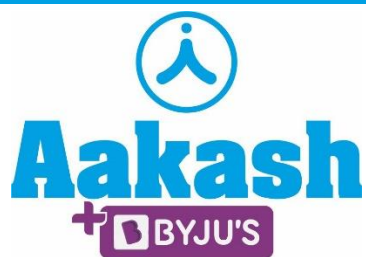


31/01/2024

Morning



Corporate Office : Aakash Tower, 8, Pusa Road, New Delhi-110005 | Ph.: 011-47623456

Answers & Solutions

Time : 3 hrs.

M.M. : 300

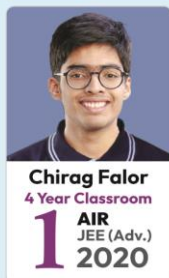
for

JEE (Main)-2024 (Online) Phase-1

(Mathematics, Physics and Chemistry)

IMPORTANT INSTRUCTIONS:

- (1) The test is of **3 hours** duration.
- (2) This test paper consists of 90 questions. Each subject (MPC) has 30 questions. The maximum marks are 300.
- (3) This question paper contains **Three Parts**. **Part-A** is Mathematics, **Part-B** is Physics and **Part-C** is Chemistry. Each part has only two sections: **Section-A** and **Section-B**.
- (4) **Section - A** : Attempt all questions.
- (5) **Section - B** : Attempt any 05 questions out of 10 Questions.
- (6) **Section - A (01 – 20)** contains 20 multiple choice questions which have **only one correct answer**. Each question carries **+4 marks** for correct answer and **–1 mark** for wrong answer.
- (7) **Section - B (21 – 30)** contains 10 **Numerical value** based questions. The answer to each question should be rounded off to the **nearest integer**. Each question carries **+4 marks** for correct answer and **–1 mark** for wrong answer.



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MATHEMATICS

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer:

1. The solution curve of the differential equation

$$y \frac{dx}{dy} = x(\log_e x - \log_e y + 1), \quad x > 0, y > 0$$

passing through the point (e, 1) is

- (1) $\left| \log_e \frac{x}{y} \right| = y$ (2) $\left| \log_e \frac{y}{x} \right| = x$
(3) $\left| \log_e \frac{y}{x} \right| = y^2$ (4) $2 \left| \log_e \frac{x}{y} \right| = y + 1$

Answer (1)

Sol. $y \frac{dx}{dy} = x(\log_e x - \log_e y + 1)$

$$\frac{dx}{dy} = \frac{x}{y} \left(\log_e \frac{x}{y} + 1 \right)$$

Let $x = vy$

$$\frac{dx}{dy} = v + y \frac{dv}{dy}$$

$$\Rightarrow v + y \frac{dv}{dy} = v \log_e v + v$$

$$\Rightarrow y \frac{dv}{dy} = v \log_e v$$

$$\Rightarrow \int \frac{dv}{v \log_e v} = \int \frac{dy}{y}$$

$$\Rightarrow \log_e (\log_e v) = \log_e y + \log_e c$$

$$\Rightarrow \log_e v = y c$$

$$\Rightarrow \log_e \left(\frac{x}{y} \right) = y c$$

It passes through (e, 1)

$$\Rightarrow \log_e e = c \Rightarrow c = 1$$

$$\Rightarrow y = \log_e \left(\frac{x}{y} \right)$$

2. For $0 < c < b < a$, let $(a + b - 2c)x^2 + (b + c - 2a)x + (c + a - 2b) = 0$ and $\alpha \neq 1$ be one of its root. Then, among the two statements

(I) If $\alpha \in (-1, 0)$, then b cannot be the geometric mean of a and c

(II) If $\alpha \in (0, 1)$, then b may be the geometric mean of a and c

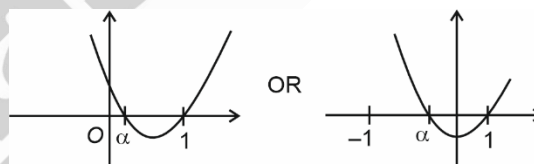
- (1) Only (I) is true
(2) Only (II) is true
(3) Neither (I) nor (II) is true
(4) Both (I) and (II) are true

Answer (4)

Sol. $f(x) = (a + b - 2c)x^2 + (b + c - 2a)x + (c + a - 2b)$

Clearly $f(1) = 0 \Rightarrow x = 1$ is a root.

Coefficient of $x^2 = a + b - 2c = (a - c) + (b - c) > 0$.



For I, if $\alpha \in (-1, 0) \Rightarrow f(-1) f(0) < 0$

$$\Rightarrow 2(2a - b - c)(c + a - 2b) < 0$$

$$\Rightarrow c + a - 2b < 0 \text{ as } 2a - b - c > 0$$

$$\Rightarrow \frac{c+a}{2} < b \Rightarrow \text{A.M. of } a \text{ and } c \text{ is less than } b.$$

Hence b cannot be G.M of a and c

For II, if $\alpha \in (0, 1) \Rightarrow f(0) f(1^-) < 0$

$$\Rightarrow c + a - 2b > 0 \text{ as } f(1^-) < 0$$

$$\Rightarrow \frac{c+a}{2} > b \Rightarrow b \text{ can be G.M of } a \text{ and } c.$$



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3. If $f(x) = \begin{vmatrix} x^3 & 2x^2+1 & 1+3x \\ 3x^2+2 & 2x & x^3+6 \\ x^3-x & 4 & x^2-2 \end{vmatrix}$ for all $x \in \mathbb{R}$, then

$2f(0) + f'(0)$ is equal to

- (1) 24 (2) 42
(3) 48 (4) 18

Answer (2)

Sol. $f(x) = \begin{vmatrix} x^3 & 2x^2+1 & 1+3x \\ 3x^2+2 & 2x & x^3+6 \\ x^3-x & 4 & x^2-2 \end{vmatrix}$

$f'(x) = \begin{vmatrix} 3x^2 & 2x^2+1 & 1+3x \\ 6x & 2x & x^3+6 \\ 3x^2-1 & 4 & x^2-2 \end{vmatrix}$

$+ \begin{vmatrix} x^3 & 4x & 1+3x \\ 3x^2+2 & 2 & x^3+6 \\ x^3-x & 0 & x^2-2 \end{vmatrix}$

$+ \begin{vmatrix} x^3 & 2x^2+1 & 3 \\ 3x^2+2 & 2x & 3x^2 \\ x^3-x & 4 & 2x \end{vmatrix}$

$f'(0) = \begin{vmatrix} 0 & 1 & 1 \\ 0 & 0 & 6 \\ -1 & 4 & -2 \end{vmatrix} + \begin{vmatrix} 0 & 0 & 1 \\ 2 & 2 & 6 \\ 0 & 0 & -2 \end{vmatrix} + \begin{vmatrix} 0 & 1 & 3 \\ 2 & 0 & 0 \\ 0 & 4 & 0 \end{vmatrix}$

$f'(0) = 6 + 0 + 12$

$f'(0) = 18$

$f(0) = \begin{vmatrix} 0 & 1 & 1 \\ 2 & 0 & 6 \\ 0 & 4 & -2 \end{vmatrix}$

$f(0) = 12$

$2f(0) + f'(0) = 24 + 18$
 $= 42$

4. $\lim_{x \rightarrow 0} \frac{e^{2|\sin x|} - 2|\sin x| - 1}{x^2}$

- (1) Is equal to -1 (2) Is equal to 2
(3) Is equal to 1 (4) Does not exist

Answer (2)

Sol. $\lim_{x \rightarrow 0} \frac{e^{2|\sin x|} - 2|\sin x| - 1}{x^2}$

Since, it is an even function

$\Rightarrow \text{LHL} = \text{RHL}$

$\text{RHL} = \lim_{x \rightarrow 0^+} \frac{e^{2\sin x} - 2\sin x - 1}{x^2}$

$= \lim_{x \rightarrow 0^+} \frac{e^{2\sin x}(2\cos x) - 2\cos x}{2x}$

$= \lim_{x \rightarrow 0^+} \left(\frac{e^{2\sin x} - 1}{2\sin x} \right) \left(\frac{2\sin x}{x} \right) \cos x$

$= 1 \times 2 \times 1$

$= 2$

5. If $f(x) = \frac{4x+3}{6x-4}$, $x \neq \frac{2}{3}$ and $(fof)(x) = g(x)$, where

$g: \mathbb{R} - \left\{ \frac{2}{3} \right\} \rightarrow \mathbb{R} - \left\{ \frac{2}{3} \right\}$, then $(gogog)(4)$ is equal to

- (1) $\frac{19}{20}$ (2) 4
(3) $-\frac{19}{20}$ (4) -4

Answer (2)

Sol. Given $f(x) = \frac{4x+3}{6x-4}$, $x \neq \frac{2}{3}$

and $g(x) = (fof)(x)$

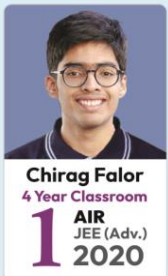
$= 4 \left(\frac{4x+3}{6x-4} \right) + 3$
 $= \frac{4 \left(\frac{4x+3}{6x-4} \right) - 4}{6 \left(\frac{4x+3}{6x-4} \right) - 4}$

$= \frac{16x+12+18x-12}{24x+18-24x+16}$

$= \frac{34x}{34} = x$

$\therefore (gogog)(x) = x$

$\Rightarrow (gogog)(4) = 4$



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6. For $\alpha, \beta, \gamma \neq 0$, if $\sin^{-1}\alpha + \sin^{-1}\beta + \sin^{-1}\gamma = \pi$ and $(\alpha + \beta + \gamma)(\alpha - \gamma + \beta) = 3\alpha\beta$, then γ equals

- (1) $\sqrt{3}$ (2) $\frac{\sqrt{3}}{2}$
(3) $\frac{\sqrt{3}-1}{2\sqrt{2}}$ (4) $\frac{1}{\sqrt{2}}$

Answer (2)

Sol. Let $\sin^{-1}\alpha = A$, $\sin^{-1}\beta = B$ and $\sin^{-1}\gamma = C$

$$\therefore A + B + C = \pi$$

$$\text{Also, } (\alpha + \beta + \gamma)(\alpha - \gamma + \beta) = 3\alpha\beta$$

$$\Rightarrow (\alpha + \beta)^2 - \gamma^2 = 3\alpha\beta$$

$$\Rightarrow \alpha^2 + \beta^2 - \gamma^2 = \alpha\beta$$

$$\Rightarrow \frac{\alpha^2 + \beta^2 - \gamma^2}{2\alpha\beta} = \frac{1}{2}$$

$$\Rightarrow \cos C = \frac{1}{2} \Rightarrow C = 60^\circ$$

$$\therefore \sin C = \frac{\sqrt{3}}{2} = \gamma$$

7. The area of the region

$$\left\{ (x, y) : y^2 \leq 4x, x < 4, \frac{xy(x-1)(x-2)}{(x-3)(x-4)} > 0, x \neq 3 \right\}$$

is

- (1) $\frac{8}{3}$ (2) $\frac{32}{3}$
(3) $\frac{16}{3}$ (4) $\frac{64}{3}$

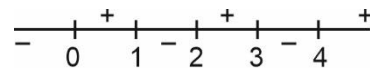
Answer (2)

Sol. Case I:

When $y \geq 0$

$$\text{Then } \frac{xy(x-1)(x-2)}{(x-3)(x-4)} < 0$$

$$\frac{x(x-1)(x-2)}{(x-3)(x-4)} < 0$$



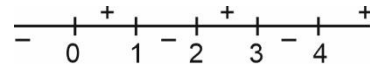
$$x \in (1, 2) \cup (3, 4)$$

Case II:

$$y < 0$$

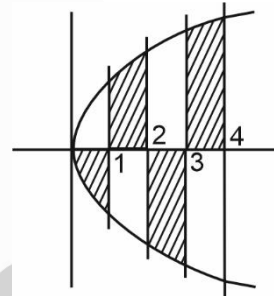
$$\frac{xy(x-1)(x-2)}{(x-3)(x-4)} < 0$$

$$\frac{x(x-1)(x-2)}{(x-3)(x-4)} > 0$$



$$x \in (0, 1) \cup (2, 3)$$

Required region



So, required area

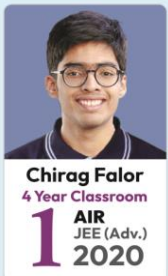
$$= \int_0^4 \sqrt{4x} \, dx = \left(2 \left(x^{3/2} \right) \frac{2}{3} \right)_0^4$$

$$= \frac{4}{3} (4 \times 2 - 0) = \frac{32}{3}$$

8. Let $\alpha, \beta, \gamma, \delta \in \mathbb{Z}$ and let $A(\alpha, \beta)$, $B(1, 0)$, $C(\gamma, \delta)$ and $D(1, 2)$ be the vertices of a parallelogram $ABCD$. If $AB = \sqrt{10}$ and the points A and C lie on the line $3y = 2x + 1$, then $2(\alpha + \beta + \gamma + \delta)$ is equal to

- (1) 10 (2) 8
(3) 12 (4) 5

Answer (2)



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Sol. $ABCD$ is a parallelogram so mid-point of AC = mid-point of BD

$$\Rightarrow \left(\frac{\alpha + \gamma}{2}, \frac{\beta + \delta}{2} \right) = \left(\frac{1+1}{2}, \frac{0+2}{2} \right)$$

$$\Rightarrow \left(\frac{\alpha + \gamma}{2}, \frac{\beta + \delta}{2} \right) = (1, 1)$$

$$\Rightarrow \alpha + \gamma = 2 \text{ and } \beta + \delta = 2$$

$$\text{So, } 2(\alpha + \beta + \gamma + \delta) = 2(2 + 2) = 8$$

9. Let $y = y(x)$ be the solution of the differential equation $\frac{dy}{dx} = \frac{(\tan x) + y}{\sin x(\sec x - \sin x \tan x)}$, $x \in \left(0, \frac{\pi}{2}\right)$

satisfying the condition $y\left(\frac{\pi}{4}\right) = 2$. Then, $y\left(\frac{\pi}{3}\right)$ is

(1) $\sqrt{3}(2 + \log_e 3)$ (2) $\sqrt{3}(1 + 2\log_e 3)$

(3) $\frac{\sqrt{3}}{2}(2 + \log_e 3)$ (4) $\sqrt{3}(2 + \log_e \sqrt{3})$

Answer (4)

Sol. $\frac{dy}{dx} = \frac{\tan x}{\sin x(\sec x - \sin x \tan x)} + \frac{y}{\sin x(\sec x - \sin x \tan x)}$

$$\frac{dy}{dx} = \frac{1}{\cos x(\sec x - \sin x \tan x)} + \frac{y}{\sin x(\sec x - \sin^2 x \sec x)}$$

$$\frac{dy}{dx} = \frac{1}{1 - \sin^2 x} + \frac{y}{\sin x \sec x (1 - \sin^2 x)}$$

$$\frac{dy}{dx} = \frac{1}{\cos^2 x} + \frac{y}{\sin x \cos x}$$

$$\frac{dy}{dx} - y(\sec x \csc x) = \sec^2 x$$

$$\begin{aligned} \text{I.F} &= e^{-\int \frac{1}{\sin x \cos x} dx} \\ &= e^{-2 \int \csc 2x dx} \\ &= e^{-\ln \tan x} \\ &= \frac{1}{\tan x} = \cot x \end{aligned}$$

$$\therefore y \cdot \cot x = \int \frac{1}{\cos^2 x} \cdot \cot x dx$$

$$y \cot x = \int \frac{1}{\sin x \cos x} dx$$

$$y \cot x = 2 \int \csc 2x dx$$

$$y \cot x = \ln \tan x + c \quad \dots(i)$$

$$y\left(\frac{\pi}{4}\right) = 2$$

$$\therefore 2 \cot \frac{\pi}{4} = \ln \tan \frac{\pi}{4} + c$$

$$2 = 0 + c$$

$$2 = c$$

$$\therefore \cot x = \ln \tan x + 2 \text{ (from i)}$$

$$\text{Put } x = \frac{\pi}{3}$$

$$y \cot\left(\frac{\pi}{3}\right) = \ln \tan \frac{\pi}{3} + 2$$

$$y \frac{1}{\sqrt{3}} = \ln \sqrt{3} + 2$$

$$y = \sqrt{3} [\ln(\sqrt{3}) + 2]$$

Option (4) is correct

10. Let $g(x)$ be a linear function and

$$f(x) = \begin{cases} g(x), & x \leq 0 \\ \left(\frac{1+x}{2+x}\right)^{\frac{1}{x}}, & x > 0 \end{cases}, \text{ is continuous at } x = 0. \text{ If}$$

$f(1) = f(-1)$, then the value $g(3)$ is

(1) $\log_e \left(\frac{4}{9}\right) - 1$ (2) $\log_e \left(\frac{4}{9e^{1/3}}\right)$

(3) $\frac{1}{3} \log_e \left(\frac{4}{9}\right) + 1$ (4) $\frac{1}{3} \log_e \left(\frac{4}{9e^{1/3}}\right)$

Answer (2)



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Sol. Let $g(x) = ax + b$

$f(x)$ is continuous at $x = 0$

$$\therefore \lim_{x \rightarrow 0^+} \left(\frac{1+x}{2+x} \right)^{\frac{1}{x}} = \left(\frac{1}{2} \right)^{\infty} = 0$$

$$\lim_{x \rightarrow 0^-} g(x) = \lim_{x \rightarrow 0^-} ax + b = b$$

So, $b = 0$

$$\text{Now, } f(x) = \left(\frac{1+x}{2+x} \right)^{\frac{1}{x}}$$

$$\ln f(x) = \frac{1}{x} [\ln(1+x) - \ln(2+x)]$$

$$\frac{1}{f(x)} \cdot f'(x) = \frac{x \left[\frac{1}{1+x} - \frac{1}{2+x} \right] - \ln \left(\frac{1+x}{2+x} \right)}{x^2}$$

$$f'(1) = f(1) \left[\frac{\left(\frac{1}{2} - \frac{1}{3} \right) - \ln \left(\frac{2}{3} \right)}{1} \right]$$

$$f'(1) = \frac{2}{3} \left[\frac{1}{6} - \ln \frac{2}{3} \right] \quad \dots(1)$$

Also $f(-1) = a(-1) + b$

$$f(-1) = -a \quad \dots(2)$$

\therefore from (1) and (2)

$$-a = \frac{1}{9} - \frac{2}{3} \ln \frac{2}{3}$$

$$a = \frac{2}{3} \ln \left(\frac{2}{3} \right) - \frac{1}{9}$$

$\therefore g(x) = ax$

$$g(3) = 3 \left(\frac{2}{3} \ln \left(\frac{2}{3} \right) - \frac{1}{9} \right)$$

$$g(3) = 2 \ln \left(\frac{2}{3} \right) - \frac{1}{3}$$

$$g(3) = \ln \frac{4}{9} - \frac{1}{3}$$

$$g(3) = \ln \frac{4}{9} - \ln e^{1/3}$$

$$g(3) = \ln \left(\frac{4}{9 \cdot e^{1/3}} \right)$$

$$g(3) = \log_e \left(\frac{4}{9e^{1/3}} \right)$$

Option (2) is correct

11. The distance of the point $Q(0, 2, -2)$ from the line passing through the point $P(5, -4, 3)$ and perpendicular to the lines

$$\vec{r} = (-3\hat{i} + 2\hat{k}) + \lambda(2\hat{i} + 3\hat{j} + 5\hat{k}), \lambda \in \mathbb{R} \quad \text{and}$$

$$\vec{r} = (\hat{i} - 2\hat{j} + \hat{k}) + \mu(-\hat{i} + 3\hat{j} + 2\hat{k}), \mu \in \mathbb{R} \text{ is :}$$

$$(1) \sqrt{20}$$

$$(2) \sqrt{54}$$

$$(3) \sqrt{86}$$

$$(4) \sqrt{74}$$

Answer (4)

$$\text{Sol. } \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & 3 & 5 \\ -1 & 3 & 2 \end{vmatrix}$$

$$\hat{i}(6-15) - \hat{j}(4+5) + \hat{k}(6+3)$$

$$-9\hat{i} - 9\hat{j} + 9\hat{k}$$

Required line

$$\frac{x-5}{1} = \frac{y+4}{1} = \frac{z-3}{-1} = \lambda$$

$$\Rightarrow x = \lambda + 5, y = \lambda - 4, z = -\lambda + 3$$

$$Q(0, 2, -2)$$

d

$$P(5, -4, 3) R(\lambda + 5, \lambda - 4, -\lambda + 3)$$

$$\overrightarrow{QR} \cdot \vec{l} = (\lambda + 5)1 + (\lambda - 6)1 + (3 - \lambda + 2)(-1) = 0$$

$$\Rightarrow \lambda = 2$$

$$R = (7, -2, 1)$$

$$QR = \sqrt{49 + 16 + 9}$$

$$= \sqrt{74}$$



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12. If the foci of a hyperbola are same as that of the ellipse $\frac{x^2}{9} + \frac{y^2}{25} = 1$ and the eccentricity of the hyperbola is $\frac{15}{8}$ times the eccentricity of the ellipse, then the smaller focal distance of the point $\left(\sqrt{2}, \frac{14}{3}\sqrt{\frac{2}{5}}\right)$ on the hyperbola, is equal to

- (1) $7\sqrt{\frac{2}{5}} + \frac{8}{3}$ (2) $14\sqrt{\frac{2}{5}} - \frac{4}{3}$
 (3) $7\sqrt{\frac{2}{5}} - \frac{8}{3}$ (4) $14\sqrt{\frac{2}{5}} - \frac{16}{3}$

Answer (3)

Sol. Foci of hyperbola is same as that of ellipse

$$\frac{x^2}{9} + \frac{y^2}{25} = 1$$

$$a_1 = 3$$

$$b_1 = 5$$

$$\text{foci} = (0, \pm b_1 e_1)$$

$$e_1 = \sqrt{1 - \frac{a_1^2}{b_1^2}}$$

$$\text{foci} = \left(0, \pm 5 \cdot \frac{4}{5}\right)$$

$$e_1 = \sqrt{1 - \frac{9}{25}} = \frac{4}{5}$$

$$\text{foci} = (0, \pm 4)$$

Take eccentricity of hyperbola = e_2

$$e_2 = \frac{15}{8} \times e_1 = \frac{15}{8} \times \frac{4}{5} = \frac{3}{2}$$

foci of hyperbola

$$(0, \pm b_2 e_2) = (0, \pm 4)$$

$$b_2 \cdot \frac{3}{2} = 4$$

$$b_2 = \frac{8}{3}$$

$$e_2 = \sqrt{1 + \frac{a_2^2}{b_2^2}} = \sqrt{1 + \frac{9a_2^2}{64}}$$

$$e_2 = \sqrt{\frac{64 + 9a_2^2}{64}}$$

$$\frac{9}{4} = \frac{64 + 9a_2^2}{64}$$

$$144 - 64 = 9a_2^2$$

$$\frac{80}{9} = a_2^2$$

Now, smaller focal distance

$$\left(\sqrt{2}, \frac{14}{3}\sqrt{\frac{2}{5}}\right) \text{ and } (0, 4)$$

$$\sqrt{2 + \left(\frac{14}{3}\sqrt{\frac{2}{5}} - 4\right)^2}$$

$$= \sqrt{\frac{1202}{45} - \frac{28}{3}\sqrt{\frac{2}{5}}}$$

$$\text{Which is } 7\sqrt{\frac{2}{5}} - \frac{8}{3}$$

13. Let a be the sum of all coefficients in the expansion of $(1 - 2x + 2x^2)^{2023} (3 - 4x^2 + 2x^3)^{2024}$ and

$$b = \lim_{x \rightarrow 0} \left(\frac{\int_0^x \frac{\log(1+t)}{t^{2024} + 1} dt}{x^2} \right). \text{ If the equations } cx^2 + dx +$$

$e = 0$ and $2bx^2 + ax + 4 = 0$ have a common root, where $c, d, e \in \mathbb{R}$, then $d : c : e$ equal

- (1) $1 : 1 : 4$ (2) $4 : 1 : 4$
 (3) $2 : 1 : 4$ (4) $1 : 2 : 4$

Answer (1)

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Sol. Sum of all coefficients in the expansion of $(1 - 2x + 2x^2)^{2023} (3 - 4x^2 + 2x^3)^{2024}$

Put $x = 1$

$$1^{2023} \cdot 1^{2024} = 1$$

$$a = 1$$

$$b = \lim_{x \rightarrow 0} \left[\frac{\int_0^x \frac{\log(1+t)}{t^{2024} + 1} dt}{x^2} \right]$$

Apply L-Hospital here

$$\lim_{x \rightarrow 0} \frac{\frac{\log(1+x)}{x^{2024} + 1}}{2x} = \lim_{x \rightarrow 0} \frac{\log(1+x)}{2x(x^{2024} + 1)}$$

Again apply L. Hospital here :

$$\lim_{x \rightarrow 0} \frac{\frac{1}{1+x}}{2(x^{2024} + 1) + 2x(2024x^{2023} + 1)}$$

$$b = \frac{1}{2}$$

$$2bx^2 + ax + 4 = x^2 + x + 4 = 0$$

$$D < 0$$

So roots are imaginary.

So they occur in pair.

So both roots have to be common.

It implies both equation are same as $c, d, e \in R$

$$cx^2 + dx + e = 0 \text{ is same as}$$

$$x^2 + x + 4 = 0$$

$$c = 1, d = 1, e = 4$$

$$d : c : e = 1 : 1 : 4$$

14. Let $\vec{a} = 3\hat{i} + \hat{j} - 2\hat{k}$, $\vec{b} = 4\hat{i} + \hat{j} + 7\hat{k}$ and $\vec{c} = \hat{i} - 3\hat{j} + 4\hat{k}$ be three vectors. If a vectors \vec{p} satisfies $\vec{p} \times \vec{b} = \vec{c} \times \vec{b}$ and $\vec{p} \cdot \vec{a} = 0$, then $\vec{p} \cdot (\hat{i} - \hat{j} - \hat{k})$ is equal to

- (1) 36 (2) 24
(3) 28 (4) 32

Answer (4)

$$\text{Sol. } \vec{a} = (3\hat{i} + \hat{j} - 2\hat{k})$$

$$\vec{b} = (4\hat{i} + \hat{j} + 7\hat{k})$$

$$\vec{c} = (\hat{i} - 3\hat{j} + 4\hat{k})$$

$$\vec{p} \times \vec{b} = \vec{c} \times \vec{b}$$

$$\Rightarrow (\vec{p} - \vec{c}) \times \vec{b} = 0$$

$$\Rightarrow \vec{p} = \vec{c} + \lambda \vec{b}$$

$$\therefore \vec{p} \cdot \vec{a} = 0 \Rightarrow \vec{c} \cdot \vec{a} + \lambda \vec{b} \cdot \vec{a} = 0$$

$$\Rightarrow \lambda = -\left(\frac{\vec{c} \cdot \vec{a}}{\vec{b} \cdot \vec{a}}\right) = -\frac{(3 \times 1 + 1 \times (-3) + (-2) \times 4)}{(3 \times 4 + 1 \times 1 + (-2) \times 7)} = -8$$

$$\text{Here } \vec{p} = -31\hat{i} - 11\hat{j} - 52\hat{k}$$

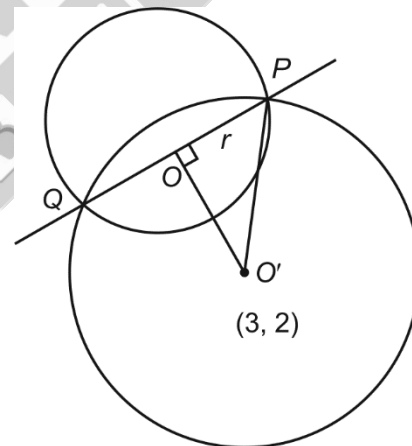
$$\vec{p} \cdot (\hat{i} - \hat{j} - \hat{k}) = 32$$

15. If one of the diameters of the circle $x^2 + y^2 - 10x + 4y + 13 = 0$ is a chord of another circle C, whose center is the point of intersection of the lines $2x + 3y = 12$ and $3x - 2y = 5$, then the radius of the circle C is :

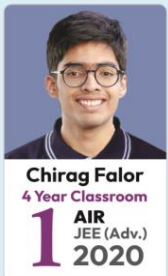
- (1) $3\sqrt{2}$ (2) $\sqrt{20}$
(3) 4 (4) 6

Answer (4)

Sol. Given circle $x^2 + y^2 - 10x + 4y + 13 = 0$



Centre (O) = (5, -2)



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$$\text{Radius } (r) = \sqrt{25 + 4 - 13}$$

$$= 4$$

Point of intersection of $2x + 3y = 12$ and $3x - 2y = 5$ is $(3, 2)$

\Rightarrow Centre of $C(O') = (3, 2)$

$$d = OO' = \sqrt{(5-3)^2 + (-2-2)^2} = \sqrt{20}$$

$$\text{Radius of } C = \sqrt{r^2 + d^2}$$

$$= \sqrt{16 + 20}$$

$$= 6$$

16. If the system of linear equations

$$x - 2y + z = -4$$

$$2x + \alpha y + 3z = 5$$

$$3x - y + \beta z = 3$$

has infinitely many solutions, then $12\alpha + 13\beta$ is equal to

(1) 64

(2) 58

(3) 60

(4) 54

Answer (2)

$$\text{Sol. } \Delta_2 = \begin{vmatrix} 1 & -4 & 1 \\ 2 & 5 & 3 \\ 3 & 3 & \beta \end{vmatrix} = 0$$

$$(5\beta - 9) + 4(2\beta - 9) - 9 = 0$$

$$\Rightarrow \beta = \frac{54}{13}$$

$$\Delta_3 = \begin{vmatrix} 1 & -2 & -4 \\ 2 & \alpha & 5 \\ 3 & -1 & 3 \end{vmatrix} = 0$$

$$\Rightarrow (3\alpha + 5) + 2(-9) - 4(-2 - 3\alpha) = 0$$

$$\Rightarrow \alpha = \frac{1}{3}$$

$$\Rightarrow 12\alpha + 13\beta = 4 + 54 = 58$$

17. The sum of the series

$$\frac{1}{1-3 \cdot 1^2 + 1^4} + \frac{2}{1-3 \cdot 2^2 + 2^4} + \frac{3}{1-3 \cdot 3^2 + 3^4} + \dots \text{ up to 10-terms is}$$

(1) $-\frac{55}{109}$

(2) $-\frac{45}{109}$

(3) $\frac{55}{109}$

(4) $\frac{45}{109}$

Answer (1)

$$\text{Sol. } T_r = \frac{1}{1-3 \cdot r^2 + r^4} = \frac{r}{(r^4 - 2r^2 + 1) - r^2}$$

$$= \frac{1}{2} \left[\frac{1}{r^2 - r - 1} - \frac{1}{r^2 + r - 1} \right]$$

Sum of 10 terms is

$$\sum_{r=1}^{10} T_r = \frac{1}{2} [-1 - 1] + \frac{1}{2} \left[1 - \frac{1}{5} \right] + \frac{1}{2} \left[\frac{1}{5} - \frac{1}{11} \right] + \dots$$

$$+ \frac{1}{2} \left[\frac{1}{89} - \frac{1}{109} \right]$$

$$= \frac{1}{2} \left[-1 - \frac{1}{109} \right] = -\frac{55}{109}$$

18. Two marbles are drawn in succession from a box containing 10 red, 30 white, 20 blue and 15 orange marbles, with replacement being made after each drawing. Then the probability, that first drawn marble is red and second drawn marble is white, is

(1) $\frac{4}{75}$

(2) $\frac{2}{3}$

(3) $\frac{2}{25}$

(4) $\frac{4}{25}$

Answer (1)

Sol. Total marbles = $10 + 30 + 20 + 15 = 75$

R : drawing a red marble in 1st



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W = drawing a white marble in 2nd

$$\Rightarrow P(R \cap W) = \left(\frac{10}{75}\right)\left(\frac{30}{75}\right) = \left(\frac{300}{75}\right) \times \frac{1}{75} = \frac{4}{75}$$

19. Let S be the set of positive integral values of a for which $\frac{ax^2 + 2(a+1)x + 9a + 4}{x^2 - 8x + 32} < 0, \forall x \in \mathbb{R}$. Then, the number of elements in S is :
- (1) 0 (2) ∞
(3) 3 (4) 1

Answer (1)

Sol. $x^2 - 8x + 32 > 0 \forall x \in \mathbb{R}$ as discriminant of this quadratic is $64 - 4 \times 32 < 0$

$$\Rightarrow ax^2 + 2(a+1)x + 9a + 4 < 0 \forall x \in \mathbb{R}$$

\Rightarrow Only possible when $a < 0$ and $D < 0$

\Rightarrow Since S is set of positive

values of $a \Rightarrow S$ is a null set

$$\Rightarrow n(S) = 0$$

20. Three rotten apples are accidentally mixed with fifteen good apples. Assuming the random variable x to be the number of rotten apples in a draw of two apples, the variance of x is

- (1) $\frac{57}{153}$ (2) $\frac{37}{153}$
(3) $\frac{47}{153}$ (4) $\frac{40}{153}$

Answer (4)

Sol.

X	0	1	2
$P(X)$	$\frac{35}{51}$	$\frac{15}{51}$	$\frac{1}{51}$

$$P(X=0) = \frac{{}^{15}C_2}{{}^{18}C_2} = \frac{35}{51}$$

$$P(X=1) = \frac{{}^{15}C_1 \times {}^3C_1}{{}^{18}C_2} = \frac{15}{51}$$

$$P(X=2) = \frac{{}^3C_2}{{}^{18}C_2} = \frac{1}{51}$$

$$\mu_x = \sum XP(X) = 0 \times \frac{35}{51} + \frac{1 \times 15}{51} + \frac{2 \times 1}{51} = \frac{17}{51}$$

$$\sigma_x^2 = \text{Variance} = \left(\sum X^2 P(X)\right) - \mu_x^2$$

$$= \left(0 \times \frac{35}{51} + \frac{1 \times 15}{51} + \frac{4 \times 1}{51}\right) - \left(\frac{17}{51}\right)^2$$

$$= \frac{19}{51} - \left(\frac{17}{51}\right)^2 = \frac{19}{51} - \frac{1}{9} = \frac{40}{153}$$

SECTION - B

Numerical Value Type Questions: This section contains 10 Numerical based questions. Attempt any 5 questions out of 10. The answer to each question should be rounded-off to the nearest integer.

21. Let $S = (-1, \infty)$ and $f : S \rightarrow \mathbb{R}$ be define as

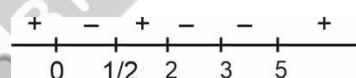
$$f(x) = \int_{-1}^x (e^t - 1)^{11} (2t - 1)^5 (t - 2)^7 (t - 3)^{12} (2t - 10)^{61} dt.$$

Let p = sum of squares of the values of x , where $f(x)$ attains local maxima on S , and q = sum of the values of x , where $f(x)$ attains local minima on S . Then, the value of $p^2 + 2q$ is _____

Answer (27)

Sol. $f'(x) = (e^x - 1)(2x - 1)^5 (x - 2)^7 (x - 3)^{12} (2x - 10)^{61} = 0$

Point of extremum = 0, $\frac{1}{2}$, 2, 3, 5



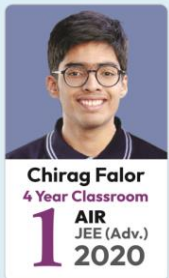
maxima = {0, 2}

minima = $\left\{\frac{1}{2}, 5\right\}$

$p = 0 + (2)^2 = 4$

$q = \frac{1}{2} + 5 = \frac{11}{2}$

$p^2 + 2q = 16 + \frac{11}{2} \times 2 = 27$



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22. If α denotes the number of solutions of

$$|1-i|^x = 2^x \text{ and } \beta = \left(\frac{|z|}{\arg(z)} \right), \text{ where}$$

$$z = \frac{\pi}{4}(1+i)^4 \left[\frac{1-\sqrt{\pi}i}{\sqrt{\pi}+i} + \frac{\sqrt{\pi}-i}{1+\sqrt{\pi}i} \right], i = \sqrt{-1}, \text{ then the}$$

distance of the point (α, β) from the line $4x - 3y = 7$ is _____

Answer (3)

Sol. $z = \frac{\pi}{4}(1+i)^4 \left[\frac{1+\pi+\pi+1}{i(1+\pi)-\sqrt{\pi}+\sqrt{\pi}} \right]$

$$= \frac{\pi}{4}(1+i)^4 \frac{2}{i} = \frac{\pi}{2} \frac{(1+i)^4}{i} = \frac{-\pi}{2} i(1+i)^4$$

$$|z| = \left| \frac{-\pi}{2} i \right| |1+i|^4 = 2\pi$$

$$z = \frac{-\pi}{2}(-4i) = 2\pi i \Rightarrow \arg(z) = \frac{\pi}{2}$$

$$\Rightarrow \beta = \frac{2\pi}{\frac{\pi}{2}} = 4$$

Also $|1-i|^x = 2^x$

$$(\sqrt{2})^x = 2^x$$

$$\Rightarrow x = 0$$

$$\Rightarrow 1 \text{ solution} \Rightarrow \alpha = 1$$

Now perpendicular distance of $4x - 3y = 7$ from $(1, 4)$

$$\left| \frac{4(1) - 3(4) - 7}{5} \right| = 3$$

23. The total number of words (with or without meaning) that can be formed out of the letters of the word 'DISTRIBUTION' taken four at a time, is equal

Answer (3734)

Sol. $I \rightarrow 3, T \rightarrow 2, D, S, R, B, U, O, N \rightarrow 1.$

$$\text{All distinct} = {}^9C_4 \times 4! = 3024$$

$$2 \text{ Alike} + 2 \text{ different} = {}^2C_1 \times {}^8C_2 \times \frac{4!}{2!} = 672$$

$$2 \text{ Alike} + 2 \text{ other Alike} = {}^2C_2 \times \frac{4!}{2!2!} = 6$$

$$3 \text{ Alike} + 1 \text{ different} = {}^1C_1 \times {}^8C_1 \times \frac{4!}{3!} = 32$$

$$\text{Total words} = 3734$$

24. Let the foci and length of the latus rectum of an ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1, a > b$ be $(\pm 5, 0)$ and $\sqrt{50}$, respectively. Then, the square of the eccentricity of the hyperbola $\frac{x^2}{b^2} - \frac{y^2}{a^2 b^2} = 1$ equals

Answer (51)

Sol. $ae = 5$

$$\frac{2b^2}{a} = \sqrt{50}$$

$$b^2 = \frac{5\sqrt{2}}{2}a$$

$$b^2 = a^2(1 - e^2)$$

$$\frac{5\sqrt{2}}{2} = a(1 - e^2)$$

$$\Rightarrow \frac{5}{e}(1 - e^2) = \frac{5}{\sqrt{2}}$$

$$\sqrt{2}(5 - 5e^2) = 5e$$

$$\Rightarrow 5\sqrt{2}e^2 + 5e - 5\sqrt{2} = 0$$

$$\sqrt{2}e^2 + e - \sqrt{2} = 0$$

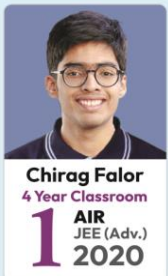
$$\Rightarrow e = -\sqrt{2} \text{ (rejected)}, e = \frac{1}{\sqrt{2}}$$

$$\text{from } ae = 5 \Rightarrow a = 5\sqrt{2} \text{ and } b^2 = 25$$

$$\text{Now eccentricity of } \frac{x^2}{b^2} - \frac{y^2}{a^2 b^2} = 1$$

$$e^2 = 1 + \frac{a^2 b^2}{b^2} = 1 + a^2 = 51$$

25. Let $A = \{1, 2, 3, 4\}$ and $R = \{(1, 2), (2, 3), (1, 4)\}$ be a relation on A . Let S be the equivalence relation on A such that $R \subset S$ and the number of elements in S is n . Then, the minimum value of n is _____



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Answer (16)

Sol. $A = \{1, 2, 3, 4\}$

$$R = \{(1, 2), (2, 3), (1, 4)\}$$

S is equivalence

for $R < S$ and reflexive

$$\{(1, 1), (2, 2), (3, 3), (4, 4)\}$$

for symmetric

$$\{(2, 1), (4, 1), (3, 2)\}$$

for transitive

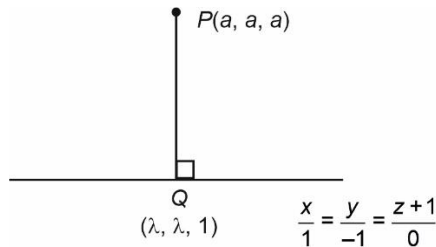
$$\{(1, 3), (3, 1), (4, 2), (2, 4)\}$$

Now set $S = \{(1, 1), (2, 2), (3, 3), (4, 4), (1, 2), (2, 3), (1, 4), (4, 3), (3, 4), (2, 1), (4, 1), (3, 2), (1, 3), (3, 1), (4, 2), (2, 4)\}$

$$n(S) = 16$$

26. Let Q and R be the feet of perpendiculars from the point $P(a, a, a)$ on the lines $x = y, z = 1$ and $x = -y, z = -1$ respectively. If $\angle QPR$ is a right angle, then $12a^2$ is equal to _____

Answer (12)

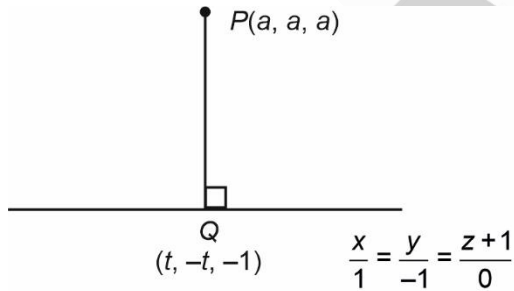


Sol.

$$\overrightarrow{PQ} \cdot (\hat{i} + \hat{j}) = 0$$

$$\Rightarrow (\lambda - a) + (\lambda - a) = 0$$

$$\Rightarrow \lambda = a \Rightarrow Q(a, a, 1)$$



$$\overrightarrow{PR} \cdot (\hat{i} - \hat{j}) = 0$$

$$\Rightarrow (t - a) - (-t - a) = 0 \Rightarrow t = 0$$

$$\Rightarrow R(0, 0, -1)$$

$$\therefore \overrightarrow{PQ} \cdot \overrightarrow{PR} = 0$$

$$((1-a)\hat{k}) \cdot (-a\hat{i} - a\hat{j} - (a+1)\hat{k}) = 0$$

$$\Rightarrow a^2 = 1$$

$$12a^2 = 12$$

27. In the expansion of $(1+x)(1-x^2)$

$\left(1 + \frac{3}{x} + \frac{3}{x^2} + \frac{1}{x^3}\right)^5$, $x \neq 0$, the sum of the coefficients of x^3 and x^{-13} is equal to _____

Answer (118)

$$\text{Sol. } E(x) = \frac{1}{x^{15}}(1+x)(1-x^2)(1+3x+3x^2+x^3)^5$$

$$= \frac{1}{x^{15}}(1+x)(1-x)(1+x)(1+x)^{15}$$

$$= \frac{1}{x^{15}}(1-x)(1+x)^{17}$$

$$= \frac{(1+x)^{17}}{x^{15}} - \frac{(1+x)^{17}}{x^{14}}$$

$$\Rightarrow \text{Coefficient of } x^3 \text{ in } E(x) = 0 - 1 = -1$$

$$\text{Coefficient of } x^{-13} \text{ in } E(x) = {}^{17}C_2 - {}^{17}C_1$$

$$= 136 - 17 = 119$$

$$\Rightarrow \text{Sum} = 118$$

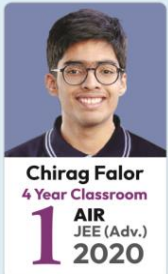
28. If the integral $525 \int_0^{\frac{\pi}{2}} \sin 2x \cos^{\frac{11}{2}} x \left(1 + \cos^{\frac{5}{2}} x\right)^{\frac{1}{2}} dx$ is equal to $(n\sqrt{2} - 64)$, then n is equal to _____

Answer (176)

$$\text{Sol. } I = 525 \int_0^{\frac{\pi}{2}} \sin 2x \cos^{\frac{11}{2}} x \left(1 + \cos^{\frac{5}{2}} x\right)^{\frac{1}{2}} dx$$

$$= 525 \int_0^{\frac{\pi}{2}} 2 \sin x \cos x \cos^{\frac{11}{2}} x \left(1 + \cos^{\frac{5}{2}} x\right)^{\frac{1}{2}} dx$$

$$= 1050 \int_0^{\frac{\pi}{2}} \sin x \cos^{\frac{13}{2}} x \left(1 + \cos^{\frac{5}{2}} x\right)^{\frac{1}{2}} dx$$



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$$\text{Put } \left(1 + \cos^{\frac{5}{2}} x\right) = t$$

$$\Rightarrow \frac{5}{2} \cos^{\frac{3}{2}} x (-\sin x) dx = dt$$

$$I = 1050 \int_2^1 -\frac{2}{5} \cos^5 x \cdot \sqrt{t} dt$$

$$= -420 \int_2^1 (t-1)^2 \sqrt{t} dt$$

$$= 420 \int_1^2 \left(t^{\frac{5}{2}} - 2t^{\frac{3}{2}} + t^{\frac{1}{2}} \right) dt$$

$$= 420 \left[\frac{2}{7} t^{\frac{7}{2}} - 2 \times \frac{2}{5} t^{\frac{5}{2}} + \frac{2}{3} t^{\frac{3}{2}} \right]_1^2$$

$$= 420 \left(\sqrt{2} \left(\frac{16}{7} - \frac{16}{5} + \frac{4}{3} \right) - \left(\frac{2}{7} - \frac{4}{5} + \frac{2}{3} \right) \right)$$

$$= 176\sqrt{2} - 64$$

$$\Rightarrow n = 176$$

29. Let $f: \mathbb{R} \rightarrow \mathbb{R}$ be a function defined by $f(x) = \frac{4x}{4^x + 2}$ and

$$M = \int_{f(a)}^{f(1-a)} x \sin^4(x(1-x)) dx,$$

$$N = \int_{f(a)}^{f(1-a)} \sin^4(x(1-x)) dx; a \neq \frac{1}{2}. \text{ If } \alpha M = \beta N,$$

$\alpha, \beta, \in \mathbb{N}$, then the least value of $\alpha^2 + \beta^2$ is equal to _____

Answer (5)

$$\text{Sol. } f(x) + f(1-x) = \frac{4^x}{4^x + 2} + \frac{4^{1-x}}{4^{1-x} + 2}$$

$$= \frac{4^x}{4^x + 2} + \frac{4}{4 + 2 \cdot 4^x}$$

$$= \frac{4^x + 2}{4^x + 2} = 1$$

$$\Rightarrow M = \int_{f(a)}^{f(1-a)} x \sin^4(x(1-x)) dx$$

$$x \rightarrow f(a) + f(1-a) - x = 1 - x$$

$$M = \int_{f(a)}^{f(1-a)} (1-x) \sin^4((1-x)x) dx$$

$$M = N - M \Rightarrow \frac{M}{N} = \frac{1}{2} = \frac{\beta}{\alpha}$$

$$\Rightarrow (\alpha^2 + \beta^2)_{\text{least}} = 1 + 4 = 5$$

30. Let \vec{a} and \vec{b} be two vectors such that $|\vec{a}| = 1$,

$|\vec{b}| = 4$, and $\vec{a} \cdot \vec{b} = 2$. If $\vec{c} = (2\vec{a} \times \vec{b}) - 3\vec{b}$ and the angle between \vec{b} and \vec{c} is α , then $192 \sin^2 \alpha$ is equal to

Answer (48)

$$\text{Sol. } \vec{c} = (2\vec{a} \times \vec{b}) - 3\vec{b}$$

$$|\vec{c}|^2 = |(2\vec{a} \times \vec{b}) - 3\vec{b}|^2$$

$$= (2|\vec{a} \times \vec{b}|)^2 + 9|\vec{b}|^2 - 12(\vec{a} \times \vec{b}) \cdot \vec{b}$$

$$= 4(|\vec{a}|^2 |\vec{b}|^2 - (\vec{a} \cdot \vec{b})^2) + 9|\vec{b}|^2$$

$$= 4(16 - 4) + 144 = 192$$

$$\vec{b} \cdot \vec{c} = -3\vec{b} \cdot \vec{b} = -48$$

$$|\vec{b}| \cdot |\vec{c}| \cos \alpha = -48$$

$$\cos \alpha = \frac{-48}{4 \times \sqrt{192}} = -\frac{12}{\sqrt{192}}$$

$$\sin^2 \alpha = 1 - \frac{144}{192} \Rightarrow 192 \sin^2 \alpha = 48$$



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PHYSICS

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer :

31. Four identical particles of mass m are kept at the four corners of a square. If the gravitational force exerted on one of the masses by the other masses is $\left(\frac{2\sqrt{2}+1}{32}\right)\frac{Gm^2}{L^2}$, the length of the sides of the square is
- (1) $2L$ (2) $3L$
(3) $4L$ (4) $\frac{L}{2}$

Answer (3)

Sol. Let a side length

$$\text{Force on a mass} = \frac{Gm^2}{a^2} \left(\sqrt{2} + \frac{1}{2} \right)$$

$$\therefore \left(\frac{2\sqrt{2}+1}{32} \right) \frac{Gm^2}{L^2} = \frac{Gm^2}{a^2} \left(\sqrt{2} + \frac{1}{2} \right)$$

$$\Rightarrow \boxed{a = 4L}$$

32. Two charges q and $3q$ are separated by a distance 'r' in air. At a distance x from charge q , the resultant electric field is zero. The value of x is :

- (1) $\frac{r}{3(1+\sqrt{3})}$ (2) $\frac{(1+\sqrt{3})}{r}$
(3) $\frac{r}{(1+\sqrt{3})}$ (4) $r(1+\sqrt{3})$

Answer (3)

$$\text{Sol. } \frac{kq}{x^2} = k \frac{(3q)}{(r-x)^2}$$

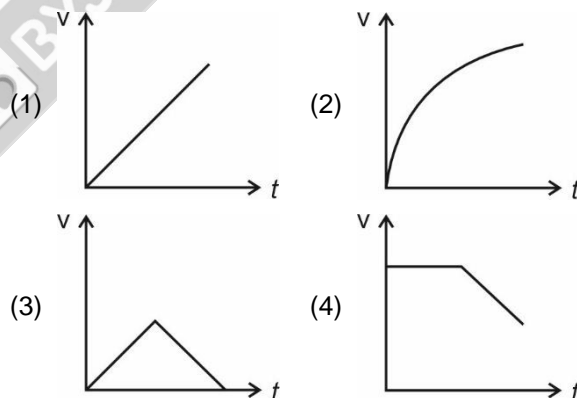
$$\Rightarrow x = \frac{r}{(\sqrt{3}+1)}$$

33. In a plane EM wave, the electric field oscillates sinusoidally at a frequency of 5×10^{10} Hz and an amplitude of 50 Vm^{-1} . The total average energy density of the electromagnetic field of the wave is : [Use $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2 / \text{Nm}^2$]
- (1) $4.425 \times 10^{-8} \text{ Jm}^{-3}$ (2) $2.212 \times 10^{-8} \text{ Jm}^{-3}$
(3) $1.106 \times 10^{-8} \text{ Jm}^{-3}$ (4) $2.212 \times 10^{-10} \text{ Jm}^{-3}$

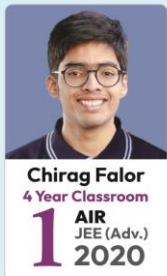
Answer (3)

$$\begin{aligned} \text{Sol. } u &= \frac{1}{2} \epsilon_0 E^2 \\ &= \frac{1}{2} \times (8.85 \times 10^{-12}) \times (50)^2 \\ &= 1.106 \times 10^{-8} \text{ Jm}^{-3} \end{aligned}$$

34. A small steel ball is dropped into a long cylinder containing glycerine. Which one of the following is the correct representation of the velocity time graph for the transit of the ball?



Answer (2)



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Sol. $a = \left(\frac{mg - v\rho g}{m} \right) - \left(\frac{6\pi nr}{m} \right) v$

$$a = C_1 - C_2 v$$

$$\therefore \int_0^v \frac{dv}{C_1 - C_2 v} = \int_0^t dt$$

$$\Rightarrow v = \frac{C_1}{C_2} (1 - e^{-C_2 t})$$

\therefore Exponentially growing graph is possible

35. When a metal surface is illuminated by light of wavelength λ , the stopping potential is 8V. When the same surface is illuminated by light of wavelength 3λ , stopping potential is 2V. The threshold wavelength for this surface is:

- (1) 3λ (2) 4.5λ
 (3) 9λ (4) 5λ

Answer (3)

Sol. $8 \text{ eV} = \frac{hc}{\lambda} - \phi_0 \quad \dots(i)$

$2 \text{ eV} = \frac{hc}{3\lambda} - \phi_0 \quad \dots(ii)$

From (i) & (ii)

$$\phi = \frac{1}{9} \frac{hc}{\lambda}$$

$$\therefore \lambda_0 = 9\lambda$$

36. The relation between time ' t ' and distance ' x ' is $t = \alpha x^2 + \beta x$, where α and β are constants. The relation between acceleration (a) and velocity (v) is:

- (1) $a = -3\alpha v^2$ (2) $a = -5\alpha v^5$
 (3) $a = -2\alpha v^3$ (4) $a = -4\alpha v^4$

Answer (3)

Sol. $\frac{1}{v} = \frac{dt}{dx} = 2\alpha x + \beta$

Now, $-\frac{1}{v^2} \frac{dv}{dt} = 2\alpha \frac{dx}{dt}$

$$\Rightarrow -\frac{1}{v^2} a = 2\alpha v$$

$$\Rightarrow a = -2\alpha v^3$$

37. A force is represented by $F = ax^2 + bt^{\frac{1}{2}}$

Where x = distance and t = time. The dimensions of b^2/a are:

- (1) $[ML^3T^{-3}]$ (2) $[ML^2T^{-3}]$
 (3) $[ML^{-1}T^{-1}]$ (4) $[MLT^{-2}]$

Answer (1)

Sol. $[a] = \left[\frac{F}{x^2} \right], [b] = \left[\frac{F}{\sqrt{t}} \right]$

$$\therefore \left[\frac{b^2}{a} \right] = \left[\frac{Fx^2}{t} \right] = [ML^2T^{-3}]$$

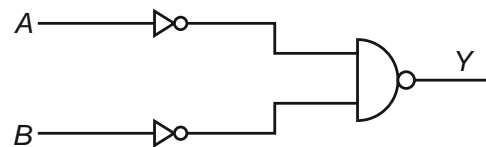
38. The parameter that remains the same for molecules of all gases at a given temperature is:

- (1) momentum (2) speed
 (3) kinetic energy (4) mass

Answer (3)

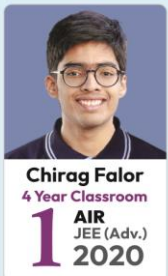
Sol. K.E. is independent of the mass of the molecules.

39. Identify the logic operation performed by the given circuit.



- (1) NOR (2) OR
 (3) AND (4) NAND

Answer (2)



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Sol. Truth table is

A	B	Y
0	0	0
1	1	1
0	1	1
1	0	1

∴ OR gate

40. The refractive index of a prism with apex angle A is $\cot \frac{A}{2}$. The angle of minimum deviation is :

- (1) $\delta_m = 180^\circ - A$ (2) $\delta_m = 180^\circ - 2A$
(3) $\delta_m = 180^\circ - 4A$ (4) $\delta_m = 180^\circ - 3A$

Answer (2)

Sol. ∴ $\mu = \frac{\sin\left(\frac{A + \delta_m}{2}\right)}{\sin\left(\frac{A}{2}\right)}$

and $\mu = \cot\left(\frac{A}{2}\right)$

∴ $\delta_m = 180 - 2A$

41. The fundamental frequency of a closed organ pipe is equal to the first overtone frequency of an open organ pipe. If length of the open pipe is 60 cm, the length of the closed pipe will be:

- (1) 30 cm (2) 45 cm
(3) 15 cm (4) 60 cm

Answer (3)

Sol. $\frac{v}{4l_c} = 2\left(\frac{v}{2l_o}\right)$ and $l_o = 60$ cm

$l_c = 15$ cm

42. A coin is placed on a disc. The coefficient of friction between the coin and the disc is μ . If the distance of the coin from the centre of the disc is r , the maximum angular velocity which can be given to the disc, so that the coin does not slip away, is:

- (1) $\sqrt{\frac{\mu g}{r}}$ (2) $\frac{\mu}{\sqrt{rg}}$
(3) $\frac{\mu g}{r}$ (4) $\sqrt{\frac{r}{\mu g}}$

Answer (1)

Sol. $F_{\text{centripetal}} \leq f_{\text{max}}$

$m\omega^2 r \leq \mu mg$

$\omega \leq \sqrt{\frac{\mu g}{r}}$

43. An artillery piece of mass M_1 fires a shell of mass M_2 horizontally. Instantaneously after the firing, the ratio of kinetic energy of the artillery and that of the shell is:

- (1) $\frac{M_2}{M_1}$
(2) $\frac{M_2}{(M_1 + M_2)}$
(3) $\frac{M_1}{M_2}$
(4) $\frac{M_1}{(M_1 + M_2)}$

Answer (1)

Sol. ∴ $p_1 = p_2$ and $K \cdot E = \frac{p^2}{2M}$

∴ $\frac{K \cdot E_1}{K \cdot E_2} = \frac{M_2}{M_1}$



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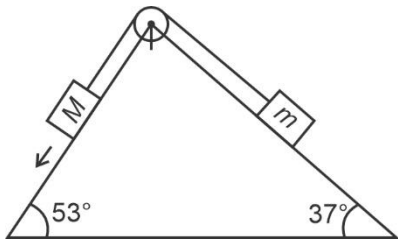


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44. In the given arrangement of a doubly inclined plane two blocks M and m are placed. The blocks are connected by a light string passing over an ideal pulley as shown. The coefficient of friction between the surface of the plane and the blocks is 0.25. The value of m , for which $M = 10$ kg will move down with an acceleration of 2 m/s^2 , is: (take $g = 10 \text{ m/s}^2$ and $\tan 37^\circ = \frac{3}{4}$)



- (1) 6.5 kg (2) 9 kg
(3) 4.5 kg (4) 2.25 kg

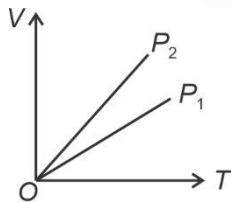
Answer (3)

Sol. $a = \frac{\text{Net pulling force}}{\text{Total mass}}$

$$2 = \frac{Mg \sin 53^\circ - mg \sin 37^\circ - \mu mg \cos 53^\circ - \mu mg \cos 37^\circ}{M + m}$$

$$\therefore m = 4.5 \text{ kg}$$

45. The given figure represents two isobaric processes for the same mass of an ideal gas, then



- (1) $P_1 > P_2$ (2) $P_1 = P_2$
(3) $P_2 \geq P_1$ (4) $P_2 > P_1$

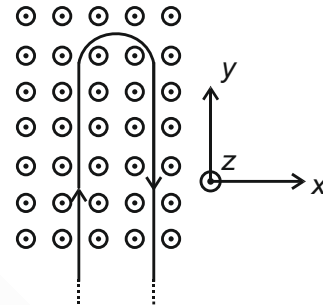
Answer (1)

Sol. at same temperature

$$V_2 > V_1$$

$$\therefore P_2 < P_1$$

46. A rigid wire consists of a semicircular portion of radius R and two straight sections. The wire is partially immersed in a perpendicular magnetic field $B = B_0 \hat{j}$ as shown in figure. The magnetic force on the wire if it has a current i is:



- (1) $2iBR\hat{j}$ (2) $-2iBR\hat{j}$
(3) $iBR\hat{j}$ (4) $-iBR\hat{j}$

Answer (2)

Sol. $F = i \left(\int d\vec{l} \times \vec{B} \right)$

$$\therefore \vec{F} = i(2R)B_0(-\hat{j})$$

47. A coil is placed perpendicular to a magnetic field of 5000 T. When the field is changed to 3000 T in 2 s, an induced emf of 22 V is produced in the coil. If the diameter of the coil is 0.02 m, then the number of turns in the coil is

- (1) 35 (2) 70
(3) 7 (4) 140

Answer (2)

Sol. $\varepsilon = \frac{\Delta\phi}{\Delta t} = \frac{N\Delta(BA)}{\Delta t}$

$$22 = \frac{N(2000) \left(\frac{22}{7} \cdot \frac{0.02^2}{4} \right)}{2}$$

$$\Rightarrow N = 70$$



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48. If the wavelength of the first member of Lyman series of hydrogen is λ . The wavelength of the second member will be

- (1) $\frac{5}{27}\lambda$ (2) $\frac{27}{5}\lambda$
(3) $\frac{32}{27}\lambda$ (4) $\frac{27}{32}\lambda$

Answer (4)

Sol. $\frac{1}{\lambda} = R \left(\frac{1}{1^2} - \frac{1}{2^2} \right) \dots (i)$

Also $\frac{1}{\lambda'} = R \left(\frac{1}{1^2} - \frac{1}{3^2} \right) \dots (ii)$

from (i) and (ii)

$$\lambda' = \frac{27}{32}\lambda$$

49. Two conductors have the same resistances at 0°C but their temperature coefficients of resistance are α_1 and α_2 . The respective temperature coefficients for their series and parallel combinations are:

- (1) $\alpha_1 + \alpha_2, \frac{\alpha_1 + \alpha_2}{2}$ (2) $\frac{\alpha_1 + \alpha_2}{2}, \alpha_1 + \alpha_2$
(3) $\frac{\alpha_1 + \alpha_2}{2}, \frac{\alpha_1 + \alpha_2}{2}$ (4) $\alpha_1 + \alpha_2, \frac{\alpha_1 \alpha_2}{\alpha_1 + \alpha_2}$

Answer (3)

Sol. For series

$$R_{\text{series}} = 2R_0 \left[1 + \left(\frac{\alpha_1 + \alpha_2}{2} \right) \Delta t \right]$$

$$\therefore \alpha_{\text{series}} = \frac{\alpha_1 + \alpha_2}{2}$$

For parallel

$$\frac{dR}{R_p^2} = \frac{-dR}{R_1^2} - \frac{dR_2}{R_2^2}$$

$$\frac{\alpha_p R_p dT}{R_p^2} = \frac{\alpha_1 R_0 dT}{R_0^2} + \frac{\alpha_2 R_0 dT}{R_0^2}$$

$$\Rightarrow \alpha_p = \frac{\alpha_1 + \alpha_2}{2}$$

50. If the percentage errors in measuring the length and the diameter of a wire are 0.1% each. The percentage error in measuring its resistance will be:

- (1) 0.2% (2) 0.144%
(3) 0.3% (4) 0.1%

Answer (3)

Sol. $\frac{\Delta R}{R} = \frac{\Delta l}{l} + \frac{2\Delta D}{D} \quad \left(\because R = \frac{4\rho l}{\pi D^2} \right)$

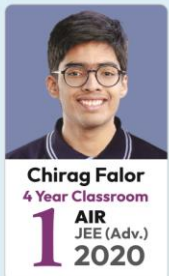
$$\Rightarrow \frac{\Delta R}{R} \times 100 = 0.1 + 2(0.1) = 0.3\%$$

SECTION - B

Numerical Value Type Questions: This section contains 10 Numerical based questions. Attempt any 5 questions out of 10. The answer to each question should be rounded-off to the nearest integer.

51. An electron moves through a uniform magnetic field $\vec{B} = B_0 \hat{i} + 2B_0 \hat{j} T$. At a particular instant of time, the velocity of electron is $\vec{v} = 3\hat{i} + 5\hat{j} \text{ m/s}$. If the magnetic force acting on electron is $\vec{F} = 5e\hat{k} \text{ N}$, where e is the charge of electron then the value of B_0 is _____ T.

Answer (5)



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Sol. $\therefore \vec{F} = e(\vec{v} \times \vec{B})$

$$= e(3\hat{i} + 5\hat{j}) \times (B_0\hat{i} + 3B_0\hat{j})$$

$$= eB_0\hat{k}$$

$$\therefore B_0 = 5 \text{ T}$$

52. The mass defect in a particular reaction is 0.4 g. The amount of energy liberated is $n \times 10^7$ kWh. Where $n =$ _____.

(Speed of light = 3×10^8 m/s)

Answer (1)

Sol. $\Delta E = \Delta mc^2$

$$n \times 10^7 \times 3.6 \times 10^6 = 0.4 \times 10^{-3} \times 9 \times 10^{16}$$

$$\Rightarrow n = 1$$

53. The depth below the surface of sea to which a rubber ball be taken so as to decrease its volume by 0.02% is _____ m.

(Take density of sea water = 10^3 kgm^{-3} , Bulk modulus of rubber = $9 \times 10^8 \text{ Nm}^{-2}$, and $g = 10 \text{ ms}^{-2}$)

Answer (18)

Sol. $\therefore B = \left| \frac{\Delta P}{\Delta V/V} \right|$

$$\therefore \Delta P = \rho gh = \frac{B \Delta V}{V}$$

$$h = \frac{B}{\rho g} \left(\frac{\Delta V}{V} \right)$$

$$= \frac{9 \times 10^8}{10^3 \times 10} (0.02 \times 10^{-2})$$

$$= 18 \text{ m}$$

54. A body starts falling freely from height H hits an inclined plane in its path at height h . As a result of this perfectly elastic impact, the direction of the velocity of the body becomes horizontal. The value of $\frac{H}{h}$ for which the body will take the maximum time to reach the ground is _____.

Answer (2)

Sol. $\sqrt{\frac{2(H-h)}{g}} + \sqrt{\frac{2h}{g}} = T$

for $T \rightarrow$ maximum

$$\frac{dT}{dh} = 0$$

$$\Rightarrow \frac{1}{2\sqrt{H-h}}(-1) + \frac{1}{2\sqrt{h}}(1) = 0$$

$$\Rightarrow h = \frac{H}{2}$$

$$\Rightarrow \frac{H}{h} = 2$$

55. A particle performs simple harmonic motion with amplitude A . Its speed is increased to three times at an instant when its displacement is $\frac{2A}{3}$. The new amplitude of motion is $\frac{nA}{3}$. The value of n is _____.

Answer (7)

Sol. $3\omega\sqrt{A^2 - \left(\frac{2A}{3}\right)^2} = \omega\sqrt{(A')^2 - \left(\frac{2A}{3}\right)^2}$

$$\Rightarrow A' = \frac{7}{3}A$$



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56. A small square loop of wire of side l is placed inside a large square loop of wire of side L ($L = \ell$). The loops are coplanar and their centres coincide. The value of the mutual inductance of the system is $\sqrt{x} \times 10^{-7} \text{ H}$, where $x = \underline{\hspace{2cm}}$.

Answer (128)

Sol. $M = \frac{\phi}{i}$

$$= \frac{4 \left[\frac{\mu_0 i}{4\pi(L/2)} \sqrt{2} \right] \ell^2}{i}$$

$$= 8\sqrt{2} \times 10^{-7} \text{ H}$$

$$= \sqrt{128} \times 10^{-7} \text{ H}$$

57. A solid circular disc of mass 50 kg rolls along a horizontal floor so that its center of mass has speed of 0.4 m/s. The absolute value of work done on the disc to stop it is $\underline{\hspace{2cm}}$ J.

Answer (6)

Sol. $W = \frac{1}{2} \left(\frac{mR^2}{2} \right) \left(\frac{v^2}{R^2} \right) + \frac{1}{2} mv^2$

$$= \frac{3}{4} mv^2$$

$$= \frac{3}{4} (50)(0.4)^2 = 6 \text{ J}$$

58. A parallel plate capacitor with plate separation 5 mm is charged up by a battery. It is found that on introducing a dielectric sheet of thickness 2 mm, while keeping the battery connections intact, the capacitor draws 25% more charge from the battery than before. The dielectric constant of the sheet is $\underline{\hspace{2cm}}$.

Answer (2)

Sol. Let $C = \frac{\epsilon_0 A}{(5 \text{ mm})}$

$$\Rightarrow C' = \frac{\epsilon_0 A}{3 + \frac{2}{k}}$$

Now

$$C'V = \frac{5}{4}(CV)$$

$$\Rightarrow \frac{\epsilon_0 A}{3 + \frac{2}{k}} = \frac{\epsilon_0 A}{5} \left(\frac{5}{4} \right)$$

$$\Rightarrow k = 2$$

59. Two waves of intensity ratio 1 : 9 cross each other at a point. The resultant intensities at that point, when (a) Waves are incoherent is I_1 (b) Waves are coherent is I_2 and differ in phase by 60° . If $\frac{I_1}{I_2} = \frac{10}{x}$ then $x = \underline{\hspace{2cm}}$.

Answer (13)

Sol. $I_1 = 10C$

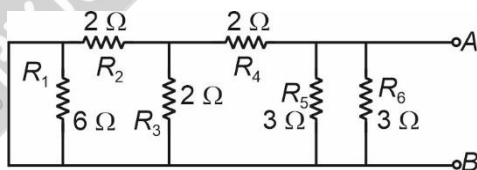
$$I_2 = C + 9C + 6C \cos 60^\circ$$

$$= 13C$$

$$\therefore \frac{I_1}{I_2} = \frac{10}{13}$$

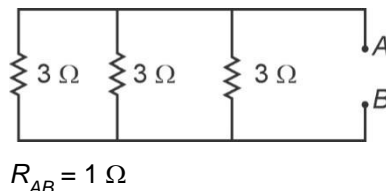
$$\Rightarrow x = 13$$

60. Equivalent resistance of the following network is $\underline{\hspace{2cm}} \Omega$.



Answer (1)

Sol. Effective circuit will look like



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CHEMISTRY

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer :

61. 'Adsorption' principle is used for which of the following purification method?

- (1) Sublimation (2) Chromatography
(3) Extraction (4) Distillation

Answer (2)

Sol. Adsorption chromatography is based upon the differential adsorption of the various components of a mixture on a suitable adsorbent such as silica gel or alumina.

62. The correct sequence of electron gain enthalpy of the elements listed below is

- A. Ar B. Br
C. F D. S

Choose the **most appropriate** from the options given below

- (1) $A > D > C > B$ (2) $C > B > D > A$
(3) $A > D > B > C$ (4) $D > C > B > A$

Answer (3)

Sol. Electron gain enthalpy of

$$D \Rightarrow S = -200 \text{ kJ mol}^{-1}$$

$$C \Rightarrow F = -333 \text{ kJ mol}^{-1}$$

$$B \Rightarrow Br = -325 \text{ kJ mol}^{-1}$$

$$A \Rightarrow Ar = 96 \text{ kJ mol}^{-1}$$

$A > D > B > C$ (source NCERT)

63. The compound that is white in colour is

- (1) ammonium arsinomolybdate
(2) lead sulphate
(3) ammonium sulphide
(4) lead iodide

Answer (2)

Sol. Lead sulphate is a white solid, which appears white in microcrystalline form.

64. The linear combination of atomic orbitals to form molecular orbitals takes place only when the combining atomic orbitals

- A. have the same energy
B. have the minimum overlap
C. have same symmetry about the molecular axis
D. have different symmetry about the molecular axis

Choose the **most appropriate** from the options given below.

- (1) B, C, D only (2) B and D only
(3) A, B, C only (4) A and C only

Answer (4)

Sol. Linear combination of atomic orbitals to form molecular orbitals takes place when

- They have same energy
- Maximum overlap
- Have same symmetry about the molecular axis


Hence, only A and C are correct.

65. Consider the oxides of group 14 elements

SiO_2 , GeO_2 , SnO_2 , PbO_2 , CO and GeO. The amphoteric oxides are

- (1) SnO_2 , CO (2) SiO_2 , GeO_2
(3) GeO, GeO_2 (4) SnO_2 , PbO_2

Answer (4)



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Sol. SnO_2 and $\text{PbO}_2 \rightarrow$ Amphoteric oxides

$\text{CO} \rightarrow$ Neutral oxide

GeO , SiO_2 , $\text{GeO}_2 \rightarrow$ Acidic oxides

66. The metals that are employed in the battery industries are

- A. Fe
- B. Mn
- C. Ni
- D. Cr
- E. Cd

Choose the correct answer from the options given below:

- (1) A, B, C and D only (2) A, B, C, D and E
(3) B, C and E only (4) B, D and E only

Answer (3)

Sol. Mn, Ni and Cd are metals that are employed in the battery industries.

Commercial dry cell has \rightarrow Zinc anode and MnO_2 + carbon black + NH_4Cl paste cathode.

Ni – Cd cell is a rechargeable cell.

$\text{Cd(s)} + \text{Ni(OH)}_3\text{(s)} \rightarrow \text{CdO(s)} + 2\text{Ni(OH)}_2\text{(s)} + \text{H}_2\text{O(l)}$

67. Match List I with List II

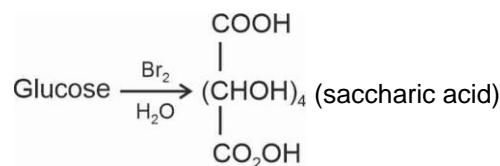
LIST I		LIST II	
A.	Glucose/ NaHCO_3/Δ	I.	Gluconic acid
B.	Glucose/ HNO_3	II.	No reaction
C.	Glucose/ HI/Δ	III.	n-hexane
D.	Glucose/Bromine water	IV.	Saccharic acid

Choose the correct answer from the options given below:

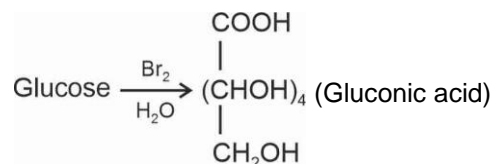
- (1) A-I, B-IV, C-III, D-II (2) A-III, B-II, C-I, D-IV
(3) A-IV, B-I, C-III, D-II (4) A-II, B-IV, C-III, D-I

Answer (4)

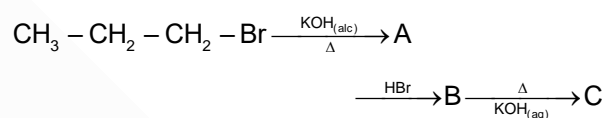
Sol. Glucose $\xrightarrow[\Delta]{\text{NaHCO}_3}$ No reaction



Glucose $\xrightarrow[\Delta]{\text{HI}} \text{n-Hexane}$



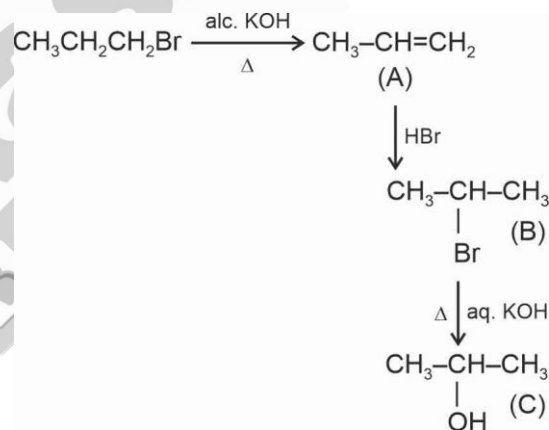
68. The product (C) in the below mentioned reaction is:



- (1) Propene (2) Propan-2-ol
(3) Propan-1-ol (4) Propyne

Answer (2)

Sol. Propan-2-ol



69. Identify correct statements from below:

- A. The chromate ion is square planar.
B. Dichromates are generally prepared from chromates.
C. The green manganate ion is diamagnetic.



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D. Dark green coloured K_2MnO_4 disproportionates in a neutral or acidic medium to give permanganate.

E. With increasing oxidation number of transition metal, ionic character of the oxides decreases.

Choose the correct answer from the options given below:

- (1) B, D, E only (2) A, D, E only
 (3) B, C, D only (4) A, B, C only

Answer (1)

Sol. (A) Chromate ions are tetrahedral and not square planar.

(B) $FeCr_2O_4 + Na_2CO_3 + O_2 \rightarrow Na_2CrO_4 + Fe_2O_3 + CO_2$

$Na_2CrO_4 + H^+ \rightarrow Na_2Cr_2O_7 + Na^+$

(C) Manganate $\rightarrow MnO_4^{2-} \rightarrow 1$ unpaired e^- in $Mn^{+6} \rightarrow$ Paramagnetic

(D) $K_2MnO_4 \xrightarrow{H^+} KMnO_4 + MnO_2 + H_2O$
 (Disproportionation)

(E) $Mn_2O_7 \rightarrow$ Covalent; CrO_3 , V_2O_5 has low melting point. Oxidation state increases then ionic character decreases.

70. The correct statements from following are:

- A. The strength of anionic ligands can be explained by crystal field theory.
 B. Valence bond theory does not give a quantitative interpretation of kinetic stability of coordination compounds.
 C. The hybridisation involved in formation of $[Ni(CN)_4]^{2-}$ complex is dsp^2
 D. The number of possible isomer(s) of $cis-[PtCl_2(en)_2]^{2+}$ is one

Choose the correct answer from the options given below :

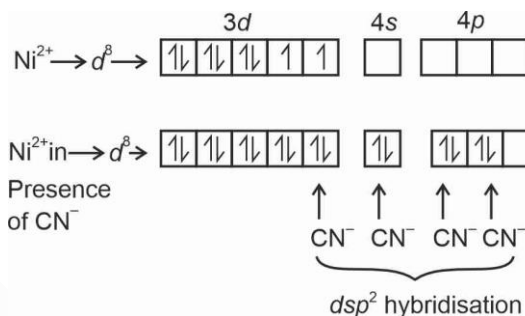
- (1) A, C only (2) A, D only
 (3) B, D only (4) B, C only

Answer (4)

Sol. (A) Strength of anionic ligands cannot be explained by CFT instead LFT i.e., ligand field theory explains the strength of ligands.

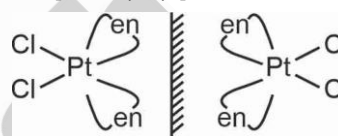
(B) VBT does not give a quantitative interpretation of kinetic stability of coordination compounds.

(C) $[Ni(CN)_4]^{2-} \rightarrow Ni^{2+}$ in presence of CN^- ligand.

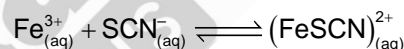


Square planar geometry since $\rightarrow 4dsp^2$ hybridised orbitals created.

(D) $cis-[PtCl_2(en)_2] \Rightarrow$ It has two possible isomers



71. For the given reaction, choose the correct expression of K_c from the following.




(1) $K_c = \frac{[Fe^{3+}][SCN^-]}{[FeSCN^{2+}]}$

(2) $K_c = \frac{[FeSCN^{2+}]^2}{[Fe^{3+}][SCN^-]}$

(3) $K_c = \frac{[FeSCN^{2+}]}{[Fe^{3+}]^2[SCN^-]^2}$

(4) $K_c = \frac{[FeSCN^{2+}]}{[Fe^{3+}][SCN^-]}$

Answer (4)



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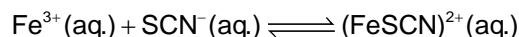
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Sol. Given reaction :



$$K_c = \frac{[\text{Product ions}]}{[\text{Reactant ions}]} = \frac{[\text{FeSCN}^{2+}]}{[\text{Fe}^{3+}][\text{SCN}^{-}]}$$

Correct answer is (4)

72. Integrated rate law equation for a first order gas phase reaction is given by

(where P_i is initial pressure and P_t is total pressure at time t)

$$(1) \quad k = \frac{2.303}{t} \times \log \frac{2P_i}{(2P_i - P_t)}$$

$$(2) \quad k = \frac{2.303}{t} \times \log \frac{P_i}{(2P_i - P_t)}$$

$$(3) \quad k = \frac{2.303}{t} \times \frac{P_i}{(2P_i - P_t)}$$

$$(4) \quad k = \frac{2.303}{t} \times \log \frac{(2P_i - P_t)}{P_i}$$

Answer (2)



Initial: P_i

Pressure at time t : $P_i - x$ $2x$

$$P_t = P_i - x + 2x$$

$$P_t = P_i + x$$

$$x = P_t - P_i$$

$$k = \frac{2.303}{t} \log \frac{\text{Initial pressure of A}}{\text{Pressure of A at time } t}$$

$$k = \frac{2.303}{t} \log \frac{P_i}{P_i - x} \Rightarrow \frac{2.303}{t} \log \frac{P_i}{P_i - P_t + P_t}$$

$$k = \frac{2.303}{t} \log \frac{P_i}{2P_i - P_t}$$

73. Match List I with List II

LIST I (Technique)		LIST II (Application)	
A.	Distillation	I.	Separation of glycerol from spent-lye
B.	Fractional distillation	II.	Aniline-Water mixture
C.	Steam distillation	III.	Separation of crude oil fractions
D.	Distillation under reduced pressure	IV.	Chloroform-Aniline

Choose the correct answer from the options given below.

(1) A-IV, B-III, C-II, D-I (2) A-IV, B-I, C-II, D-III

(3) A-I, B-II, C-IV, D-III (4) A-II, B-III, C-I, D-IV

Answer (1)

Sol. A-IV: Chloroform and aniline can be separated by distillation.

B-III: Separation of crude oil fractions in petroleum industry is done by fractional distillation.

C-II: Aniline water mixture can be separated by steam distillation due to difference in boiling point.

D-I: Separation of glycerol from spent-lye done by distillation under reduced pressure (vacuum distillation).

74. Identify the mixture that shows positive deviations from Raoult's law.

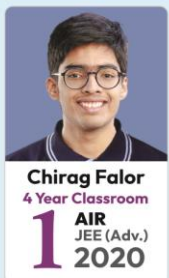
(1) $(\text{CH}_3)_2\text{CO} + \text{C}_6\text{H}_5\text{NH}_2$

(2) $\text{CHCl}_3 + \text{C}_6\text{H}_6$

(3) $\text{CHCl}_3 + (\text{CH}_3)_2\text{CO}$

(4) $(\text{CH}_3)_2\text{CO} + \text{CS}_2$

Answer (4)



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- Sol.** (1) $\text{CH}_3-\text{C}(=\text{O})-\text{CH}_3 + \text{C}_6\text{H}_5\text{NH}_2$
acetone Aniline
H-Bonding between acetone and aniline is more stronger than acetone-acetone and aniline-aniline.
- (2) $\text{CHCl}_3 + \text{C}_6\text{H}_6$
Chloroform Benzene
H-Bonding between π -cloud of Benzene and H-atom of chloroform (Negative deviation)
- (3) $\text{CHCl}_3 + \text{CH}_3-\text{C}(=\text{O})-\text{CH}_3$
Chloroform Acetone
Shows negative deviation due to H-Bonding
- (4) $\text{CH}_3-\text{C}(=\text{O})-\text{CH}_3 + \text{S}=\text{C}=\text{S}$
Acetone Carbondisulphide
Shows positive deviation because solute solvent interaction is weaker than solute-solute and solvent-solvent.

75. Given below are two statements: One is labelled as **Assertion A** and the other is labelled as **Reason R**.

Assertion A: Alcohols react both as nucleophiles and electrophiles.

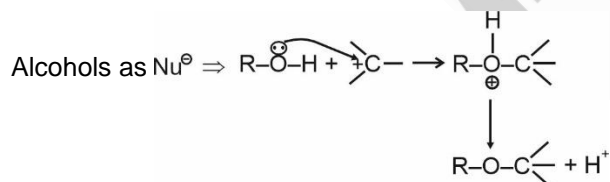
Reason R: Alcohol is react with active metals such as sodium, potassium and aluminium to yield corresponding alkoxides and liberate hydrogen.

In the light of the above statements, choose the correct answer from the options given below.

- (1) Both A and R are true but R is NOT the correct explanation of A
- (2) A is true but R is false
- (3) Both A and R are true and R is the correct explanation of A
- (4) A is false but R is true

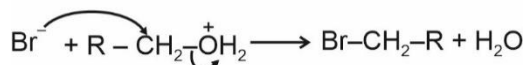
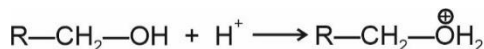
Answer (1)

Sol. Assertion is correct \Rightarrow

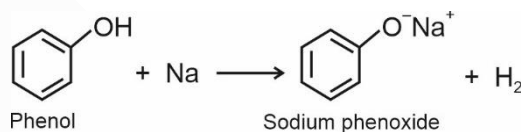
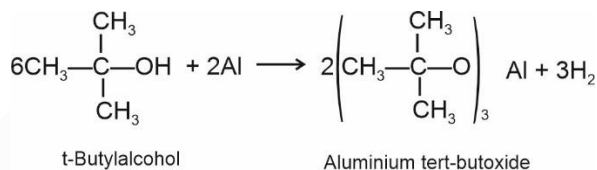
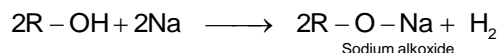


Bond between $\text{R}-\text{O}-\text{H}$ is broken when alcohol act as nucleophile

Alcohols as electrophile \Rightarrow Bond between $\text{H}_3\text{C}-\text{OH}$ is broken where alcohol act as electrophile.



Reason is also correct :



76. Given below are two statements: One is labelled as **Assertion A** and the other is labelled as **Reason R**.

Assertion A: pK_a value of phenol is 10.0 while that of ethanol is 15.9.

Reason R: Ethanol is stronger acid than phenol.

In the light of the above statements, choose the correct answer from the options given below.

- (1) Both A and R are true but R is NOT the correct explanation of A
- (2) A is true but R is false
- (3) Both A and R are true and R is the correct explanation of A
- (4) A is false but R is true

Answer (2)

Sol. pK_a of phenol = 10.0

pK_a of ethanol = 15.9

Acid which has more pK_a is weaker acid.



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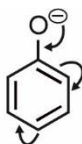
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Ethanol is weaker acid than phenol



Negative charge is destabilised by +I effect of ethyl group.



Negative charge is stabilised by -R effect of benzene ring.

Hence, removal of H^+ is easier in case of phenol as compared to ethanol.

77. A species having carbon with sextet of electrons and can act as electrophile is called

- (1) Pentavalent carbon (2) Carbon free radical
(3) Carbocation (4) Carbanion

Answer (3)

Sol. Sextet of electron means 6 electrons in outermost shell.

A species having six electron in outermost shell is electron deficient and hence can act as electrophile (electron loving).

Carbocation is a species which have $6e^-$ s in outermost shell and can act as E^+ .

78. Given below are two statements:

Statement I: IUPAC name of $\text{HO}-\text{CH}_2-(\text{CH}_2)_3-\text{CH}_2-\text{COCH}_3$ is 7-hydroxyheptan-2-one.

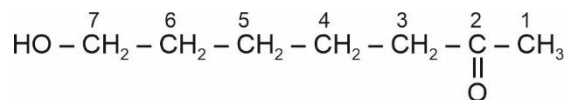
Statement II: 2-oxoheptan-7-ol is the correct IUPAC name for above compound.

In the light of the above statements, choose the most appropriate answer from the options given below.

- (1) Both statement I and statement II are incorrect
(2) Statement I is incorrect but statement II is correct
(3) Statement I is correct but statement II is incorrect
(4) Both statement I and statement II are correct

Answer (3)

Sol.



Correct IUPAC name is

7-Hydroxyheptan-2-one

Hence, statement I is correct and statement II is incorrect.

79. Given below are two statements:

Statement I: Noble gases have very high boiling points.

Statement II: Noble gases are monoatomic gases. They are held together by strong dispersion forces. Because of this they are liquefied at very low temperature. Hence, they have very high boiling points.

In the light of the above statements, choose the correct answer from the options given below.

- (1) Both statement I and statement II are true
(2) Both statement I and statement II are false
(3) Statement I is false but statement II is true
(4) Statement I is true but statement II is false

Answer (2)

Sol. Noble gases have very low melting and boiling points because noble gases are held together by weak dispersion forces.

Even helium has lowest boiling point (4.2 K) of any known substance.

Therefore, both statement I and II are incorrect.

80. Identify the factor from the following that does not affect electrolytic conductance of a solution.

- (1) The nature of solvent used
(2) Concentration of the electrolyte
(3) The nature of the electrolyte added
(4) The nature of the electrode used

Answer (4)

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Sol. Conductivity of electrolytic solution depends upon:

- Nature of electrolyte added.
- Size of ions produced and their solvation
- Nature of the solvent and viscosity.
- Concentration of the electrolyte.
- Temperature (Increases with increase of temp.).

It does not depend on nature of electrode used.

SECTION - B

Numerical Value Type Questions: This section contains 10 Numerical based questions. Attempt any 5 questions out of 10. The answer to each question should be rounded-off to the nearest integer.

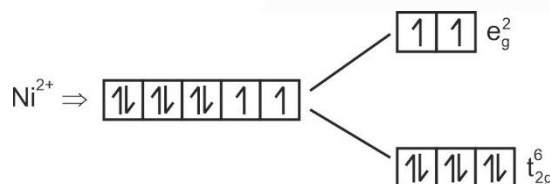
81. The 'spin only' magnetic moment for $[\text{Ni}(\text{NH}_3)_6]^{2+}$ is _____ $\times 10^{-1}$ BM.

(given = atomic number of Ni : 28)

Answer (28)

Sol. $[\text{Ni}(\text{NH}_3)_6]^{2+} \Rightarrow$ Nickel in +2 oxidation state

Ni^{2+} in presence of 6 NH_3 ligand (strong field).



Ni^{2+} have two unpaired electrons, and forms sp^3d^2 hybridisation in presence of 6 NH_3 ligand.

$$\mu = \sqrt{n(n+2)} = \sqrt{2(2+2)} = \sqrt{2 \times 4}$$

$$\mu = \sqrt{8} = 2.82 \approx 2.8 \text{ BM}$$

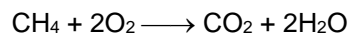
$$\approx 28 \times 10^{-1} \text{ BM}$$

Hence, answer is $\Rightarrow 28$

82. Number of moles of methane required to produce 22 g $\text{CO}_{2(g)}$ after combustion is $x \times 10^{-2}$ moles. The value of x is _____.

Answer (50)

Sol. Reaction of combustion of methane:



1 mol methane produce 1 mol CO_2 .

\therefore 1 mol methane produce 44 g CO_2 .

Hence, $\frac{1}{2}$ mol CH_4 will produce 22 g CO_2 .

\therefore Moles of methane required to produce 22 g CO_2 .

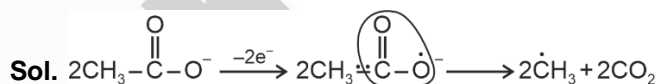
$$\Rightarrow 0.5 \text{ mol}$$

$$\Rightarrow 50 \times 10^{-2} \text{ mol}$$

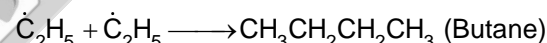
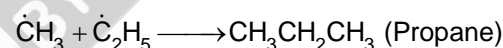
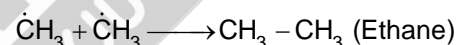
Hence, the value of $x = 50$

83. Number of alkanes obtained on electrolysis of a mixture of CH_3COONa and $\text{C}_2\text{H}_5\text{COONa}$ is _____.

Answer (3)



$\dot{\text{C}}_2\text{H}_5$ and $\dot{\text{C}}\text{H}_3$ created.

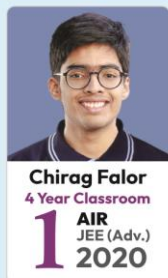


3 alkanes were obtained on electrolysis of $\text{CH}_3\text{COO}^-\text{Na}^+$ and $\text{C}_2\text{H}_5\text{COO}^-\text{Na}^+$ mixture.

84. Molar mass of the salt from NaBr , NaNO_3 , KI and CaF_2 which does not evolve coloured vapours on heating with concentrated H_2SO_4 is _____ g mol^{-1} .

(Molar mass in g mol^{-1} : Na : 23, N : 14, K : 39, O : 16, Br : 80, I : 127, F : 19, Ca : 40)

Answer (78)



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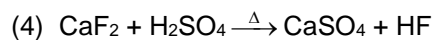
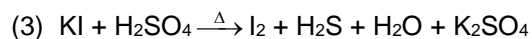
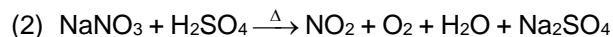
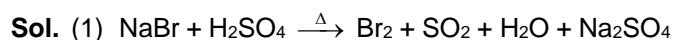
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CaF_2 will not give coloured vapours on heating with conc. H_2SO_4 .

Other will give coloured vapours due to formation of Br_2 , NO_2 , I_2 .

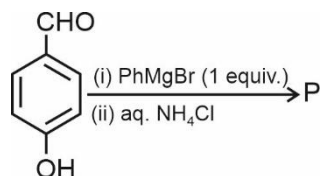
$\text{Br}_2 \rightarrow$ Red-brown colour

$\text{I}_2 \rightarrow$ Violet colour

$\text{NO}_2 \rightarrow$ Deep red orange gas.

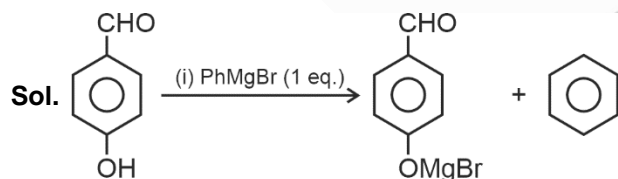
Molar mass of $\text{CaF}_2 \Rightarrow 40 + 19 + 19 = 78 \text{ g/mol}$.

85. The product of the following reaction is P.

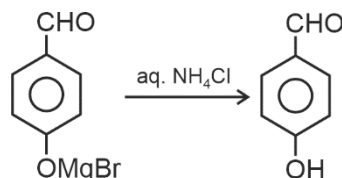


The number of hydroxyl groups present in the product P is _____.

Answer (1)



Number of hydroxyl group = zero.



Phenolic ($-\text{OH}$) group = 1

86. The ionization energy of sodium in kJ mol^{-1} , if electromagnetic radiation of wavelength 242 nm is just sufficient to ionize sodium atom is _____.

Answer (494)

Sol. $\lambda = 242 \text{ nm} = 242 \times 10^{-9} \text{ m}$

Energy to just remove 1 electron from 1 mol sodium atom =

Energy for removal of $1e^-$ from 1 atom

$$\Rightarrow E = \frac{hc}{\lambda} = \frac{6.62 \times 10^{-34} \times 3 \times 10^8}{242 \times 10^{-9}}$$

Energy for removal of $1e^-$ from 1 mol atoms

$$\Rightarrow E = \frac{hc}{\lambda} \times N_A$$

$$E = \frac{6.62 \times 10^{-34} \times 3 \times 10^8 \times 6.023 \times 10^{23}}{242 \times 10^{-9}}$$

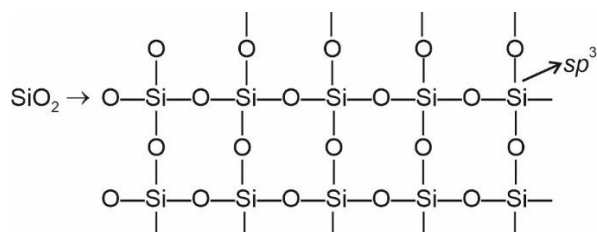
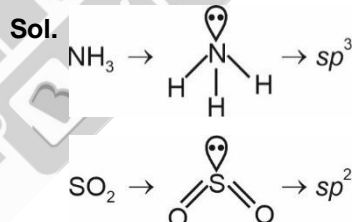
$$E = 494.28 \text{ kJ/mol}$$

$$\approx 494$$

87. The number of species from the following in which the central atom uses sp^3 hybrid orbitals in its bonding is _____.

NH_3 , SO_2 , SiO_2 , BeCl_2 , CO_2 , H_2O , CH_4 , BF_3

Answer (4)



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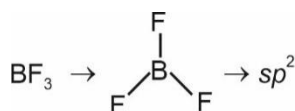
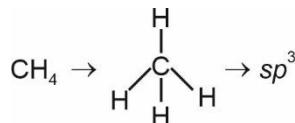
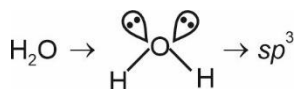
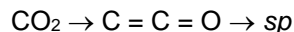
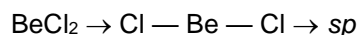
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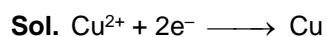
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88. One Faraday of electricity liberates $x \times 10^{-1}$ gram atom of copper from copper sulphate. x is _____.

Answer (5)



2 Faraday will liberate = 1 mol Cu

= 1 gram atom Cu

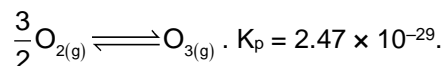
1 Faraday will liberate = 0.5 mol Cu

= 0.5 gram atom Cu

$$0.5 = 5 \times 10^{-1}$$

$$\therefore \text{Ans} \Rightarrow x = 5$$

89. Consider the following reaction at 298 K.



$\Delta_r G^\circ$ for the reaction is _____ kJ. (Given $R = 8.314 \text{ JK}^{-1} \text{ mol}^{-1}$)

Answer (163)

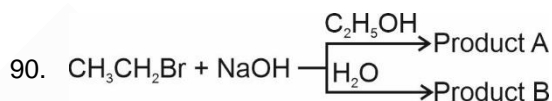
Sol. $\Delta G^\circ = -RT \ln K_p$

$$\Delta G^\circ = -8.314 \times 298 \times 2.303 \times \log 2.47 \times 10^{-29}$$

$$\Delta G^\circ = +163199.52 \text{ J}$$

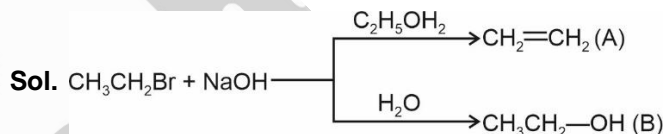
$$\Delta G^\circ = 163.2 \text{ J}$$

$$\Delta G^\circ \approx 163 \text{ kJ}$$



The total number of hydrogen atoms in product A and product B is _____.

Answer (10)




In product A = 4 Hydrogen atoms are present

In product B = 6 Hydrogen atoms are present

Total H-atom = 4 + 6 = 10

□ □ □



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