Questions & Answers

Time : 1 hr

for

Max. Marks : 120

International Olympiad Qualifiers (Part I)
Astronomy (IOQA) 2020-21

INSTRUCTIONS TO CANDIDATES

(1)   There are 32 objective type questions. Out of 32 questions, 24 questions in **Part A1** and 8 questions in **Part A2**. All questions are compulsory.

(2)   In **Part A1** each question has four alternatives out of which one is correct.

(3)   In **Part A2** each question has four alternatives out of which any number of alternative(s) (1,2,3 or 4) may be correct.

(4)   For **Part A1**, each correct answer carries 3 marks whereas 1 mark will be deducted for each wrong answer.

(5)   For **Part A2**, each correct answer carries 6 marks if all correct answers are marked and no incorrect. No negative marking for this part.

PART-A1

1. In the Period-Luminosity relationship of Cepheid variables, type I Cepheid has 4 times the luminosity than that of type II Cepheid for the same period. The distance to Andromeda Galaxy was determined by assuming a Cepheid located in it as type I. If it had been assumed to be a type II Cepheid, the distance would

   (a) Increase by a factor of 4
   (b) Increase by a factor of 2
   (c) Decrease by a factor of 4
   (d) Decrease by a factor of 2

Answer (d)

2. The energy emitted by the Sun is due to fusion reaction $4_1H^1 \rightarrow {}_2He^4 + 2_1\beta^0 + 2v_e$ (v_e are neutrinos) with a release of 27 MeV. Assume the solar constant i.e., the energy received per second per meter^2 on the surface of Earth is 1.4 k Wm^{-2}. The neutrino flux on the Earth (in m^{-2} s^{-1}) is approximately (assume that the neutrinos do not interact with anything on their way to the Earth)

   (a) 6.5×10^{14}
   (b) 6.5×10^{10}
   (c) 6.5×10^{18}
   (d) 6.5×10^{22}

Answer (a)

3. A large cluster of radius R has N stars each having a mass M. The stars are moving in the cluster such that the average kinetic energy of a star equals the magnitude of the average gravitational potential energy between two neighbouring stars. Assume the average gravitational potential energy of a star due to a neighbouring star is proportional to $\left(-\dfrac{GM^2}{r} \right)$, where r is the average distance between two stars. Then the average speed of the star is proportional to

   (a) $\sqrt{\left[\dfrac{GMN^{\frac{1}{3}}}{R} \right]}$
   (b) $\sqrt{\left[\dfrac{GMN^{\frac{2}{3}}}{R} \right]}$

   (c) $\sqrt{\left[\dfrac{GMN}{R} \right]}$
   (d) $\sqrt{\left[\dfrac{GMN^{\frac{4}{3}}}{R} \right]}$

Answer (a)

4. The distance to Venus from Earth at a particular time is 9.00×10^{10} m. Assume the orbits of Venus and Earth around the Sun to be circular with radii 1.10×10^{11} m and 1.50×10^{11} m respectively. The angle between Sun and Venus as viewed from the Earth is approximately

   (a) 20°
   (b) 47°
   (c) 60°
   (d) 80°

Answer (b)

5. As viewed from a place on the Earth, a star makes an angle of 10° with the north pole and is just circumpolar. The latitude of the place is

   (a) 10°N
   (b) 80°N
   (c) 10°S
   (d) 80°S

Answer (b)

6. The Moon makes hour angle of 40° at 6 pm on a particular day when the Sun is about to set. The hour angle of the Moon at the same time next day is approximately

   (a) 70°
   (b) 40°

   (c) −40°
   (d) 27°

Answer (d)

7. Consider a cube with one of its 6 faces open. A charge q is placed at the center of the open face. The total electric flux through the rest of the 5 faces will be nearly equal to

   (a) Zero
   (b) $\dfrac{q}{\varepsilon_0}$

   (c) $\dfrac{q}{2\varepsilon_0}$
   (d) $\dfrac{5q}{6\varepsilon_0}$

Answer (c)

8. In the diagram of solenoid shown, point P is inside the solenoid and point Q is just outside the solenoid. Which of the following is true for Magnetic Fields $\vec{B}_P$ and $\vec{B}_Q$ at point P and Q respectively?
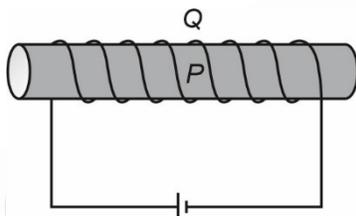
   (a) $\vec{B}_P \neq 0 \,\&\, \vec{B}_Q \approx 0$
   (b) $\vec{B}_P \approx 0 \,\&\, \vec{B}_Q \neq 0$

   (c) $\vec{B}_P \neq 0 \,\&\, \vec{B}_Q = \vec{B}_P$
   (d) $\vec{B}_P = 0 \,\&\, \vec{B}_Q \neq 0$

Answer (a)

9. A 156 Ω non-inductive resistor is connected to an AC source which generates an emf which is given by $e = 312 \sin(100\pi t + \pi\sqrt{2})$V. The value of current flowing through the resistor as measured by a millimetre (in A) will be

   (a) $2\sqrt{2}$
   (b) 2

   (c) $\sqrt{2}$
   (d) 1

Answer (c)

10. Consider an atom of mass m in an excited state, moving with a speed v, ($v << c$) along the axis. It makes a transition to the ground state by emitting a photon along the y axis. If ΔE is the energy difference between the excited state and the ground state, the frequency of the emitted photon is

   (a) $\dfrac{\Delta E}{h}$
   (b) $\dfrac{\Delta E}{h}\left[1 - \dfrac{\Delta E}{mc^2}\right]$

   (c) $\dfrac{mc^2}{h}\left[\left(\sqrt{1 + 2\dfrac{\Delta E}{mc^2}}\right) - 1\right]$
   (d) Not determinable

Answer (c)

11. Messier Object MI is

    (a) Andromeda Nebula
    (b) Crab Nebula
    (c) Orion Nebula
    (d) Horsehead Nebula

Answer (b)

12. The right ascension of winter solstice is

    (a) 18 hours
    (b) 12 hours
    (c) 6 hours
    (d) Depends on the time of the year

Answer (a)

13. The latitude and longitude of the two cities A and B are at (13.0°N, 77.6°E) and (28.7°N, 77.6°E) respectively. On 15th December 2021

    (a) The Sun will rise earlier and set later in A compared to B
    (b) The Sun will rise earlier and set earlier in A compared to B
    (c) The Sun will rise later and set earlier in A compared to B
    (d) The Sun will rise later and set later in A compared to B

Answer (a)

14. Consider the two curves $y_1 = \dfrac{4x^2}{\pi^2}$ and $y_2 = \sin x$ in the region $0 < x < \pi$. The angle made by the curves at the point of intersection is

    (a) $\tan^{-1}\left(\dfrac{1}{\pi}\right)$
    (b) $\tan^{-1}\left(\dfrac{4}{\pi}\right)$
    (c) $\tan^{-1}\infty$
    (d) $\tan^{-1}0$

Answer (b)

15. The three points (2, 3, −4), (1, −2, 3) and (3, 8, r) are collinear. The value of r is

    (a) 0
    (b) −10
    (c) −11
    (d) 10

Answer (c)

16. Time period of a simple pendulum is theoretically π seconds. In an experiment to measure this time period, a stop clock having least count of one-hundredth of a second is used and the time taken for 'n' oscillations is measured. The percentage error in the calculation of the time period will be

    (a) $(n\pi)^{-1}$%
    (b) π%
    (c) 2%
    (d) $2(n\pi)^{-1}$%

Answer (a)

17. A large sphere A of 20 kg being accelerated at 5.0 ms^{-2} strikes another sphere B of mass 8.0 kg. At the moment of impact, the acceleration of B is 12 ms^{-2}. The force on B at the moment of impact is

    (a) 40N
    (b) 96N
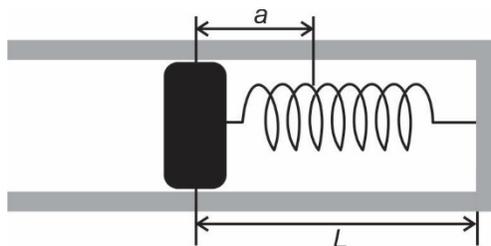   (c) 240N
    (d) 100N

Answer (b)

18. Consider that in space with no air resistance and negligible gravity, a ball of mass 250 g, initially at rest, is projected with a force of 30 N giving it a speed of 20 ms^{-1}. The ball travels a distance of 1000 m before it strikes a space ship. The original energy, E (in joule) with which the ball was projected is

(a) 30,000

(b) 50

(c) $50 < E < 30,000$

(d) None of these

Answer (b)

19. The diagram shows a mass m free to slide inside a long frictionless tube along the x-axis. It is attached to a spring of spring constant k whose unscratched length is L. Initially the mass is pushed to a position $x = a(<L)$ and released from rest. Let there be a certain position $x = x_m$ at which the maximum power, P_{max}, is generated due to kinetic energy. The values x_m and P_{max} are respectively

(a) $\dfrac{a}{2}$ & $\left(\dfrac{3ka^2}{2}\sqrt{\dfrac{k}{m}}\right)$

(b) 0 & $\left(ka^2\sqrt{\dfrac{k}{m}}\right)$

(c) $\dfrac{a}{\sqrt{2}}$ & $\left(\dfrac{ka^2}{2}\sqrt{\dfrac{k}{m}}\right)$

(d) $\dfrac{3a}{4}$ & $\left(2ka^2\sqrt{\dfrac{k}{m}}\right)$

Answer (c)

20. The value of $\tan^{-1}\left[\dfrac{\cos x}{1-\sin x}\right]$ is equal to

(a) $\dfrac{x}{2}$

(b) $\dfrac{x}{2}-\dfrac{\pi}{2}$

(c) $\dfrac{x}{2}-\dfrac{\pi}{4}$

(d) $\dfrac{x}{2}+\dfrac{\pi}{4}$

Answer (d)

21. The determinant $\begin{vmatrix} 1 & 1 & -1 \\ -1 & 1 & 1 \\ 1 & 1 & x \end{vmatrix} = 0$. The value of x is

(a) $x = 0$ or 1

(b) $x = \pm 1$

(c) $x = -1$

(d) $x = 1$

Answer (c)

22. The value of the given integral $\displaystyle\int_{\pi/3}^{\pi/4} \frac{dx}{\sin^2 x . \cos^2 x}$ is

(a) $\dfrac{\pi}{4} - \dfrac{\pi}{3}$

(b) 0

(c) $\dfrac{1}{\sqrt{3}}$

(d) $-\dfrac{2}{\sqrt{3}}$

Answer (d)

23. Consider the four points A, B, C, D forming a regular tetrahedron with sides each of length L. The coordinates (x, y, z) of A, B and C are $A\,(0, 0, 0)$, $B\,(L, O, O)$ and $C\left(\dfrac{L}{2}, \dfrac{L\sqrt{3}}{2}, 0\right)$. The possible coordinates of D are

(a) $\left(\dfrac{L}{2}, \dfrac{L}{2}, \pm\dfrac{L}{\sqrt{2}}\right)$

(b) $\left(\dfrac{L}{2}, \dfrac{L}{2\sqrt{3}}, \pm\dfrac{L\sqrt{2}}{\sqrt{3}}\right)$

(c) $\left(\dfrac{L}{\sqrt{2}}, \dfrac{L}{\sqrt{3}}, \pm\dfrac{L}{\sqrt{3}}\right)$

(d) $\left(\dfrac{L}{\sqrt{2}}, \dfrac{L}{\sqrt{3}}, \pm\dfrac{L\sqrt{5}}{\sqrt{12}}\right)$
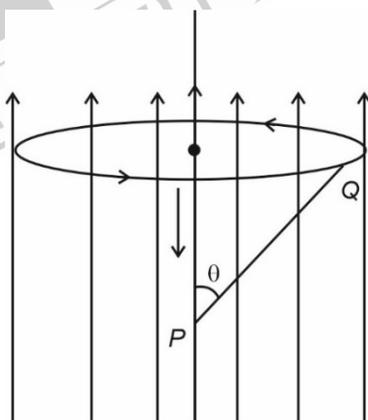
Answer (b)

24. The argument of the complex number $z = \dfrac{1+i}{1-i\sqrt{3}}$ is

(a) π

(b) $\dfrac{7\pi}{12}$

(c) $-\dfrac{5\pi}{12}$

(d) $\dfrac{5\pi}{12}$

Answer (b)

PART-A2

25. A uniform magnetic field $\vec{B} = B_0 \hat{k}$ exists over a certain region of space as shown in figure. A metal rod PQ of length L is fixed at P and PQ makes a constant angle of θ with $\hat{k}$ as it rotates about $\hat{k}$ with a constant angular velocity ω.

(a) The velocity of point Q is $\vec{v} = \vec{\omega} \times \vec{L}$

(b) The magnitude of induced electric field along the rod at a distance r from P is $E = r\omega B_0 \sin^2\theta$

(c) The magnitude of e.m.f. developed between P and Q is $= 0.5L^2 \omega B_0 \sin 2\theta$

(d) The magnitude of emf developed between P and Q is $= 0.5L^2 \omega B_0 \sin^2\theta$

Answer (a, b, d)

26. Spectroscopic analysis of light from stars gives us information about

    (a) The abundance of elements in the stars

    (b) Parallax of stars

    (c) The radial velocity of stars

    (d) Proper motion of stars

Answer (a, b, c)

27. Which of the following terms refer to a variable star?

    (a) White dwarf
    (b) RR Lyrae

    (c) Black hole
    (d) Eclipsing binary

Answer (a, b, d)

28. Which of the statement(s) about Globular cluster(s) is/are true?

    (a) They are in the outer regions of the Milky Way

    (b) They comprise of variable stars

    (c) They comprise of young stars

    (d) They are receding from us at very high speed

Answer (a, b, d)

29. If a and b are real numbers, the equation $a(x+3)^2 + b(y+4)^2 = 1$ represents

    (a) An ellipse or a circle if $a > 0$ and $b > 0$

    (b) An ellipse or a circle if $a < 0$ and $b < 0$

    (c) A hyperbola if $a > 0$ and $b < 0$ or $a < 0$ and $b > 0$

    (d) A parabola if $a > 0$ and $b = 0$

Answer (a, c)

30. If $\tan\theta = \cot\left(\dfrac{\pi}{3}\right)$ then θ can be

    (a) $\dfrac{\pi}{6}$
    (b) $\dfrac{7\pi}{6}$

   (c) $\dfrac{13\pi}{6}$
    (d) $\dfrac{5\pi}{6}$

Answer (a, b, c)

31. The critical velocity of a flowing liquid depends on

    (a) Coefficient of viscosity
    (b) Reynold number

    (c) Density of the liquid
    (d) Diameter of the tube

Answer (a, b, c, d)

32. Consider the situation as shown in the diagram where a symmetric biconvex lens is half covered with an opaque object. Given that the object shown *AB* is symmetric about the principal axis, which of the following is true about the image seen on the screen?
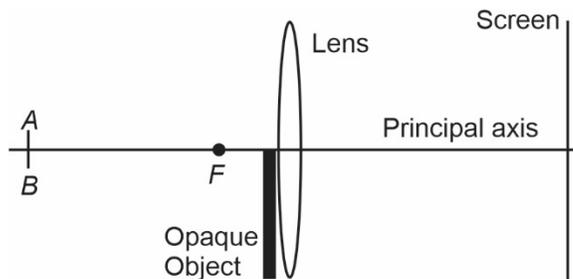
(a) Full image of *AB* is formed

(b) Intensity of the image is reduced

(c) Full image of *AB* is formed and the intensity is reduced

(d) Only half of *AB* is visible

Answer (a, b, c)