



Aakash

Medical | IIT-JEE | Foundations

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MM : 180

AIATS For One Year JEE(Advanced)-2026 (XII Studying & XII Passed)_Test-5A_Paper-1_Online

Time : 180 Min.

CHEMISTRY

Section-I

1. (D)
2. (D)
3. (D)
4. (C)

Section-II

5. (B,C,D)
6. (A,C)
7. (A,B,C)

Section-III

8. (78.30,78.90)
9. (01.00)
10. (55.21)
11. (06.00)
12. (00.34)
13. (12.00)

Section-IV

14. (A)
15. (B)
16. (D)

MATHEMATICS

Section-I

17. (A)
18. (D)
19. (C)
20. (B)

Section-II

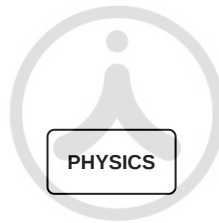
- 21. (B,C)
- 22. (A,B,D)
- 23. (A,B,C,D)

Section-III

- 24. (07.00)
- 25. (25.00)
- 26. (33.00)
- 27. (01.00)
- 28. (24.00)
- 29. (02.00)

Section-IV

- 30. (D)
- 31. (C)
- 32. (B)



Section-I

- 33. (B)
- 34. (D)
- 35. (D)
- 36. (D)



Section-II

- 37. (B,D)
- 38. (B,C)
- 39. (A,B)

Section-III

- 40. (00.00)
- 41. (02.00)
- 42. (12.00)
- 43. (12.00)
- 44. (04.00)
- 45. (05.00)

Section-IV

- 46. (D)
- 47. (C)

48. (A)



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Hints and Solutions

CHEMISTRY

Section-I

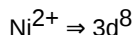
(1) Answer : (D)

Hint:

Since Ni^{2+} is present at octahedral voids hence octahedral splitting will take place. NiO is antiferromagnetic substance having zero magnetic moment.

Solution:

P is NiO



n = 2

$$\mu = \sqrt{2(2+2)} = \sqrt{8} = 2.83 \text{ BM}$$

Since Ni^{2+} is present at octahedral voids hence octahedral splitting will take place. NiO is antiferromagnetic substance having zero magnetic moment.

(2) Answer : (D)

Hint:

Fluorides of alkaline earth metals are sparingly soluble in water.

Solution:

• The crystal structures of MgO, CaO and SrO are rock salt type, in which O^{2-} form ccp and metal ions are at all octahedral void.

• Order of density : Ca < Mg < Be < Sr < Ba

• Fluorides of alkaline earth metals are sparingly soluble in water.

(3) Answer : (D)

Hint:

For adiabatic process, q = 0

Solution:

$$\Delta U = q + W$$

For adiabatic process

$$q = 0$$

$$\Delta U = W$$

For real gases

$$\Delta U = -n^2 a \left[\frac{1}{V_2} - \frac{1}{V_1} \right]$$

$$W = n^2 a \left[\frac{1}{V_2} - \frac{1}{V_1} \right]$$

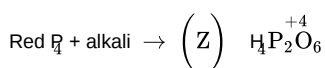
For ideal gas

$$W = -PdV$$

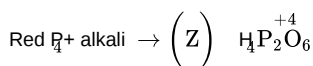
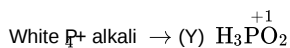
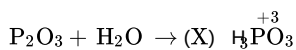
Due to interparticle forces in real gas the internal energy decreases more during expansion compared to an ideal gas.

(4) Answer : (C)

Hint:



Solution:



Section-II

(5) Answer : (B,C,D)

Hint:

KMnO_4 is an oxidising agent oxidises $\text{Fe}^{2+} \rightarrow \text{Fe}^{3+}$

Solution:

KMnO_4 is an oxidising agent oxidises $\text{Fe}^{2+} \rightarrow \text{Fe}^{3+}$

Meq of $\text{Fe}^{2+} = \text{Meq of KMnO}_4$

m.moles \times nf = N \times V

m.moles \times 1 = 0.1×50

Millimoles of $\text{Fe}^{2+} = 0.1 \times 50 = 5 \text{ mmol}$

Mass of ion in ore = $5 \times 10^{-3} \times 56 = 0.28 \text{ g}$

% of Fe in ore = $\frac{0.28}{0.56} \times 100 = 50\%$

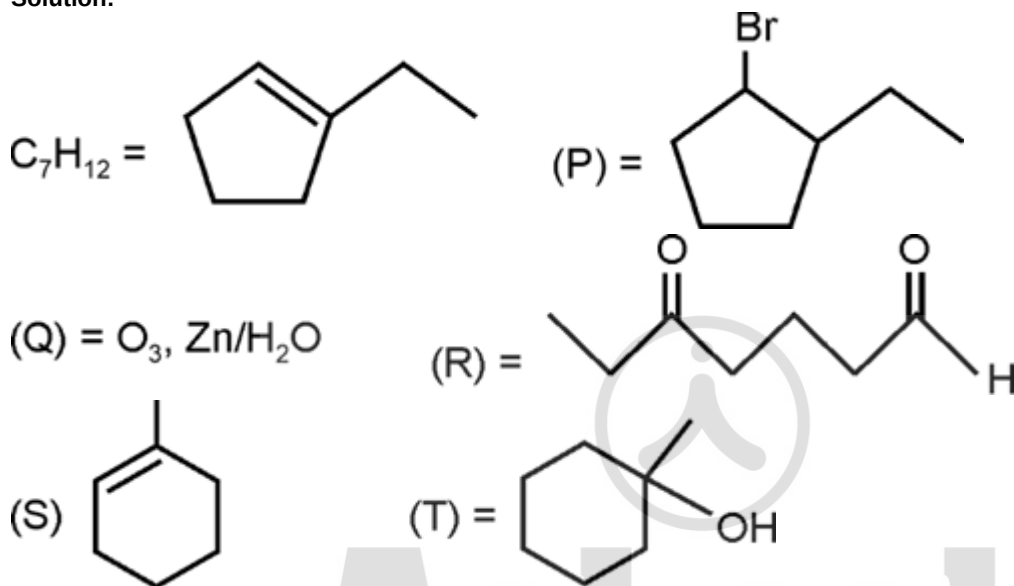
Molarity of KMnO_4 used = $\frac{N}{n_f} = \frac{0.1}{5} = 0.02 \text{ M}$

(6) Answer : (A,C)

Hint:

HBr in presence of R_2O_2 follow Anti-Markovnikov rule.

Solution:

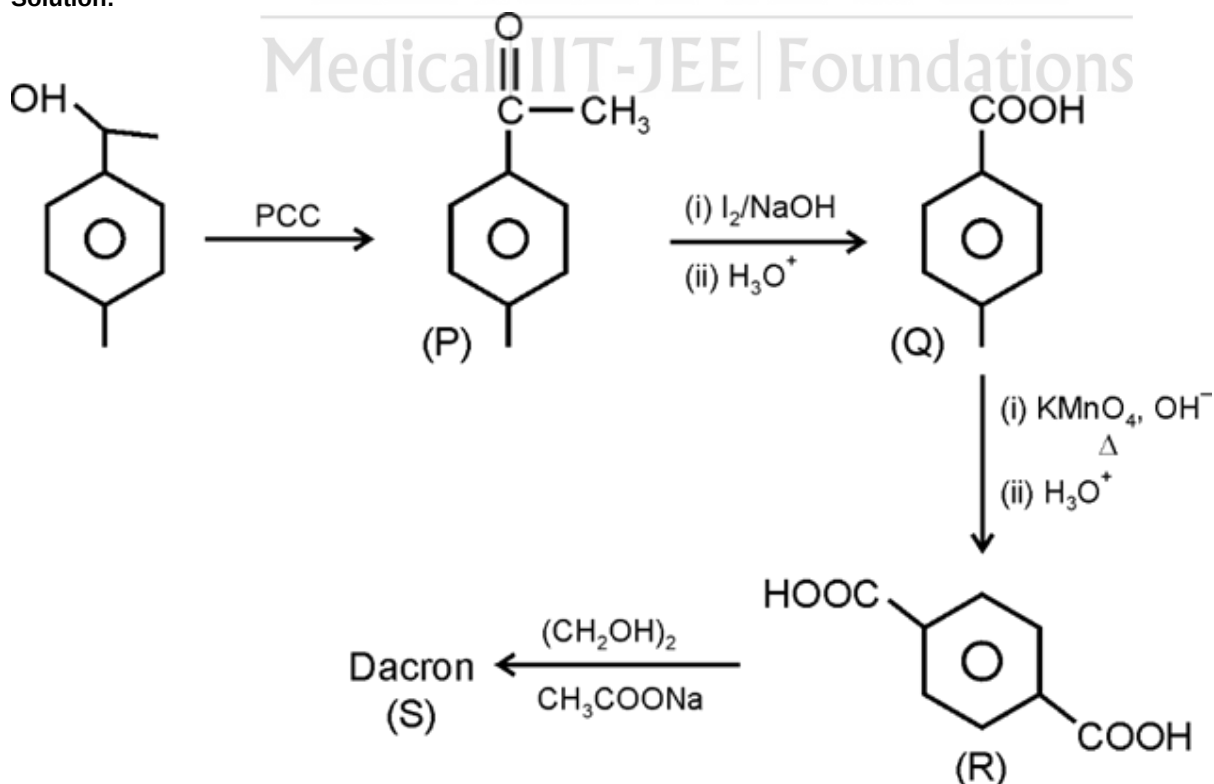


(7) Answer : (A,B,C)

Hint:

Dacron is a polymer of ethylene glycol and terephthalic acid.

Solution:



Section-III

(8) Answer : 78.30,78.90

Hint:

$$K_b = \frac{M_{\text{solvent}} \times RT_b^2}{1000 \times \Delta H_{\text{vap}}}$$

Solution:

$$K_b = \frac{M_{\text{solvent}} \times RT_b^2}{1000 \times \Delta H_{\text{vap}}}$$

$$K_b = \frac{78 \times 8.3 \times 353 \times 353}{1000 \times 30800} \text{ K kg mol}^{-1}$$

$$K_b = 2.62 \text{ K kg mol}^{-1}$$

$$\Delta T_b = 1 \text{ K}$$

$$\Delta T_b = K_b \times m$$

$$1 = 2.62 \times \frac{3}{M \times 100} \times 1000$$

$$M = 2.62 \times 3 \times 10$$

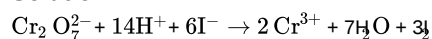
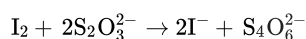
$$M = 78.6 \text{ g/mol}$$

(9) Answer : 01.00

Hint:

The brown solution M is due to I_2

Solution:

The brown solution M is due to I_2 

$$\text{Meq of } Cr_2O_7^{2-}$$

$$= \text{Meq of } S_2O_3^{2-}$$

$$(n \times n_f)_{Cr_2O_7^{2-}} = (n \times n_f)_{S_2O_3^{2-}}$$

$$n \times 6 = 6 \times 1$$

$$n = 1$$

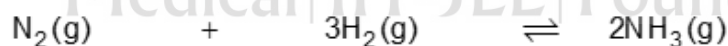
$$\text{Millimoles of } Cr_2O_7^{2-} = 1$$

(10) Answer : 55.21

Hint:

$$\Delta G = -RT \ln K_{eq}$$

Solution:



$$t = 0 \quad 3 \times 10^{-2} \text{ mol} \quad 5 \times 10^{-2} \text{ mol} \quad -$$

$$t = eq \quad (3-1) \times 10^{-2} \text{ mol} \quad (5-3) \times 10^{-2} \text{ mol} \quad 1 \times 10^{-2} \times 2 = 2 \times 10^{-2} \text{ mol}$$

$$K_{eq} = \frac{\left(\frac{2}{2} \times 10^{-2}\right)^2}{\left(\frac{2}{2} \times 10^{-2}\right)^3 \left(\frac{2}{2} \times 10^{-2}\right)}$$

$$K_{eq} = \frac{10^{-4}}{10^{-6} \times 10^{-2}} = 10^4$$

$$\Delta G^\circ = -RT \ln K_{eq}$$

$$\Delta G^\circ = -8.3 \times 723 \times \ln 10^4$$

$$\Delta G^\circ = -4 \times 8.3 \times 723 \ln 10$$

$$\Delta G^\circ = -4 \times 8.3 \times 723 \times 2.3 \text{ J/mol}$$

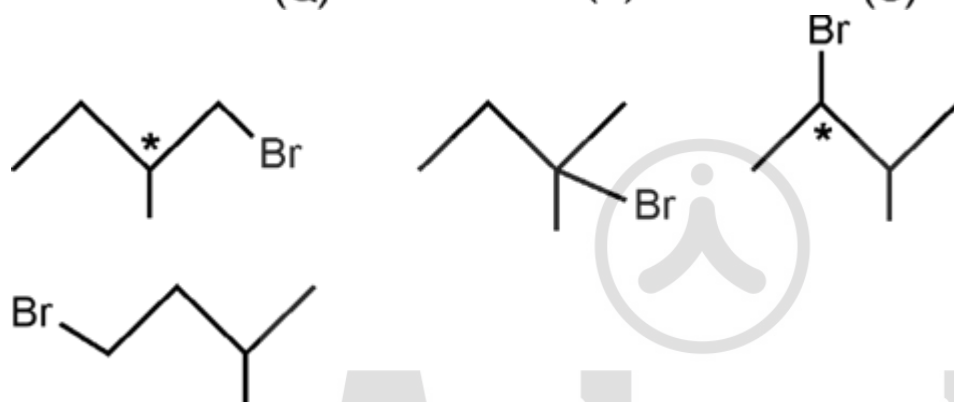
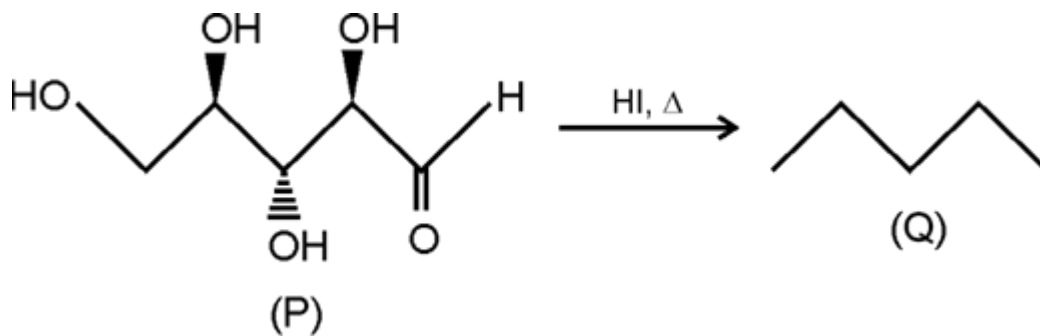
$$\Delta G^\circ = -55.21 \text{ kJ/mol}$$

(11) Answer : 06.00

Hint:

A is n-pentane, B is 2-methyl butane and C is 2,2-dimethyl propane.

Solution:



(12) Answer : 00.34

Hint:

Kjeldahl's method is not applicable to compounds containing nitrogen in nitro and azo group as nitrogen of these compounds does not change to ammonium sulphate under the condition.

Solution:

Kjeldahl's method is not applicable to compounds containing nitrogen in nitro and azo group as nitrogen of these compounds does not change to ammonium sulphate under the condition.

$$\text{Mole of X} = \frac{3.02}{302} = 10^{-2} \text{ mol}$$

$$\text{Mole of ammonia produced} = 2 \times 10^{-2} \text{ mol}$$

$$\text{Mass of ammonia} = 0.02 \times 17 = 0.34 \text{ g}$$

(13) Answer : 12.00

Hint:

$$X = {}_{11}\text{Na}$$

$$Y = {}_{12}\text{Mg}$$

$$Z = {}_{13}\text{Al}$$

Solution:

$$X = {}_{11}\text{Na}$$

$$Y = {}_{12}\text{Mg}$$

$$Z = {}_{13}\text{Al}$$

$$r_{\text{met}} = \text{Na} > \text{Mg} > \text{Al}$$

$$\Delta_f H_1 = \text{Mg} > \text{Al} > \text{Na}$$

$$A_e = \text{Na} > \text{Al} > \text{Mg}$$

Section-IV

(14) Answer : (A)

Hint:

$(\text{NH}_4)_2\text{CO}_3$ in the presence of NH_4OH group-V reagent $\Rightarrow \text{Ca}^{2+}$ precipitates

Solution:

Adding dil HCl group-I reagent \Rightarrow Pb^{2+} precipitates

NH_4OH in presence of NH_4Cl group-III reagent \Rightarrow Fe^{3+} precipitates

Passing H_2S in the presence of NH_4OH group-IV reagent \Rightarrow Ni^{2+} precipitates

$(NH_4)_2CO_3$ in the presence of NH_4OH group-V reagent \Rightarrow Ca^{2+} precipitates

(15) Answer : (B)

Hint:

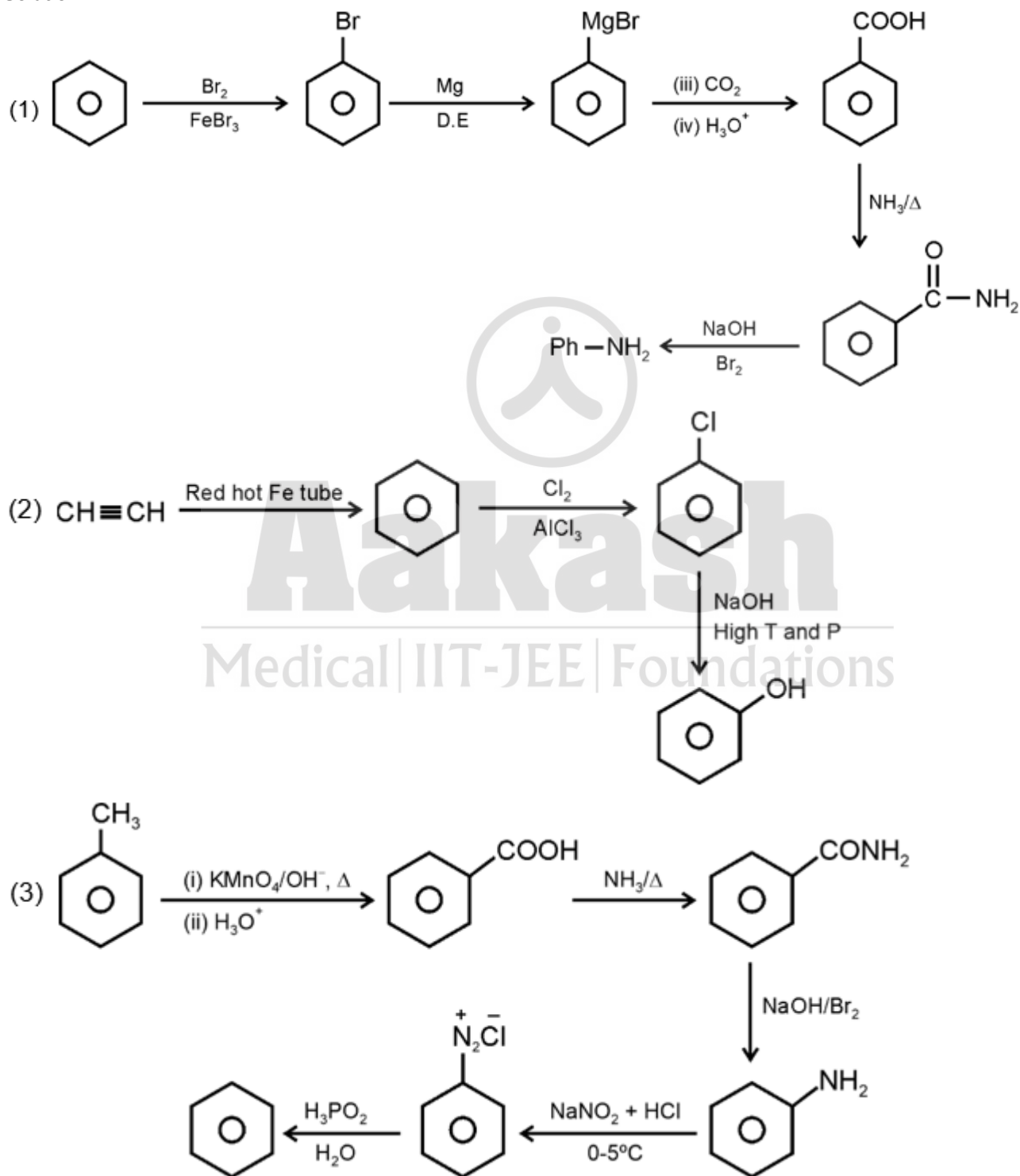
Reactant of P is phenol

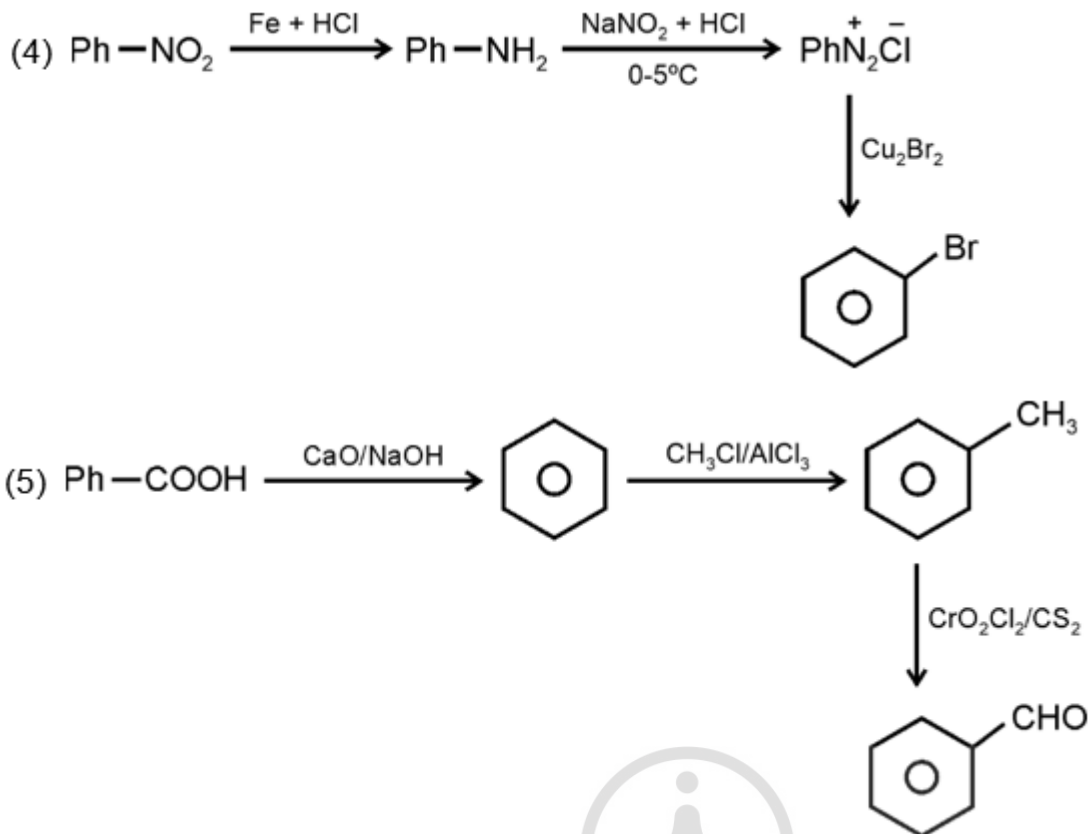
Reactant of Q is aryl halide

Reactant of R is benzene

Reactant of S is aniline

Solution:





(16) Answer : (D)

Hint:

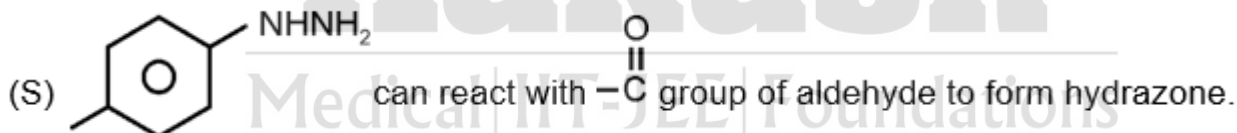
α -amino acid can give ninhydrin test, but absence of phenolic $-\text{OH}$ group so, can't give violet colour with FeCl_3

Solution:

(P) α -amino acid can give ninhydrin test, but absence of phenolic $-\text{OH}$ group can't give violet colour with FeCl_3

(Q) After hydrolysis 2-amino acid is formed, which can give ninhydrin test, due to presence of phenolic $-\text{OH}$ group can give phthalein test.

(R) Aniline can form yellow dye with diazonium salt



MATHEMATICS

Section-I

(17) Answer : (A)

Hint:

$(a, a) \in T \Rightarrow$ reflexive

Solution:

$\because (1, 2) \in S$ but $(2, 1) \notin S$

$\Rightarrow S$ is not equivalence

$T : \{(x, y) : x - y \text{ is an integer}\}$

$\because (a, a) \in T \Rightarrow$ reflexive

$(a, b) \Rightarrow (b, a) \Rightarrow$ symmetric

$(a, b) \in I \Rightarrow a - b \in I$

$(b, c) \Rightarrow b - c \in I$

$\Rightarrow a - c \in 2I \in I' \Rightarrow$ transitive

$\Rightarrow T$ is an equivalence relation.

(18) Answer : (D)

Hint:

$$x_1 + x_2 + x_3 = 75$$

$$\Rightarrow x_1 + x_2 + x_3 = 72$$

Solution:

$$\text{As AM} = 25 \Rightarrow \text{Sum} = 75$$

$$\therefore x_1 + x_2 + x_3 = 75 \quad x_1 \geq 1, x_2 \geq 1, x_3 \geq 1$$

$$\Rightarrow x_1 + x_2 + x_3 = 72$$

$$\text{Number of non-negative integral solution} = {}^{72+3-1}C_{3-1} = {}^{74}C_2 = {}^{74}C_{72}$$

$$\text{Total outcome} = (100)^3$$

$$\Rightarrow P(E) = \frac{{}^{74}C_{72}}{100^3}$$

(19) Answer : (C)

Hint:

$$x \rightarrow \frac{\pi}{2}^+ [\cot x] = -1$$

Solution:

$$x \rightarrow \frac{\pi}{2}^+ [\cot x] = -1$$

$$\therefore \lim_{x \rightarrow \frac{\pi}{2}^+} f(x) = e^{-1} = \frac{1}{e}$$

$$\text{at } x \rightarrow \frac{\pi}{2}^- [\cot x] = 0$$

$$\Rightarrow \lim_{x \rightarrow \frac{\pi}{2}^-} f(x) = e^0 = 1$$

(20) Answer : (B)

Hint:

$$M'AM \text{ is } 1 \times 1$$

Solution:

$$M \text{ is } n \times 1$$

$$M' \text{ is } 1 \times n$$

$$A \text{ is } n \times n$$

$$\therefore M'AM \text{ is } 1 \times 1$$

$$\text{Let } M'AM = k$$

$$(M'AM)' = k$$

$$M'A'M = k$$

$$\therefore A' = -A$$

$$\Rightarrow M'AM = k$$

$$\therefore k = -k \Rightarrow k = 0$$

(21) Answer : (B,C)

Hint:

$$l + m - 2n + 3 = 0$$

Solution:

Let the co-ordinates of point(s) be l, m and n

$$\therefore \text{Line : } \frac{x-l}{1} = \frac{y-m}{-5} = \frac{z-n}{-2}$$

$$\begin{vmatrix} 1 & -5 & -2 \\ 1 & 1 & 1 \\ l & m+5 & n+1 \end{vmatrix} = 0 \Rightarrow l + m - 2n + 3 = 0 \quad \dots(1)$$

$$\text{Similarly } 11l + 15m - 32n + 55 = 0 \quad \dots(2)$$

Solving (1) & (2)

$$(2, -3, 1) \text{ and } (1, 2, 3)$$

(22) Answer : (A,B,D)

Hint:

$f(x)$ is discontinuous and bijective function

Solution:

$$f(x) = \begin{cases} \frac{1}{1+x} & , & 0 \leq x < 1 \\ \frac{2}{x} & , & 1 \leq x < 2 \\ \frac{3}{x-1} & , & 2 \leq x < \frac{5}{2} \end{cases}$$

Clearly $f(x)$ is discontinuous and bijective function.

$$\lim_{x \rightarrow 1^-} f(x) = \frac{1}{2} \quad \lim_{x \rightarrow 1^+} f(x) = 2$$

$$\min \left(\lim_{x \rightarrow 1^-} f(x), \lim_{x \rightarrow 1^+} f(x) \right) = \frac{1}{2} \neq f(1)$$



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Section-II

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$$\lim_{x \rightarrow 2^-} f(x) = 1, \quad \lim_{x \rightarrow 2^+} f(x) = 3$$

$$\max \left(\lim_{x \rightarrow 2^-} f(x), \lim_{x \rightarrow 2^+} f(x) \right) = 3 = f(2)$$

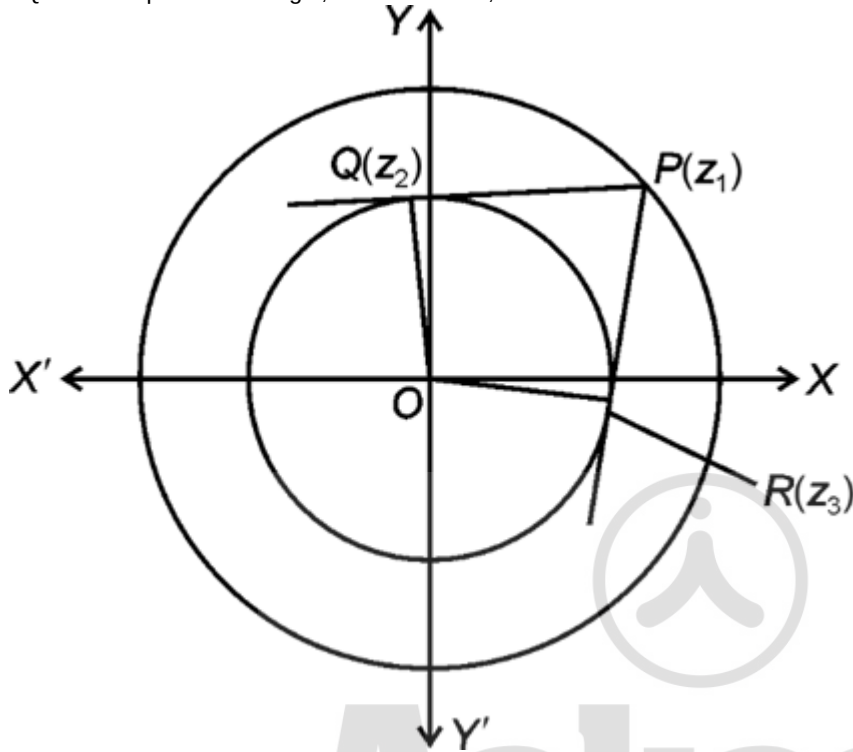
(23) Answer : (A,B,C,D)

Hint:

PQR is an equilateral triangle

Solution:

PQR is an equilateral triangle, so orthocentre, circumcentre and centroid will coincide.



$$f(z) = g(z)(z - i)(z + i) + az + b; \text{ where } a, b \in \mathbb{C}$$

$$f(i) = i \Rightarrow ai + b = i \dots (1)$$

$$f(-i) = 1 + i \Rightarrow a(-i) + b = 1 + i \dots (2)$$

From equation (1) and (2), we get

$$a = \frac{i}{2}, \quad b = \frac{1}{2} + i$$

Hence, required remainder = $az + b = \frac{1}{2}iz + \frac{1}{2} + i$

(B) $\left| \frac{z_1 + z_2 + z_3}{3} \right| = 1 \Rightarrow |z_1 + z_2 + z_3|^2 = 9$

$$\Rightarrow (z_1 + z_2 + z_3)(\bar{z}_1 + \bar{z}_2 + \bar{z}_3) = 9$$

$$\Rightarrow \left(\frac{4}{z_1} + \frac{1}{z_2} + \frac{1}{z_3} \right) \left(\frac{4}{z_1} + \frac{1}{z_2} + \frac{1}{z_3} \right) = 9$$

(C) $\angle QOR = 120^\circ$

Section-III

(24) Answer : 07.00

Hint:

$$\{(1, 1), (2, 2), (3, 3), (2, 1), (3, 2), (1, 3), (3, 1)\}$$

Solution:

$$\{(1, 1), (2, 2), (3, 3), (2, 1), (3, 2), (1, 3), (3, 1)\}$$

(25) Answer : 25.00

Hint:

$$\vec{a} \cdot \vec{b} = 0 \Rightarrow x_1 + x_2 + x_3 = 0$$

Solution:

$$\vec{a} \cdot \vec{b} = 0 \Rightarrow x_1 + x_2 + x_3 = 0$$

$$\Rightarrow \text{Coefficient of } x^0 \mid (x^{-3} + x^{-2} + x^{-1} + x^0 + x^1 + x^2)^3$$

$$x^0 \mid \left(\frac{1+x+x^2+x^3+x^4+x^5}{x^3} \right)^3$$

$$\Rightarrow x^a \text{ in } (1-x^6)^3(1-x)^{-3}$$

$$= {}^{11}C_9 - 3 \cdot {}^5C_3 = 25$$

(26) Answer : 33.00

Hint:

Median = 46 which lies in 40-50 class

Solution:

Median = 46 which lies in 40-50 class

$$\text{Median} = l + h \frac{\left\{ \frac{N}{2} - Cf \right\}}{f}$$

$$46 = 40 + 10 \left\{ \frac{\frac{195+x}{2} - (x+42)}{65} \right\} \Rightarrow x = 33$$

{ \because x is an integer }

(27) Answer : 01.00

Hint:

$$f(0) = \lim_{x \rightarrow 0} f(x) = \lim_{x \rightarrow 0} \frac{\cos(\sin x) - \cos x}{x^4}$$

Solution:

$$f(0) = \lim_{x \rightarrow 0} f(x) = \lim_{x \rightarrow 0} \frac{\cos(\sin x) - \cos x}{x^4}$$

$$\lim_{x \rightarrow 0} \frac{-2 \sin\left(\frac{\sin x + x}{2}\right) \sin\left(\frac{\sin x - x}{2}\right)}{x^4}$$

$$-2 \lim_{x \rightarrow 0} \frac{\sin\left(\frac{\sin x + x}{2}\right) \sin\left(\frac{\sin x - x}{2}\right) \left(\frac{\sin x + x}{2}\right) \left(\frac{\sin x - x}{2}\right)}{\left(\frac{\sin x + x}{2}\right) \left(\frac{\sin x - x}{2}\right) \cdot x^4} = \frac{1}{6}$$

(28) Answer : 24.00

Hint:

$$\Sigma T_n = \Sigma n^3 + \Sigma 3n^2 + \Sigma 2n$$

Solution:

$$N^r : 1 \cdot 2 \cdot 3 + 2 \cdot 3 \cdot 4 + \dots$$

$$T_n = n(n+1)(n+2)$$

$$\Sigma T_n = \Sigma n^3 + \Sigma 3n^2 + \Sigma 2n$$

$$= \left(\frac{n(n+1)}{2}\right)^2 + \frac{3n(n+1)(2n+1)}{6} + n(n+1)$$

$$D^r = 1 \cdot 2 + 2 \cdot 3 + \dots$$

$$T_n = n(n+1)$$

$$\Sigma T_n = \Sigma n^2 + \Sigma n$$

$$= \frac{n(n+1)(2n+1)}{6} + \frac{n(n+1)}{2}$$

$$\lim_{h \rightarrow \infty} \left[\frac{\left(\frac{n(n+1)}{2}\right)^2 + \frac{n(n+1)(2n+1)}{6} + n(n+1)}{n \left[\frac{n(n+1)}{2} + \frac{n(n+1)(2n+1)}{6}\right]} \right] = \frac{3}{4} \Rightarrow k = 3$$

(29) Answer : 02.00

Hint:

dividing by x^3y

$$\frac{2dx}{x} + \frac{2dy}{y} + \frac{3y^2x^4dy - 2y^3x^3dx}{x^6} = 0$$

Solution:

$$(2x^2y - 2y^4)dx + (2x^3 + 3xy^3)dy = 0$$

dividing by x^3y

$$\frac{2dx}{x} + \frac{2dy}{y} + \frac{3y^2x^4dy - 2y^3x^3dx}{x^6} = 0$$

$$2 \int \frac{dx}{x} + 2 \int \frac{dy}{y} + \int \frac{3y^2x^2dy - 2xy^3dx}{x^4} = 0$$

$$2 \ln|x| + 2 \ln|y| + \frac{y^3}{x^2} = c$$

$\therefore c = 1$

$$f(x, y) = 2 \ln|x| + 2 \ln|y| + \frac{y^3}{x^2} - 1$$



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$$f(1, -1) = -2$$

Section-IV

(30) Answer : (D)

Hint:

If a set contain n elements then number of subsets equal to 2^n **Solution:**

(P) Required number of subsets

= Total number of subsets – Number of subsets containing no even number

$$= 2^7 - 2^4$$

$$= 128 - 16$$

$$= 112$$

(Q) Prime factorization of 105 is $3 \cdot 5 \cdot 7$ We have to assign 3 to any of y_1, y_2 or y_3 similarly 5, 7 can be assign with 3 ways.Thus number of given equation is $3 \times 3 \times 3 = 27$

(R) We cannot use 0 at any place. The required number of six digit numbers is equal to number of ways of selecting 6 digit out of 9

$${}^9C_6 = {}^9C_3 = \frac{9 \cdot 8 \cdot 7}{3 \cdot 2 \cdot 1} = 84$$

(S) The number of function from

 $\{1, 2, 3, \dots, n\}$ to $\{1, 2, 3, \dots, m\}$ Where $n < m$ is m^n

Option (D) is correct

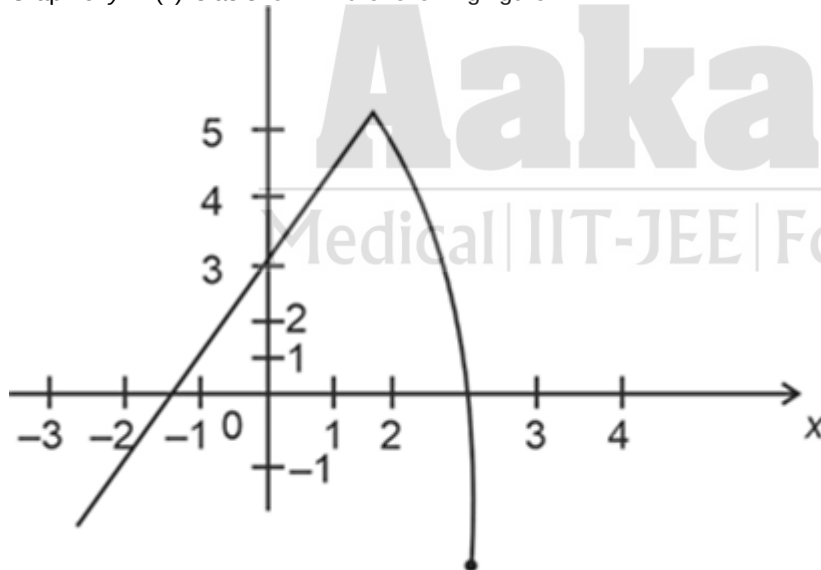
(31) Answer : (C)

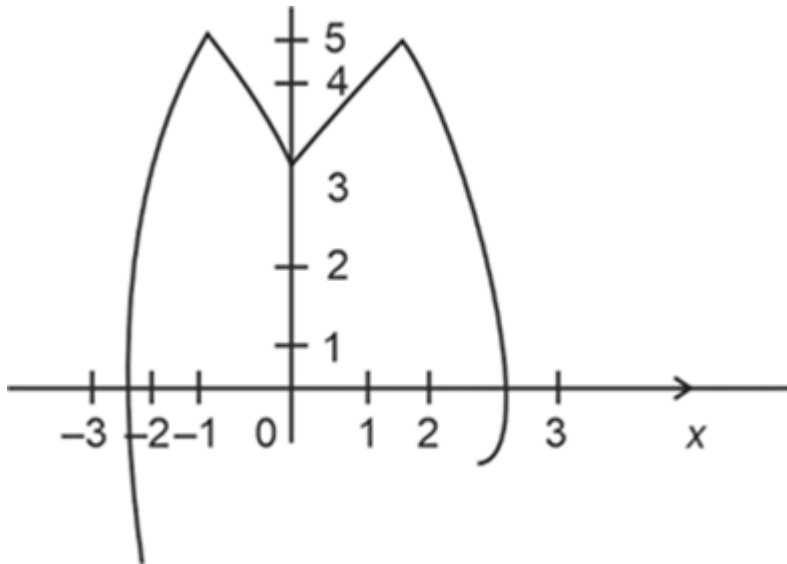
Hint:

$$f(x) = \begin{cases} 2x + 3, & x \leq 1 \\ -x^2 + 6, & x > 1 \end{cases}$$

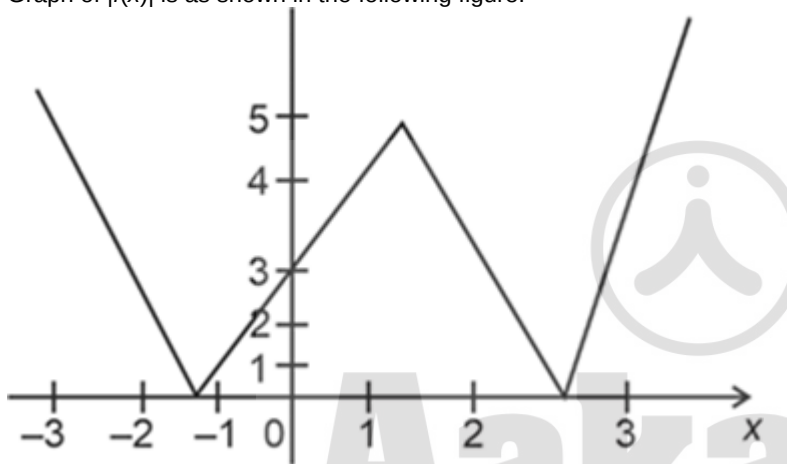
Solution:

$$f(x) = \begin{cases} 2x + 3, & x \leq 1 \\ -x^2 + 6, & x > 1 \end{cases}$$

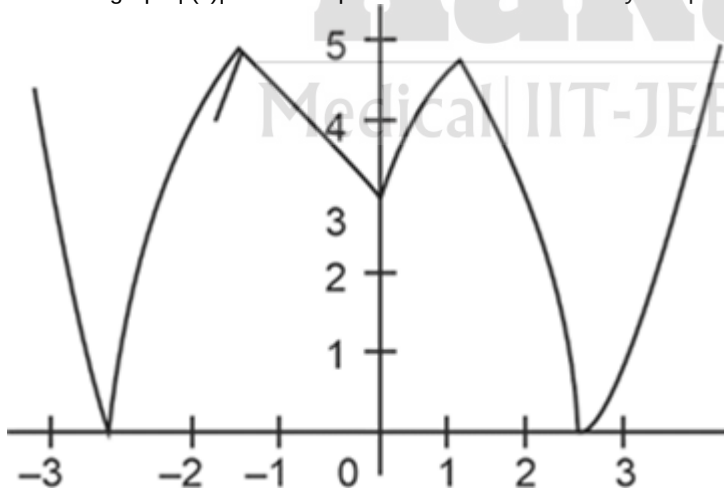
Graph of $y = f(x)$ is as shown in the following figureFrom the graph $f(x)$ has one-point of non-differentiability Graph of $f(|x|)$ is as shown in the following figure.



From the graph $f(x)$ has three points of non-differentiability
Graph of $|f(x)|$ is as shown in the following figure.



From the graph $|f(x)|$ has three points of non-differentiability. Graph of $|f(|x|)|$ is as shown in the following figure.



From the graph $|f(|x|)|$ has 5 points. of non-differentiability

(32) Answer : (B)

Hint:

3-Dimensional geometry

Solution:

(P) Line of shortest distance is perpendicular to both the lines. Hence, the vector is along the line of shortest distance $a \times b$.

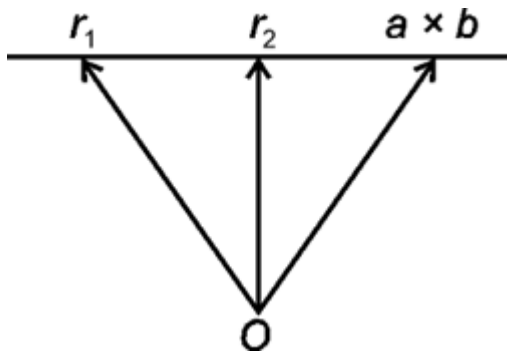
(Q) The vector $r_1 - r_2$ is along the plane in which both the straight lines are lying and $a \times b$, is the vector perpendicular to the plane of line.

$$\therefore (r_1 - r_2) \cdot (a \times b) = 0 \Rightarrow c = r_1 - r_2$$

(R) If lines are intersecting, then

$$(r_1 - r_2) \cdot (a \times b) = 0$$

(S) Since, $(r_1 - r_2)$ and $(a \times b)$ are coplanar.



$$\therefore (r_1 \times r_2) \cdot (a \times b) = 0$$

$$\therefore \text{Option (B) is correct}$$

PHYSICS

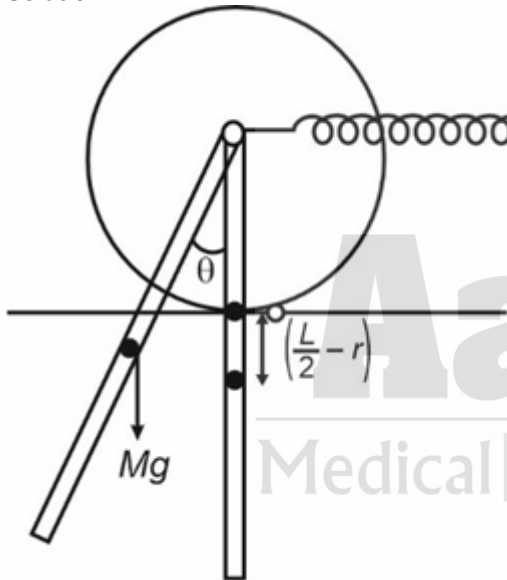
Section-I

(33) Answer : (B)

Hint:

Calculate net torque about point of contact.

Solution:



System will oscillate about 0

$$(I_{\text{system}})_0 = \frac{3}{2}Mr^2 + \frac{ML^2}{12} + M\left(\frac{L}{2} - r\right)^2$$

$$\tau_0 = \left(Mg\frac{L}{2}(\sin\theta) + K(r\theta)r\right) = (I_{\text{system}})_0 \alpha$$

$$\Rightarrow \omega^2 = \left(\frac{g\left(\frac{L}{2} + r\right)}{(I_{\text{system}})_0}\right) \left\{Kr = Mg\right\}$$

$$\omega = \left[\frac{g\left(\frac{L}{2} + r\right)}{\frac{3}{2}r^2 + \frac{L^2}{12} + \left(\frac{L}{2} - r\right)^2}\right]^{1/2}$$

(34) Answer : (D)

Hint:

$$T = 2\pi\sqrt{\frac{I}{Mgd}}$$

Solution:

$$T = 2\pi\sqrt{\frac{I}{Mgd}}$$

I – moment of inertia about hinge point.

d – distance of C.O.M.

$$100\% \times \frac{\Delta T}{T} = \frac{1}{2} \frac{\Delta I}{I}$$

$$I_1 = 12MR^2$$

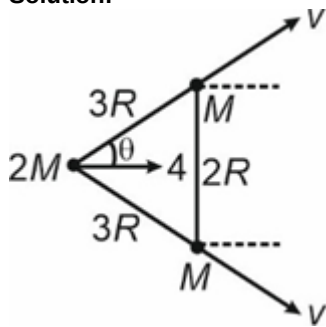
$$I_2 = \frac{23}{2}MR^2$$

(35) Answer : (D)

Hint:

Conserve linear momentum along line of motion.

Solution:



$$Mu = 2Mv\cos\theta \quad \dots(i)$$

$$e = \frac{v}{u\cos\theta} \quad \dots(ii)$$

$$\Rightarrow e = \frac{1}{2\cos^2\theta} = \frac{9}{16}$$

(36) Answer : (D)

Hint:

L.C. = 1 M.S.D - 1 V.S.D

Solution:

L.C. = 1 M.S.D - 1 V.S.D

1 V.S.D. = $\frac{9}{10}$ M.S.D.

= $\frac{1}{10}$ M.S.D = $\frac{0.1}{10}$ cm = 0.01 cm = 0.1 mm

Reading $3.2 + 0.01 \times 4 = 3.24$ cm



Section-II

(37) Answer : (B,D)

Hint:

Energy \propto (Amplitude) 2

Solution:

$$y_j = A \cos(ax + bt) = (0.2 + 0.8)A \cos(ax + bt)$$

$$y_r = -0.8A \cos(ax - bt)$$

$$y_j + y_r = A \cos ax \cos bt - A \sin ax \cdot \sin bt - 0.8 A \cos ax \cos bt - 0.8 A \sin ax \sin bt$$

$$= -1.8 A \sin ax \cdot \sin bt + 0.2 A \cos ax \cos bt$$

$$I' = 0.64I \quad \frac{I'}{I} = 0.64 = \frac{A'^2}{A^2}$$

$$\Rightarrow A' = 0.8A$$

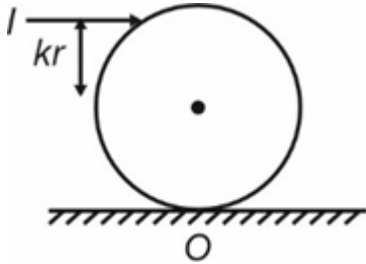
$$C = 0.2$$

(38) Answer : (B,C)

Hint:

Calculate angular impulse

Solution:



$$L_0 = I(1+k)r = I_0\omega = \frac{7}{5}mr^2\omega$$

$$= \frac{7}{5}mr(v)$$

$$v = \frac{5}{7} (1+k) \frac{I}{m}$$

$$\Rightarrow v_0 = \frac{I}{m} \quad \omega_0 = \frac{Ikr}{2/5 mr^2} = \frac{v_0}{r}$$

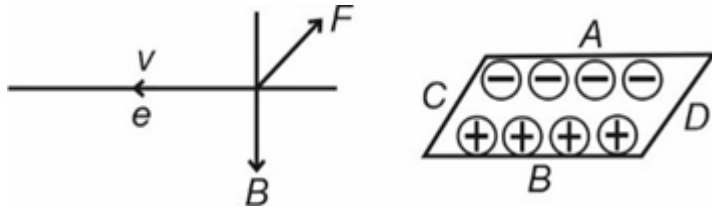
$$K = \frac{2}{5}$$

(39) Answer : (A,B)

Hint:

Electrons will experience force due to flow.

Solution:



$$\vec{E} = (\vec{v} \times \vec{B})$$

Section-III

(40) Answer : 00.00

Hint:

Ampere circuital law.

Solution:

Conceptual

(41) Answer : 02.00

Hint:

They will revolve due to their natural gravitation.

Solution:



$$\frac{2Mv^2}{l} = \frac{GM^2}{l^2}$$

$$v = \sqrt{\frac{GM}{2l}}$$

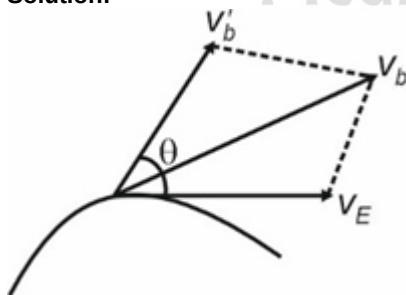
$$T = \frac{\sqrt{2}\pi r^{3/2}}{\sqrt{GM}}$$

(42) Answer : 12.00

Hint:

$$v_{eq} = v_0\sqrt{2}$$

Solution:



$$v_0 = \sqrt{\frac{GM}{R_0}} = 30 \text{ km/s}$$

$$v_{eq} = \sqrt{2}v_0$$

$$\text{So, } \Delta v = v_0(\sqrt{2} - 1)$$

$$\Delta v = 30(0.4) = 12 \text{ km/s}$$

(43) Answer : 12.00

Hint:

$$\frac{\Delta v}{v} \times 100 = 3 \cdot \frac{\Delta r}{r} \times 100$$

Solution:

$$v = \frac{4}{3}\pi r^3$$

$$\frac{\Delta v}{v} \times 100 = 3 \cdot \frac{\Delta r}{r} \times 100$$

$$= 3 \left(\frac{0.2}{5.0} \right) \times 100 = 12\%$$

(44) Answer : 04.00

Hint:

Apply Faraday's law.

Solution:

$$\phi \text{ (flux)} = \frac{N\mu_0 i R^2}{2(R^2 + l^2)^{3/2}} \times \pi r^2$$

$$\varepsilon = \frac{d\phi}{dt} = \frac{N\mu_0 b \pi R^2 r^2}{4\sqrt{l}(r^2 + l^2)^{3/2}}$$

(45) Answer : 05.00

Hint:

Mechanical energy will remain conserved.

Solution:

$$E_{(r)} = \frac{KQ'}{r^2} = \frac{KQr}{R^3}$$

$$\frac{1}{2} m v_{\min}^2 = \Delta v = q \int_0^R E \cdot dr$$

$$\frac{1}{2} m v_{\min}^2 = \frac{KqQ}{2R}$$

$$\Rightarrow v_{\min} = \sqrt{\frac{kqQ}{4\pi\epsilon_0 m R}}$$

$$\alpha = 5$$

Section-IV

(46) Answer : (D)

Hint:

$$\delta = \pi - 2i$$

(deviation)

Solution:

$$\delta = \pi - 2i$$



$$(P) i = 45^\circ$$

$$\tan \theta = \tan(90 - i) = \cot i$$

$$\Rightarrow \frac{dy}{dx} = 2 \cos\left(\frac{\pi x}{L}\right) = \cot i$$

$$h = y = \frac{2L}{\pi} \sin\left(\frac{\pi x}{L}\right) = \frac{L\sqrt{3}}{\pi}$$

$$(Q) i = 60^\circ \quad 2 \cos\left(\frac{\pi x}{L}\right) = \cot 60^\circ$$

$$h = \frac{L}{\pi} \sqrt{\frac{\pi}{3}}$$

$$(R) i = 30^\circ \quad h = \frac{L}{\pi}$$

$$(S) i = 53^\circ \quad h = \frac{L}{\pi} \sqrt{\frac{55}{16}}$$

(47) Answer : (C)

Hint:

$$e v_0 = \frac{hc}{\lambda} - \phi$$

Solution:

$$(P) n_e = \frac{P \pi r^2 \times 10^{-6}}{4\pi(100r)^2 \times E} \quad P = 3.2 \text{ mW}$$

$$= 10^5 \quad E = 5 \text{ eV}$$

$$(Q) \lambda_d = \sqrt{\frac{150}{(5-3)}} \text{ \AA} = 8.68 \text{ \AA} \quad KE = E - \phi$$

$$(R) \frac{Kq}{r} = 2 \Rightarrow q = \frac{2r}{9 \times 10^9} = 1.78 \times 10^{-12} \text{ C}$$

$$(S) q = n_e + t x_e$$

$$\Rightarrow t = \frac{q}{n_e \times e} = \frac{16}{9} \times \frac{10^{-12}}{10^5 \times 1.6 \times 10^{-19}} = \frac{10^3}{9} \text{ sec}$$

(48) Answer : (A)

Hint:

Faraday's law and Lenz's law

Solution:

(P) $v \parallel dt$, $\phi = \text{const}$ $\varepsilon = 0$

(Q) $\varepsilon = 0$, $\phi = \text{const}$. $dE = \vec{v} \times \vec{B} \cdot dt \neq 0$

(R) $\varepsilon = \frac{d\phi}{dt} = E \cdot 2\pi R$ $\vec{E} \neq 0$

(S) $\varepsilon \neq 0$ $dE = \left(\vec{v} \times \vec{B} \right) \cdot dt \neq 0$



Aakash

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