y = 6\alpha$$

$$3\alpha x + 2\alpha y = 6$$

$$3x + 2y = \frac{6}{\alpha}$$

$$9x^2 - 4y^2 = 36$$

$$\frac{x^2}{4} - \frac{y^2}{9} = 1$$

Tangent to S,

$$y = mx \pm \sqrt{4m^2 - 9}$$

$$m = \frac{5}{2}$$

$$\Rightarrow y = \frac{5x}{2} \pm \sqrt{16} = \frac{5x}{2} + 4$$

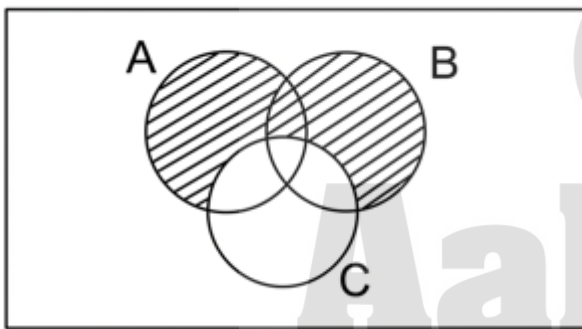
(35) Answer : (C)

Solution:

Let $n(A)$ = number of 3-digit numbers that are divisible by 3.

$n(B)$ = number of 3-digit numbers that are divisible by 5.

$n(C)$ = number of 3-digit numbers that are divisible by 11.



$$n(A) = 300, n(B) = 180, n(C) = 81,$$

$$n(A \cap B) = 60, n(B \cap C) = 17, n(A \cap C) = 27,$$

$$n(A \cap B \cap C) = 6.$$

$$\text{Required number} = 300 + 180 - 60 - 17 - 27 + 6 = 382$$

(36) Answer : (D)

Solution:

$$(2x + 1)^2 + (3y + 3)^2 = P + 10$$

$$\frac{\left(x + \frac{1}{2}\right)^2}{\frac{P+10}{4}} + \frac{(y+1)^2}{\frac{P+10}{9}} = 1$$

$$\frac{2B^2}{A^2} = 4$$

$$\Rightarrow 2 \left(\frac{P+10}{9} \right) = \frac{4}{2} \sqrt{P+10}$$

$$\Rightarrow P = 71$$

$$\Rightarrow a = 2 \cdot \frac{9}{2} = 9$$

$$b = 6$$

$$\Rightarrow a + b = 15$$

Section-II

(37) Answer : (B,C)

Hint:

$$C.V. = \frac{\sigma}{\mu} \times 100$$

Solution:

$$\sum_{i=1}^6 x_i = 36 \Rightarrow \text{Mean} = 6 = \mu_A$$

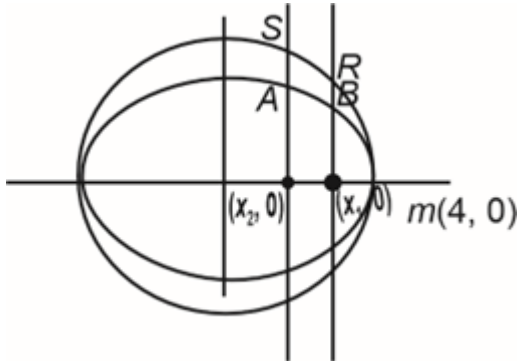
$$\sigma_A = \sqrt{\frac{244}{6} - (6)^2} = 2.16$$

$$\sum_{j=1}^5 x_j = 25 \Rightarrow \text{Mean} = 5 = \bar{x}_B$$

$$\sigma_B = \sqrt{\frac{175}{5} - 25} = \sqrt{10}$$

(38) Answer : (A,C)

Solution:



$$R : \left(4 \cos \frac{\pi}{6}, 4 \sin \frac{\pi}{6}\right) : \left(\frac{4\sqrt{3}}{2}, 2\right)$$

$$S : \left(4 \cos \frac{\pi}{4}, 4 \sin \frac{\pi}{4}\right) : \left(\frac{4}{\sqrt{2}}, \frac{4}{\sqrt{2}}\right)$$

$$B : \left(\frac{4\sqrt{3}}{2}, \frac{3}{2}\right), A : \left(\frac{4}{\sqrt{2}}, \frac{3}{\sqrt{2}}\right)$$

$$\text{Line joining A \& B : } y - \frac{3}{2} = \frac{\frac{3}{\sqrt{2}} - \frac{3}{2}}{\frac{4}{\sqrt{2}} - \frac{4\sqrt{3}}{2}} \left(x - \frac{4\sqrt{3}}{2}\right)$$

$$\frac{|N_2 B|}{|N_2 S|} = \frac{\frac{3}{\sqrt{2}}}{\frac{4}{\sqrt{2}}} = \frac{3}{4}$$

$$\Rightarrow 4|N_2 B| = 3|N_2 S|$$

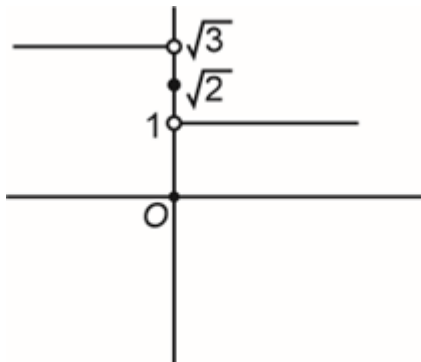
$$\frac{|N_1 P|}{|N_1 R|} = \frac{3}{2} = \frac{3}{4}$$

$$\Rightarrow 4|N_1 P| = 3|N_1 R|$$

(39) Answer : (A,C,D)

Solution:

$$\text{sgn}(x) = \begin{cases} 1, & x > 0 \\ 0, & x = 0 \\ -1, & x < 0 \end{cases}$$



$$x > 0 \Rightarrow f(x) = \sqrt{2-1} = 1$$

$$x = 0 \Rightarrow f(x) = \sqrt{2-0} = \sqrt{2}$$

$$x < 0 \Rightarrow f(x) = \sqrt{2-(-1)} = \sqrt{3}$$

Section-III

(40) Answer : 05.88

Solution:

Multiply & divide by 7^x

$$\lim_{x \rightarrow 2} \frac{7^{2x} - 56 \cdot 7^x + 343}{7^{x/2} - 7}$$

$$\lim_{x \rightarrow 2} \frac{(7^x - 49)(7^x - 7)}{(7^{x/2} - 7)}$$

$$\lim_{x \rightarrow 2} \frac{(7^{x/2} - 7)(7^{x/2} + 7)(7^x - 7)}{(7^{x/2} - 7)}$$

$$= (7 + 7)(7^2 - 7)$$

$$= 14 \cdot 42$$

$$= 588$$

(41) Answer : 06.00

Solution:

$$n(X) = 78$$

$$n(Y) = 59$$

$$(AP)_x \rightarrow 3, 6, 9, 12, \dots$$

$$\text{Last term} = 234$$

$$(AP)_y \rightarrow 5, 9, 13, 17, \dots$$

$$\text{Last term} = 237$$

$$d = \gcd(d_x, d_y) = 12$$

$$\text{Last term} \Rightarrow n < \frac{225}{12} + 1$$

$$n = 19$$

$$\text{So number of terms in } X \cup Y = 78 + 59 - 19$$

$$= 118$$

$$\Rightarrow \frac{K+2}{20} = 6$$

(42) Answer : 08.00

Solution:

$$(1 + x^3)^3 = 1 + 3x^3 + 3x^6 + x^9$$

$$(1 + x^3)^3 (1 + x)^n = (1 + 3x^3 + 3x^6 + x^9) ({}^n C_0 + {}^n C_1 x + {}^n C_2 x^2 + \dots)$$

$$a_0 = 1$$

$$a_1 = n$$

$$a_2 = {}^n C_2$$

$$a_3 = {}^n C_3 + 3 \cdot {}^n C_0$$

$$2 + ({}^n C_3 + 3 \cdot {}^n C_0) = n + {}^n C_2$$

$$\Rightarrow n = 3, 5$$

(43) Answer : 03.00

Solution:

$$\frac{-6}{\sqrt{21}\sqrt{54}} + \frac{4a}{\sqrt{21}\sqrt{54}} + \left(\frac{-6}{\sqrt{21}\sqrt{54}} \right) = 0 \Rightarrow 4a = 12 \Rightarrow a = 3$$

(44) Answer : 10.00

Solution:

We have numbers as 7, 6, 4, 11, 7

We write it in increasing order 4, 6, 7, 7, 11

Clearly, Mean = Median = Mode = 7

After adding $a, b, c, d,$

New mean, mode, median will be 9.

We have old mode 7 which repeats itself for 2 times.

If 9 is the new mode then it has to repeat at least for 3 times. Median is also 9.

So we have 4, 6, 7, 7, 9, 9, 11, d

Now mean is also 9, so

$$\frac{4+6+7+7+9+9+9+11+d}{9} = 9$$

$$\Rightarrow 62 + d = 81$$

$$\Rightarrow d = 19$$

$$a = b = c = 9, d = 19$$

$$d - c = 19 - 9 = 10$$

(45) Answer : 04.00

Solution:

As we know, $z\bar{z} = |z|^2$

Equation can be written as:

$$12z\bar{z} = 2(z+2)(\bar{z}+2) + (z^2+1)(\bar{z}^2+1) + 31$$

$$\begin{aligned} &\Rightarrow -12z\bar{z} + 2z\bar{z} + 4(z + \bar{z}) + 8 + z^2\bar{z}^2 + (z^2 + \bar{z}^2) + 32 = 0 \\ &\Rightarrow (z^2 + 2z\bar{z} + \bar{z}^2) + 4(z + \bar{z}) + 4 + (z^2\bar{z}^2 - 12z\bar{z} + 36) = 0 \\ &\Rightarrow (z + \bar{z} + 2)^2 + (z\bar{z} - 6)^2 = 0 \Rightarrow z + \bar{z} + 2 = 0 \Rightarrow z + \bar{z} = -2 \\ &\& z\bar{z} - 6 = 0 \\ &-2(z + \bar{z}) = 4 \end{aligned}$$

Section-IV

(46) Answer : (D)

Solution:

$$\sin x - \cos x = 1$$

$$\cos\left(\frac{\pi}{4} + x\right) = -\frac{1}{\sqrt{2}}$$

$$\Rightarrow x = -\frac{3\pi}{2}, -\pi, \frac{\pi}{2}, \pi$$

$$\text{II } \tan 3x = \sqrt{3}$$

$$3x = n\pi + \frac{\pi}{3}$$

$$x = \frac{-8\pi}{9}, \frac{-5\pi}{9}, \frac{-2\pi}{9}, \frac{\pi}{9}, \frac{4\pi}{9}, \frac{7\pi}{9}$$

$$\text{III } \sin x + \cos x = 1$$

$$\cos\left(x - \frac{\pi}{4}\right) = \frac{1}{\sqrt{2}}$$

$$x - \frac{\pi}{4} = 2n\pi \pm \frac{\pi}{4}$$

$$x = 0, \frac{\pi}{2}, 2\pi$$

$$\text{IV } \cos 2x = \frac{1}{2}$$

$$2x = 2n\pi \pm \frac{\pi}{3}$$

$$x = \frac{\pi}{6}, \frac{5\pi}{6}$$

(47) Answer : (A)

Solution:

$$2g_1g_2 + 2f_1f_2 = 2g_2g_3 + 2f_2f_3 = 2g_3g_1 + 2f_3f_1 = 0$$

 (centroid (h, k))

$$h = -\frac{(g_1/2 + g_2/2 + g_3/2)}{3}$$

$$K = -\frac{(f_1/2 + f_2/2 + f_3/2)}{3}$$

$$(6h)^2 + (6k)^2 = m + n$$

$$(1) m + n = 1 \Rightarrow r = 1/6$$

$$(2) m + n = 4 \Rightarrow r = 1/3$$

$$(3) m + n = 9 \Rightarrow r = 1/2$$

$$(4) m + n = 36 \Rightarrow r = 1$$

(48) Answer : (B)

Solution:

 Number of diagonals of a polygon of n sides

$$= \frac{n(n-3)}{2} = \frac{11(11-3)}{2} = 44$$

 Number of triangle by n points out of which only m are collinear = ${}^nC_3 - {}^mC_3$

$${}^{15}C_3 - {}^7C_3 = 420$$

 Maximum number of points of intersection of n circles : $2 \cdot {}^nC_2 = 30$

 Number of lines by n points in which no three points are collinear is

$${}^nC_2 = {}^7C_2 = 21$$