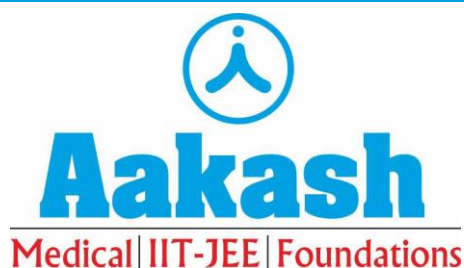


24/01/2025

Evening



Corporate Office : AESL, 3rd Floor, Incuspace Campus-2, Plot-13, Sector-18, Udyog Vihar,  
Gurugram, Haryana-122018

## Answers & Solutions

Time : 3 hrs.

for

M.M. : 300

### JEE (Main)-2025 Phase-1

[Computer Based Test (CBT) mode]

(Mathematics, Physics and Chemistry)

#### IMPORTANT INSTRUCTIONS:

- (1) The test is of **3 hours** duration.
- (2) This test paper consists of 75 questions. Each subject (MPC) has 25 questions. The maximum marks are 300.
- (3) This question paper contains **Three** Parts. **Part-A** is Physics, **Part-B** is Chemistry and **Part-C** is **Mathematics**. Each part has only two sections: **Section-A** and **Section-B**.
- (4) **Section - A** : Attempt all questions.
- (5) **Section - B** : Attempt all questions.
- (6) **Section - A (01 – 20)** contains 20 multiple choice questions which have **only one correct answer**. Each question carries **+4 marks** for correct answer and **–1 mark** for wrong answer.
- (7) **Section - B (21 – 25)** contains 5 **Numerical value** based questions. The answer to each question should be rounded off to the **nearest integer**. Each question carries **+4 marks** for correct answer and **–1 mark** for wrong answer.

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**MATHEMATICS**

**SECTION - A**

**Multiple Choice Questions:** This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

**Choose the correct answer:**

1. Group A consists of 7 boys and 3 girls, while group B consists of 6 boys and 5 girls. The number of ways, 4 boys and 4 girls can be invited for a picnic if 5 of them must be from group A and the remaining 3 from group B, is equal to:

- (1) 8575 (2) 8750  
(3) 8925 (4) 9100

**Answer (3)**

**Sol.**

Group A		Group B		
B	G	B	G	Ways
4	1	0	3	${}^7C_4 \cdot {}^3C_1 \cdot {}^6C_0 \cdot {}^5C_3$
3	2	1	2	${}^7C_3 \cdot {}^3C_2 \cdot {}^6C_1 \cdot {}^5C_2$
2	3	2	1	${}^7C_2 \cdot {}^3C_3 \cdot {}^6C_2 \cdot {}^5C_1$

$$\text{Total ways} = 30 \cdot {}^7C_4 + 180 \cdot {}^7C_3 + 75 \cdot {}^7C_2 = 8925$$

2. Let  $\vec{a} = 3\hat{i} - \hat{j} + 2\hat{k}$ ,  $\vec{b} = \vec{a} \times (\hat{i} - 2\hat{k})$  and  $\vec{c} = \vec{b} \times \hat{k}$ .

Then the projection of  $\vec{c} = 2\hat{j}$  on  $\vec{a}$  is:

- (1)  $\sqrt{14}$  (2)  $2\sqrt{7}$   
(3)  $2\sqrt{14}$  (4)  $3\sqrt{7}$

**Answer (3)**

**Sol.**

$$\vec{a} = 3\hat{i} - \hat{j} + 2\hat{k} \quad \vec{b} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 3 & -1 & 2 \\ 1 & 0 & -2 \end{vmatrix} = 2\hat{i} + 8\hat{j} + \hat{k}$$

$$\vec{b} = \vec{a} \times (\hat{i} - 2\hat{k}) \Rightarrow \vec{c} = 2\hat{j}$$

$$\vec{c} = \vec{b} \times \hat{k} = 8\hat{i} - 2\hat{j} \Rightarrow \vec{c} - 2\hat{j} = 8\hat{i} - 4\hat{j}$$

Projection of  $(\vec{c} - 2\hat{j})$  on  $\vec{a}$

$$= (\vec{c} - 2\hat{j}) \cdot \frac{\vec{a}}{|\vec{a}|} = \left( \frac{24 + 4}{\sqrt{14}} \right) = 2\sqrt{14}$$

3. Let  $f: (0, \infty) \rightarrow \mathbf{R}$  be function which is differentiable at all points of its domain and satisfies the condition  $x^2 f'(x) = 2xf(x) + 3$ , with  $f(1) = 4$ . Then  $2f(2)$  is equal to:

- (1) 23 (2) 19  
(3) 29 (4) 39

**Answer (4)**

**Sol.**  $x^2 f'(x) = 2xf(x) + 3$

Let  $y = f(x) \Rightarrow \frac{dy}{dx} = f'(x)$

$$\frac{dy}{dx} = \frac{2y}{x} + \frac{3}{x^2}$$

$$\Rightarrow \frac{dy}{dx} + y \left( \frac{-2}{x} \right) = \frac{3}{x^2}$$

$$\text{I.F} = e^{\int \frac{-2}{x} dx} = e^{-2 \ln x} = \frac{1}{x^2}$$

$$\Rightarrow y \left( \frac{1}{x^2} \right) = \int \frac{3}{x^2} \times \frac{1}{x^2} dx + c$$

$$\frac{y}{x^2} = -x^{-3} + c, f(1) = 4 = y$$

$$\frac{4}{(1)^2} = -(1)^{-3} + c \Rightarrow c = 5$$

$$\Rightarrow \frac{y}{x^2} = \frac{-1}{x^3} + 5 \Rightarrow f(x) = \frac{-1}{x} + 5x^2$$

$$2f(2) = 2 \left[ \frac{-1}{2} + 5(2)^2 \right] = 2 \left[ \frac{-1}{2} + 20 \right] = 39$$



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4. Let the position vectors of three vertices of a triangle be  $4\vec{p} + \vec{q} - 3\vec{r}$ ,  $-5\vec{p} + \vec{q} + 2\vec{r}$  and  $2\vec{p} - \vec{q} + 2\vec{r}$ . If the position vectors of the orthocentre and the circumcentre of the triangle are  $\frac{\vec{p} + \vec{q} + \vec{r}}{4}$  and  $\alpha\vec{p} + \beta\vec{q} + \gamma\vec{r}$  respectively, then  $\alpha + 2\beta + 5\gamma$  is equal to:

- (1) 4 (2) 6  
(3) 3 (4) 1

**Answer (3)**

**Sol.** Orthocentre =  $\frac{\vec{p} + \vec{q} + \vec{r}}{4}$

Circumcentre =  $\alpha\vec{p} + \beta\vec{q} + \gamma\vec{r}$

Centroid =  $\left( \frac{4\vec{p} + \vec{q} - 3\vec{r} - 5\vec{p} + \vec{q} + 2\vec{r} + 2\vec{p} - \vec{q} + 2\vec{r}}{3} \right)$   
 $= \left( \frac{\vec{p} + \vec{q} + \vec{r}}{3} \right)$

Now



$\frac{2(\alpha\vec{p} + \beta\vec{q} + \gamma\vec{r}) + \frac{\vec{p} + \vec{q} + \vec{r}}{4}}{2+1} = \left( \frac{\vec{p} + \vec{q} + \vec{r}}{3} \right)$

$\Rightarrow 8(\alpha\vec{p} + \beta\vec{q} + \gamma\vec{r}) = 3(\vec{p} + \vec{q} + \vec{r})$

$\Rightarrow 8\alpha = 3, 8\beta = 3, 8\gamma = 3$

$\alpha = \frac{3}{8} = \beta = \gamma$

$\alpha + 2\beta + 5\gamma = \frac{3}{8} + \frac{6}{8} + \frac{15}{8} = \frac{27}{8} = 3$

5. Let  $(2, 3)$  be the largest open interval in which the function  $f(x) = 2 \log_e(x-2) - x^2 + ax + 1$  is strictly increasing and  $(b, c)$  be the largest open interval, in which the function  $g(x) = (x-1)^3(x+2-a)^2$  is strictly decreasing. Then  $100(a+b-c)$  is equal to:

- (1) 280 (2) 360  
(3) 160 (4) 420

**Answer (2)**

**Sol.**  $f(x) = 2 \ln(x-2) - x^2 + ax + 1$

$f'(x) = \frac{2}{x-2} - 2x + a > 0$

$f''(x) = \frac{-2}{(x-2)^2} - 2 < 0$

$\Rightarrow f'(x)$  is decreasing

and  $f'(3) \geq 0$

$2 - 6 + a \geq 0 \Rightarrow a \geq 4$

$a_{\min} = 4$

$\therefore g(x)$  is strictly decreasing

Now,  $g(x) = (x-1)^3(x-2)^2$

$g'(x) = 2(x-1)^3(x-2) + 3(x-1)^2(x-2)^2 < 0$

$= (x-1)^2(x-2)[2(x-1) + 3(x-2)] < 0$

$= (x-1)^2(x-2)(5x-8) < 0$

$\Rightarrow x \in \left( \frac{8}{5}, 2 \right) \Rightarrow b = \frac{8}{5} \quad c = 2$

Now,  $100(a+b-c) = 100 \left[ 4 + \frac{8}{5} - 2 \right]$

$= 100 \times \frac{18}{5} = 360$

6. The equation of the chord, of the ellipse  $\frac{x^2}{25} + \frac{y^2}{16} = 1$ ,

whose mid-point is  $(3, 1)$  is:

- (1)  $5x + 16y = 31$   
(2)  $25x + 101y = 176$   
(3)  $48x + 25y = 169$   
(4)  $4x + 122y = 134$

**Answer (3)**

**Sol.**  $\frac{x^2}{25} + \frac{y^2}{16} = 1$

Chord with mid-point  $(3, 1)$

$T = S_1$



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$$\frac{xx_1}{25} + \frac{yy_1}{16} - 1 = \frac{x_1^2}{25} + \frac{y_1^2}{16}$$

$$\frac{3x}{25} + \frac{y}{16} = \frac{9}{25} + \frac{1}{16}$$

$$48x + 25y = 9 \times 16 + 25$$

$$48x + 25y = 169$$

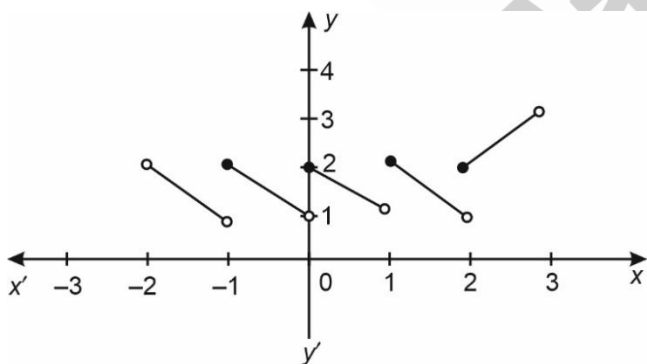
7. Let  $[x]$  denote the greatest integer function, and let  $m$  and  $n$  respectively be the numbers of the points, where the function  $f(x) = [x] + |x - 2|$ ,  $-2 < x < 3$ , is not continuous and not differentiable. Then  $m + n$  is equal to :

- (1) 8  
(2) 6  
(3) 7  
(4) 9

**Answer (1)**

**Sol.**  $f(x) = [x] + |x - 2|$ ,  $-2 < x < 3$

$$\therefore f(x) = \begin{cases} -x, & -2 < x < -1 \\ 1-x, & -1 \leq x < 0 \\ 2-x, & 0 \leq x < 1 \\ 3-x, & 1 \leq x < 2 \\ x, & 2 \leq x < 3 \end{cases}$$



It is clearly discontinuous at 4 points and non-differentiable at 4 points.

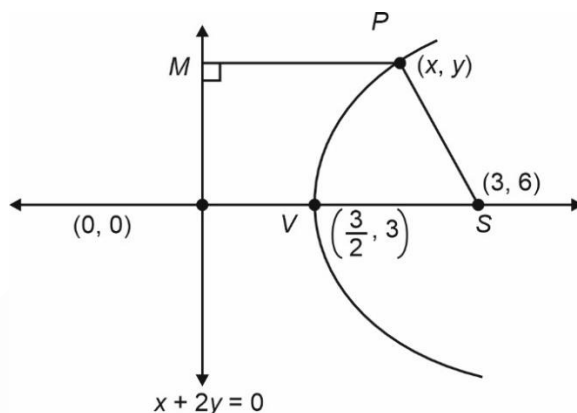
$$\therefore m + n = 8$$

8. If the equation of the parabola with vertex  $V\left(\frac{3}{2}, 3\right)$  and the directrix  $x + 2y = 0$  is  $\alpha x^2 + \beta y^2 - \gamma xy - 30x - 60y + 225 = 0$ , then  $\alpha + \beta + \gamma$  is equal to:

- (1) 7  
(2) 6  
(3) 9  
(4) 8

**Answer (3)**

**Sol.**



$\therefore$  Equation of parabola is  $PS = PM$

$$\Rightarrow PS^2 = PM^2$$

$$(x-3)^2 + (y-6)^2 = \left(\frac{x+2y}{\sqrt{5}}\right)^2$$

$$5x^2 - 30x + 5y^2 - 60y + 225 = x^2 + 4y^2 + 4xy$$

$$4x^2 + y^2 - 4xy - 30x - 60y + 225 = 0$$

We get :  $\alpha = 4$ ,  $\beta = 1$ ,  $\gamma = 4$

$$\therefore \alpha + \beta + \gamma = 9$$

9. Let  $A = [a_{ij}]$  be a square matrix of order 2 with entries either 0 or 1. Let  $E$  be the event that  $A$  is an invertible matrix. Then the probability  $P(E)$  is :

- (1)  $\frac{3}{16}$   
(2)  $\frac{3}{8}$   
(3)  $\frac{1}{8}$   
(4)  $\frac{5}{8}$

**Answer (2)**

**Sol.**  $A = [a_{ij}]_{2 \times 2}$  and entries are 0 or 1.

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$$\therefore \begin{vmatrix} a & b \\ c & d \end{vmatrix} = 0$$

$$\Rightarrow ad - bc = 0$$

$$\text{Case I: } ad = bc = 1$$

$$\therefore a = b = c = d = 1$$

$$\text{Case II: } ad = bc = 0$$

$$a = 0, d = 0 \quad b = 0, c = 0$$

$$a = 0, d = 1 \quad b = 0, c = 1$$

$$a = 1, d = 0 \quad b = 1, c = 0$$

$\therefore$  Total 10 cases when matrix is non invertible

$$\text{Total possible matrix} = 2^4 = 16$$

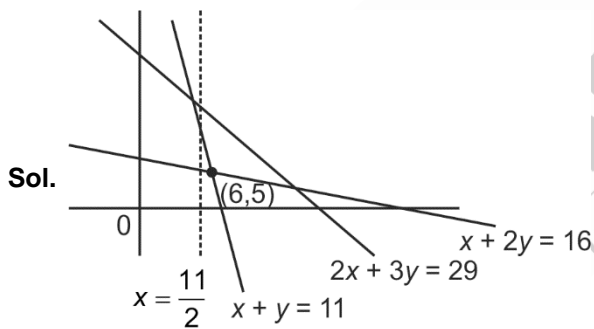
Required probability of invertible

$$= \frac{16 - 10}{16} = \frac{6}{16} = \frac{3}{8}$$

10. Let the points  $\left(\frac{11}{2}, \alpha\right)$  lie on or inside the triangle with sides  $x + y = 11$ ,  $x + 2y = 16$  and  $2x + 3y = 29$ . Then the product of the smallest and the largest value of  $\alpha$  is equal to :

- (1) 22                      (2) 55  
(3) 33                      (4) 44

**Answer (3)**



Clearly,  $x = \frac{11}{2}$  intersect  $x + y - 11 = 0$  at  $\left(\frac{11}{2}, \frac{11}{2}\right)$

and  $2x + 3y - 29 = 0$  at  $\left(\frac{11}{2}, 6\right) \Rightarrow \alpha = \left[\frac{11}{2}, 6\right]$

$$\alpha_{\min} \cdot \alpha_{\max} = \frac{11}{2} \cdot 6 = 33$$

$$11. \text{ If } 7 = 5 + \frac{1}{7}(5 + \alpha) + \frac{1}{7^2}(5 + 2\alpha) + \frac{1}{7^3}(5 + 3\alpha) +$$

$\dots \infty$ , then the value of  $\alpha$  is

- (1) 1  
(2) 6  
(3)  $\frac{1}{7}$   
(4)  $\frac{6}{7}$

**Answer (2)**

$$\text{Sol. } S = a + (a + d)r + (a + 2d)r^2 + \dots$$

$$\text{Then } S = \frac{a}{1-r} + \frac{dr}{(1-r)^2}, |r| < 1$$

$$\text{Since, } r = \frac{1}{7} \text{ and } a = 5, d = \alpha$$

$$7 = \frac{5}{1 - \frac{1}{7}} + \frac{\alpha \cdot \frac{1}{7}}{\left(1 - \frac{1}{7}\right)^2}$$

$$\Rightarrow \alpha = 6$$

12. Suppose  $A$  and  $B$  are the coefficients of  $30^{\text{th}}$  and  $12^{\text{th}}$  terms respectively in the binomial expansion of  $(1 + x)^{2n-1}$ . If  $2A = 5B$ , then  $n$  is equal to :

- (1) 19                      (2) 20  
(3) 21                      (4) 22

**Answer (3)**

$$\text{Sol. } T_{r+1} = {}^{2n-1}C_r x^r$$

$$\text{Coefficient of } T_{30} = {}^{2n-1}C_{29} = A$$

$$\text{Coefficient of } T_{12} = {}^{2n-1}C_{11} = B$$

$$\Rightarrow 2({}^{2n-1}C_{29}) = 5({}^{2n-1}C_{11})$$

$$\frac{2n}{30} \cdot {}^{2n-1}C_{29} = \frac{2n}{12} \cdot {}^{2n-1}C_{11}$$

$$\Rightarrow n = 21$$



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13. Let

$$A = \left\{ x \in (0, \pi) - \left( \frac{\pi}{2} \right) : \log_{(2/\pi)} |\sin x| + \log_{(2/\pi)} |\cos x| = 2 \right\}$$

$$\text{and } B = \{ x \geq 0 : \sqrt{x}(\sqrt{x} - 4) - 3|\sqrt{x} - 2| + 6 = 0 \}.$$

Then  $n(A \cup B)$  is equal to

- (1) 2                                      (2) 6  
(3) 4                                      (4) 8

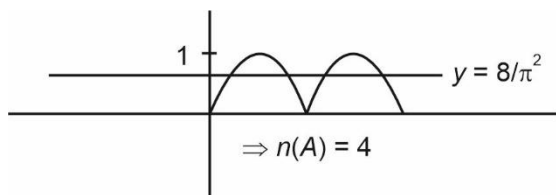
**Answer (4)**

**Sol.**  $A = \left\{ x \in (0, \pi) - \left( \frac{\pi}{2} \right) : \log_{(2/\pi)} |\sin x| + \log_{(2/\pi)} |\cos x| = 2 \right\}$

$$\log_{2/\pi} |\sin x \cos x| = 2$$

$$\frac{|\sin 2x|}{2} = \frac{4}{\pi^2}$$

$$\Rightarrow |\sin 2x| = \frac{8}{\pi^2}$$



$$\text{and } B = \{ x \geq 0 : \sqrt{x}(\sqrt{x} - 4) - 3|\sqrt{x} - 2| + 6 = 0 \}$$

$$x - 4\sqrt{x} - 3\sqrt{x} + 6 + 6 = 0 \text{ when } \sqrt{x} - 2 \geq 0$$

$$\sqrt{x} \geq 2$$

$$\Rightarrow x - 7\sqrt{x} + 12 = 0$$

$$\Rightarrow x - 4\sqrt{x} - 3\sqrt{x} + 12 = 0$$

$$\Rightarrow \sqrt{x}\sqrt{x} - 4 - 3(\sqrt{x} - 4) = 0$$

$$\sqrt{x} = 4, \sqrt{x} = 3$$

$$\Rightarrow x = 16, 9$$

$$\text{When } \sqrt{x} - 2 < 0$$

$$\Rightarrow x - 4\sqrt{x} + 3\sqrt{x} - 6 + 6 = 0$$

$$\Rightarrow x - \sqrt{x} = 0$$

$$\Rightarrow \sqrt{x}(\sqrt{x} - 1) = 0$$

$$\Rightarrow \sqrt{x} = 0, 1$$

$$\Rightarrow x = 0, 1$$

$$\Rightarrow n(B) = 4$$

Now as  $A$  and  $B$  are mutually exclusive sets

$$N(A \cup B) = 4 + 4 = 8$$

14. In an arithmetic progression, if  $S_{40} = 1030$  and  $S_{12} = 57$ , then  $S_{30} - S_{10}$  is equal to

- (1) 525                                      (2) 510  
(3) 515                                      (4) 505

**Answer (3)**

**Sol.**  $S_{40} = 1030 \Rightarrow \frac{40}{2}[2a + 39d] = 1030$

$$\Rightarrow 2a + 39d = \frac{103}{2} \quad \dots(1)$$

$$S_{12} = 57 \Rightarrow \frac{12}{2}[2a + 11d] = 57$$

$$\Rightarrow 2a + 11d = \frac{57}{6} \quad \dots(2)$$

Equation (1) – equation (2)

$$28d = \frac{103}{2} - \frac{57}{6}$$

$$28d = \frac{309 - 57}{6}$$

$$d = \frac{3}{2}$$

$$\Rightarrow a = -\frac{7}{2}$$

$$S_{30} - S_{10} = \frac{30}{2}[2a + 29d] - \frac{10}{2}[2a + 9d]$$

$$= 15[2a + 29d] - 5[2a + 9d]$$

$$= 5[6a + 87d - 2a - 9d]$$

$$= 5[4a + 78d]$$

$$= 5[-14 + 117]$$

$$= 515$$

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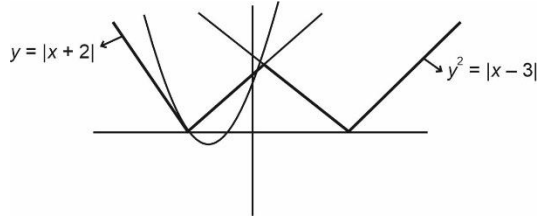
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15. The number of real solution(s) of the equation  $x^2 + 3x + 2 = \min \{|x-3|, |x+2|\}$  is

- (1) 2 (2) 1  
(3) 3 (4) 0

**Answer (1)**

**Sol.**  $x^2 + 3x + 2 = \min \{|x-3|, |x+2|\}$



$$y = x^2 + 3x + 2$$

$$y = x^2 + 2\left(\frac{3}{2}\right)x + \frac{9}{4} - \frac{9}{4} + 2$$

$$y = \left(x + \frac{3}{2}\right)^2 - \frac{1}{4}$$

$$y + \frac{1}{4} = \left(x + \frac{3}{2}\right)^2$$

$$\Rightarrow \text{Parabola vertex } \left(\frac{-3}{2}, \frac{-1}{4}\right)$$

$\Rightarrow$  By graph 2 solution possible

16. For some  $a, b$ , let  $f(x) = \begin{vmatrix} a + \frac{\sin x}{x} & 1 & b \\ a & 1 + \frac{\sin x}{x} & b \\ a & 1 & b + \frac{\sin x}{x} \end{vmatrix}$ ,

$x \neq 0$ ,  $\lim_{x \rightarrow 0} f(x) = \lambda + \mu a + \nu b$ . Then  $(\lambda + \mu + \nu)^2$  is

equal to

- (1) 36  
(2) 16  
(3) 9  
(4) 25

**Answer (2)**

**Sol.**  $\lim_{x \rightarrow 0} \begin{vmatrix} a + \frac{\sin x}{x} & 1 & b \\ a & 1 + \frac{\sin x}{x} & b \\ a & 1 & b + \frac{\sin x}{x} \end{vmatrix} = \lambda + \mu a + \nu b$

At  $\lim x \rightarrow 0$ ,

$$f(x) = \begin{vmatrix} a+1 & 1 & b \\ a & 1+1 & b \\ a & 1 & b+1 \end{vmatrix} = \lambda + \mu a + \nu b$$

$$R_1 \rightarrow R_1 - R_2$$

$$R_2 \rightarrow R_2 - R_3$$

$$\begin{vmatrix} 1 & -1 & 0 \\ 0 & 1 & -1 \\ a & 1 & b+1 \end{vmatrix} = \lambda + \mu a + \nu b$$

$$C_2 \rightarrow C_1 - C_2$$

$$\begin{vmatrix} 1 & 0 & 0 \\ 0 & 1 & -1 \\ a & a+1 & b+1 \end{vmatrix} = \lambda + \mu a + \nu b$$

$$a + b + 2 = \lambda + \mu a + \nu b$$

$$\lambda = 2, \mu = 1, \nu = 1$$

$$(\lambda + \mu + \nu) = (2 + 1 + 1)^2 = 16$$

17. The function  $f : (-\infty, \infty) \rightarrow (-\infty, 1)$ , defined by

$$f(x) = \frac{2^x - 2^{-x}}{2^x + 2^{-x}}$$
 is:

- (1) Onto but not one-one  
(2) Both one-one and onto  
(3) One-one but not onto  
(4) Neither one-one nor onto

**Answer (3)**



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**Sol.**  $f(x) = \frac{2^x - 2^{-x}}{2^x + 2^{-x}} = \frac{2^{2x} - 1}{2^{2x} + 1} = \frac{2^{2x} + 1 - 2}{2^{2x} + 1}$

$$f(x) = 1 - \frac{2}{2^{2x} + 1}$$

$2^{2x}$  is one-one, so  $f(x)$  is one-one

for  $x \in (-\infty, \infty)$

$2^x \in (0, \infty)$

$2^{2x} + 1 \in (1, \infty)$

$$\frac{1}{2^{2x} + 1} \in (0, 1)$$

$$\frac{-2}{2^{2x} + 1} \in (-2, 0)$$

$$1 - \frac{2}{2^{2x} + 1} \in (-1, 1)$$

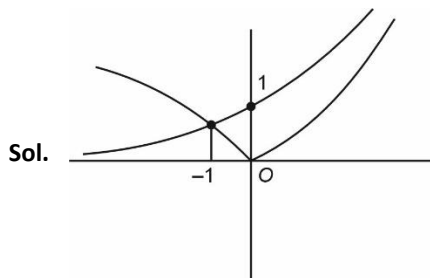
Range of  $f(x)$  is  $(-1, 1)$  but codomain of  $f(x)$  is  $(-\infty, 1)$

So  $f(x)$  is into

18. The area of the region enclosed by the curves  $y = e^x$ ,  $y = |e^x - 1|$  and  $y$ -axis is:

- (1)  $1 + \log_e 2$
- (2)  $\log_e 2$
- (3)  $1 - \log_e 2$
- (4)  $2\log_e 2 - 1$

**Answer (3)**



$$e^x = 1 - e^x \Rightarrow 2e^x = 1$$

$$\Rightarrow e^x = \frac{1}{2}$$

$$\Rightarrow x = \ln \frac{1}{2}$$

$$\int_{\ln(1/2)}^0 [e^x - (1 - e^x)] dx$$

$$= \int_{\ln 2}^0 (2e^x - 1) dx = 2e^x - x \Big|_{\ln 2}^0$$

$$= 2 - (1 + \ln 2)$$

$$= 1 - \log_e 2$$

19. If  $\alpha > \beta > \gamma > 0$ , then the expression

$$\cot^{-1} \left\{ \beta + \frac{(1 + \beta^2)}{(\alpha - \beta)} \right\} + \cot^{-1} \left\{ \gamma + \frac{(1 + \gamma^2)}{(\beta - \gamma)} \right\} + \cot^{-1} \left\{ \alpha + \frac{1 + \alpha^2}{\gamma - \alpha} \right\}$$

equal to:

- (1) 0
- (2)  $\frac{\pi}{2} - (\alpha + \beta + \gamma)$
- (3)  $3\pi$
- (4)  $\pi$

**Answer (4)**

**Sol.**  $\cot^{-1} \left( \frac{\alpha\beta - \beta^2 + 1 + \beta^2}{\alpha - \beta} \right) + \cot^{-1} \left( \frac{\beta\gamma - \gamma^2 + 1 + \gamma^2}{\beta - \gamma} \right) + \cot^{-1} \left( \frac{\alpha\gamma - \alpha^2 + 1 + \alpha^2}{\gamma - \alpha} \right)$

$$= \cot^{-1} \left( \frac{1 + \alpha\beta}{\alpha - \beta} \right) + \cot^{-1} \left( \frac{1 + \beta\gamma}{\beta - \gamma} \right) + \cot^{-1} \frac{1 + \gamma\alpha}{\gamma - \alpha}$$

$$= \tan^{-1} \left( \frac{\alpha - \beta}{1 + \alpha\beta} \right) + \tan^{-1} \left( \frac{\beta - \gamma}{1 + \beta\gamma} \right) + \pi + \tan^{-1} \left( \frac{\gamma - \alpha}{1 + \gamma\alpha} \right)$$

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$$= \tan^{-1}\alpha - \tan^{-1}\beta + \tan^{-1}\beta - \tan^{-1}\gamma + \pi + \tan^{-1}\gamma - \tan^{-1}\alpha$$

$$= \pi$$

20. If the system of equations

$$x + 2y - 3z = 2$$

$$2x + \lambda y + 5z = 5$$

$$14x + 3y + \mu z = 33$$

has infinitely many solutions, then  $\lambda + \mu$  is equal to:

(1) 12

(2) 10

(3) 13

(4) 11

**Answer (1)**

**Sol.**  $\Delta = \begin{vmatrix} 1 & 2 & -3 \\ 2 & \lambda & 5 \\ 14 & 3 & \mu \end{vmatrix} = 0 \Rightarrow \lambda\mu + 42\lambda - 4\mu + 107 = 0$

$$\Delta_1 = \begin{vmatrix} 2 & 2 & -3 \\ 5 & \lambda & 5 \\ 33 & 3 & \mu \end{vmatrix} = 0 \Rightarrow 2\lambda\mu + 99\lambda - 10\mu + 255 = 0$$

$$\Delta_2 = \begin{vmatrix} 1 & 2 & -3 \\ 2 & 5 & 5 \\ 14 & 33 & \mu \end{vmatrix} = 0 \Rightarrow \mu = 13$$

Also,  $\lambda = -1$

Hence,  $\lambda + \mu = 13 - 1 = 12$

### SECTION - B

**Numerical Value Type Questions:** This section contains 5 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. Let  $P$  be the image of the point  $Q(7, -2, 5)$  in the line

$$L: \frac{x-1}{2} = \frac{y+1}{3} = \frac{z}{4} \text{ and } R(5, p, q) \text{ be a point on } L.$$

Then the square of the area of  $\Delta PQR$  is \_\_\_\_\_.

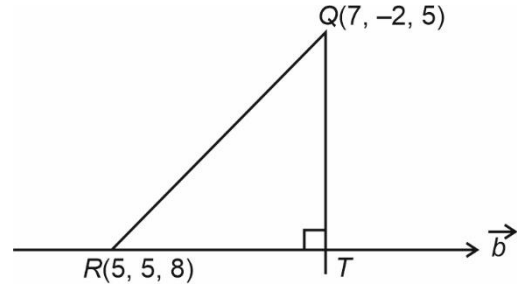
**Answer (957)**

**Sol.** Let  $R(2\lambda + 1, 3\lambda - 1, 4\lambda)$

$$2\lambda + 1 = 5$$

$$\lambda = 2$$

$$\Rightarrow R(5, 5, 8)$$



Let say  $T(2\lambda + 1, 3\lambda - 1, 4\lambda)$

$$\text{So, } \overrightarrow{QT} = (2\lambda - 6)\hat{i} + (3\lambda + 1)\hat{j} + (4\lambda - 5)\hat{k}$$

$$\text{and } \vec{b} = 2\hat{i} + 3\hat{j} + 4\hat{k}$$

$$\overrightarrow{QT} \cdot \vec{b} = 0$$

$$4\lambda - 12 + 9\lambda + 3 + 16\lambda - 20 = 0$$

$$\lambda = 1$$

$$T(3, 2, 4)$$

$$QT = \sqrt{33}, RT = \sqrt{29}$$

$$(\text{ar}(\Delta PQR))^2 = \left(\frac{1}{2} \sqrt{33} \cdot 2 \cdot \sqrt{29}\right)^2$$

$$= 957$$

22. If  $\int \frac{2x^2 + 5x + 9}{\sqrt{x^2 + x + 1}} dx = x\sqrt{x^2 + x + 1} + \alpha\sqrt{x^2 + x + 1} +$

$$\beta \log_e \left| x + \frac{1}{2} + \sqrt{x^2 + x + 1} \right| + C, \text{ where } C \text{ is the constant of integration, then } \alpha + 2\beta \text{ is equal to } \underline{\hspace{2cm}}.$$

**Answer (16)**



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**Sol.**  $I = \int \frac{2x^2 + 5x + 9}{x^2 + x + 1} dx$

Let  $\frac{2x^2 + 5x + 9}{\sqrt{x^2 + x + 1}} = \frac{A(x^2 + x + 1) + B(2x + 1) + C}{\sqrt{x^2 + x + 1}}$

Then,  $A = 2, B = \frac{3}{2}$  and  $C = \frac{11}{2}$

$$\begin{aligned} \therefore I &= \int \frac{2(x^2 + x + 1) + \frac{3}{2}(2x + 1) + \frac{11}{2}}{\sqrt{x^2 + x + 1}} dx \\ &= 2 \int \sqrt{x^2 + x + 1} dx + \frac{3}{2} \cdot 2 \int \sqrt{x^2 + x + 1} + \frac{11}{2} \int \frac{1}{\sqrt{x^2 + x + 1}} dx \\ &= 2 \int \sqrt{\left(x + \frac{1}{2}\right)^2 + \left(\frac{\sqrt{3}}{2}\right)^2} dx + 3 \int \sqrt{x^2 + x + 1} + \frac{11}{2} \int \frac{dx}{\left(x + \frac{1}{2}\right)^2 + \left(\frac{\sqrt{3}}{2}\right)^2} \\ &= \left\{ \frac{x + \frac{1}{2}}{2} \sqrt{x^2 + x + 1} + \frac{3}{8} \ln \left| \left(x + \frac{1}{2}\right) + \sqrt{x^2 + x + 1} \right| \right\} \\ &\quad + 3 \sqrt{x^2 + x + 1} + \frac{11}{2} \ln \left| x + \frac{1}{2} + \sqrt{x^2 + x + 1} \right| + C \\ &= \left( \frac{2x + 1}{2} \right) \sqrt{x^2 + x + 1} + \frac{3}{4} \ln \left| x + \frac{1}{2} + \sqrt{x^2 + x + 1} \right| \\ &\quad + 3 \sqrt{x^2 + x + 1} + \frac{22}{7} \ln \left| x + \frac{1}{2} + \sqrt{x^2 + x + 1} \right| + C \\ &= \frac{2x + 7}{2} \sqrt{x^2 + x + 1} + \frac{25}{4} \ln \left| x + \frac{1}{2} + \sqrt{x^2 + x + 1} \right| + C \end{aligned}$$

$$\begin{aligned} &= x \sqrt{x^2 + x + 1} + \frac{7}{2} \sqrt{x^2 + x + 1} \\ &\quad + \frac{25}{4} \ln \left| x + \frac{1}{2} + \sqrt{x^2 + x + 1} \right| + C \end{aligned}$$

$\therefore \alpha = \frac{7}{2}, \beta = \frac{25}{4}$

Then  $\alpha + 2\beta = \frac{7}{2} + \frac{25}{4} = 16$

23. Let  $H_1: \frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$  and  $H_2: -\frac{x^2}{A^2} + \frac{y^2}{B^2} = 1$  be two hyperbolas having length of latus rectums  $15\sqrt{2}$  and  $12\sqrt{5}$  respectively. Let their eccentricities be  $e_1 = \sqrt{\frac{5}{2}}$  and  $e_2$  respectively. If the product of the lengths of their transverse axes is  $100\sqrt{10}$ , then  $25e_2^2$  is equal to \_\_\_\_\_.

**Answer (55)**

**Sol.**  $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$

$\frac{2b^2}{a} = 15\sqrt{2} \quad \dots(i)$

$\sqrt{1 + \frac{b^2}{a^2}} = \sqrt{\frac{5}{2}} \quad \dots(ii)$

From (i) and (ii)

$a = 5\sqrt{2}$  and  $b^2 = 75$

$\frac{x^2}{A^2} - \frac{y^2}{B^2} = -1$

$\frac{2A^2}{B} = 12\sqrt{5} \quad \dots(iii)$

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---------------------------------------------------------------------------	----------------------------------------------------------------------------------------	--------------------------------------------------------------------------------------

Since, product of transverse axis is  $= 100\sqrt{10}$

$$(2A) \cdot (2B) = 100\sqrt{10} \quad \dots(iv)$$

From (iii) and (iv)

$$A^2 = 150 \text{ and } B = 5\sqrt{5}$$

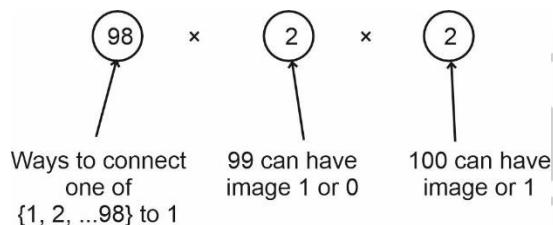
$$e_2 = \sqrt{1 + \frac{A^2}{B^2}} = \sqrt{\frac{11}{5}}$$

$$\therefore 25e_2^2 = 25\left(\frac{11}{5}\right) = 55$$

24. Number of functions  $f: \{1, 2, \dots, 100\} \rightarrow \{0, 1\}$ , that assign 1 to exactly one of the positive integers less than or equal to 98, is equal to \_\_\_\_.

**Answer (392)**

**Sol.**



$$= 98 \times 2 \times 2 = 392$$

25. Let  $y = y(x)$  be the solution of the differential equation

$$2\cos x \frac{dy}{dx} = \sin 2x - 4y \sin x, \quad x \in \left(0, \frac{\pi}{2}\right). \text{ If } y\left(\frac{\pi}{3}\right) = 0$$

, then  $y'\left(\frac{\pi}{4}\right) + y\left(\frac{\pi}{4}\right)$  is equal to \_\_\_\_.

**Answer (01)**

**Sol.**  $2\cos x \frac{dy}{dx} = \sin 2x - 4y \sin x$

$$\frac{dy}{dx} = \frac{2\sin x \cos x}{2\cos x} - \frac{4y \sin x}{2\cos x}$$

$$\frac{dy}{dx} + 2y \tan x = \sin x$$

$$I.F = e^{\int 2 \tan x dx}$$

$$I.F = e^{2 \ln |\sec x|}$$

$$I.F = |\sec x|^2 = \sec^2 x \quad \forall x \in (0, \pi/2)$$

$$y \cdot \sec^2 x = \int \sin x \cdot \sec^2 x dx$$

$$y \cdot \sec^2 x = \int \frac{\sin x}{\cos^2 x} dx$$

$$\text{Let, } \cos x = t$$

$$-\sin x dx = dt$$

$$y \cdot \sec^2 x = -\int \frac{1}{t^2} dt$$

$$y \cdot \sec^2 x = \frac{1}{t} + C$$

$$y \cdot \sec^2 x = \sec x + C$$

$$y\left(\frac{\pi}{3}\right) = 0$$

$$C = -2$$

$$\therefore y = \cos x - 2\cos^2 x$$

$$y'(x) = -\sin x + 2\sin 2x$$

$$y'\left(\frac{\pi}{4}\right) = \frac{1}{\sqrt{2}} + 2$$

$$y'\left(\frac{\pi}{4}\right) = \frac{1}{\sqrt{2}} - 1$$

$$\therefore y'\left(\frac{\pi}{4}\right) + y\left(\frac{\pi}{4}\right) = 1$$



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**PHYSICS**

**SECTION - A**

**Multiple Choice Questions:** This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

**Choose the correct answer :**

26. The temperature of a body in air falls from  $40^{\circ}\text{C}$  to  $24^{\circ}\text{C}$  in 4 minutes. The temperature of the air is  $16^{\circ}\text{C}$ . The temperature of the body in the next 4 minutes will be :

- (1)  $\frac{14}{3}^{\circ}\text{C}$  (2)  $\frac{28}{3}^{\circ}\text{C}$   
(3)  $\frac{42}{3}^{\circ}\text{C}$  (4)  $\frac{56}{3}^{\circ}\text{C}$

**Answer (4)**

**Sol.**  $\Delta T = T_2 - T_1 = 16^{\circ}\text{C}$

And  $T_0 = 16^{\circ}\text{C}$

$$\frac{\Delta T}{t_1} = -k(32 - 16) \quad \dots(i)$$

$$\frac{(24 - T_3)}{4} = -k\left(\frac{24 + T_3}{2} - 16\right) \quad \dots(ii)$$

$$\frac{16}{4} = -k(16)$$

$$\Rightarrow \frac{(24 - T_3)}{4} = -k\left(12 + \frac{T_3}{2} - 16\right)$$

$$\Rightarrow \frac{16}{24 - T_3} = \frac{16}{\frac{T_3}{2} - 4}$$

$$\Rightarrow \frac{T_3}{2} - 4 = 24 - T_3$$

$$\Rightarrow \frac{3T_3}{2} = 28$$

$$\Rightarrow T_3 = \frac{56}{3}^{\circ}\text{C}$$

27. A solid sphere is rolling without slipping on a horizontal plane. The ratio of the linear kinetic energy of the centre of mass of the sphere and rotational kinetic energy is :

- (1)  $\frac{5}{2}$  (2)  $\frac{4}{3}$   
(3)  $\frac{3}{4}$  (4)  $\frac{2}{5}$

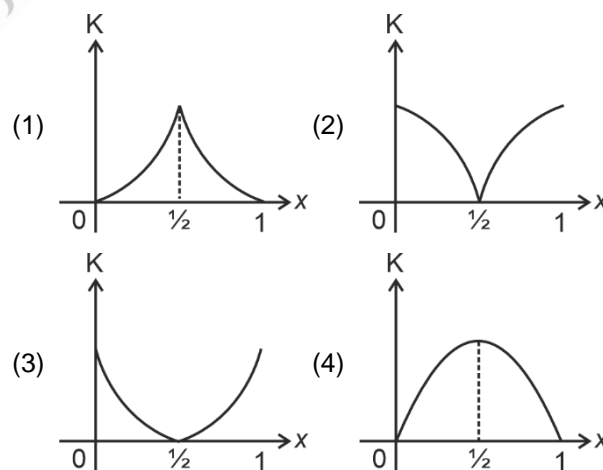
**Answer (1)**

**Sol.**  $\text{KE}_{(T)} = \frac{1}{2}mv^2$

$$\text{KE}_{(R)} = \frac{1}{2} \cdot \frac{2}{5}mR^2 \cdot \frac{v^2}{R^2} = \frac{1}{2}mv^2\left(\frac{2}{5}\right)$$

$$\text{So, } \frac{\text{KE}_{(T)}}{\text{KE}_{(R)}} = \frac{5}{2}$$

28. A particle oscillates along the x-axis according to the law,  $x(t) = x_0 \sin^2\left(\frac{t}{2}\right)$  where  $x_0 = 1$  m. The kinetic energy (K) of the particle as a function of x is correctly represented by the graph



**Answer (4)**

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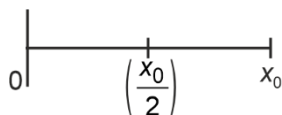
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**100** Sanvi Jain  
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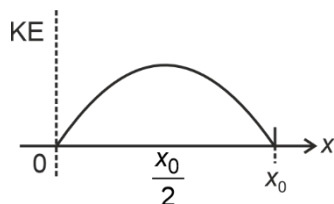
**100** M Sai Divya Teja Reddy  
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**100** Rishi Shekher Shukla  
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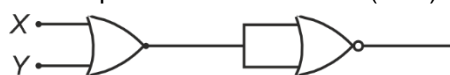
**Sol.**  $x(t) = x_0 \sin^2\left(\frac{t}{2}\right) = \frac{x_0}{2}(1 - \cos t)$



Clearly  $\frac{x_0}{2}$  is mean position.



29. The output of the circuit is low (zero) for :

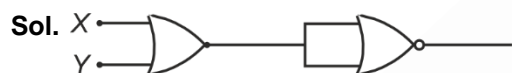


- (A)  $X = 0, Y = 0$  (B)  $X = 0, Y = 1$   
 (C)  $X = 1, Y = 0$  (D)  $X = 1, Y = 1$

Choose the **correct** answer from the options given below :

- (1) (A), (B) and (D) only (2) (A), (C) and (D) only  
 (3) (A), (B) and (C) only (4) (B), (C) and (D) only

**Answer (4)**



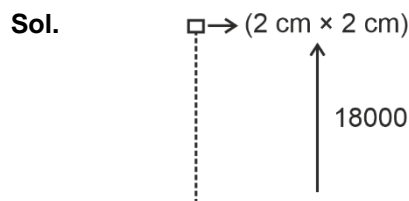
Clearly  $\overline{x+y}$  = output

So, when either of  $x$  or  $y$  is 1 then output will be zero.

30. A photograph of a landscape is captured by a drone camera at a height of 18 km. The size of the camera film is 2 cm x 2 cm and the area of the landscape photographed is 400 km<sup>2</sup>. The focal length of the lens in the drone camera is :

- (1) 0.9 cm (2) 2.5 cm  
 (3) 1.8 cm (4) 2.8 cm

**Answer (3)**



Linear size of image = 2 cm

Linear size of object =  $20 \times 10^5$  cm

$$m = \frac{2}{20 \times 10^5} = 10^{-6}$$

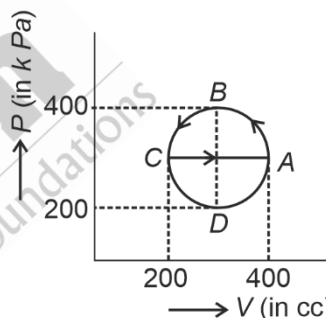
$$\text{So, } v = \frac{u}{10^6}$$

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f} \Rightarrow \frac{10^6}{u} + \frac{1}{u} = \frac{1}{f}$$

$$\Rightarrow \frac{(1 + 10^6)}{u} = \frac{1}{f} \Rightarrow f \approx \left(\frac{u}{10^6}\right)$$

$$\Rightarrow f = \frac{18000 \times 100}{10^6} \text{ cm} = 1.8 \text{ cm}$$

31. The magnitude of heat exchanged by a system for the given cyclic process ABCA (as shown in figure) is (in SI unit)



- (1)  $5\pi$   
 (2)  $40\pi$   
 (3)  $10\pi$   
 (4) Zero

**Answer (1)**

**Sol.** For cyclic process

$$\Delta u = \Delta Q - \Delta w = 0$$

$$\Rightarrow |\Delta Q| = |\Delta w| = \frac{\pi}{2} \times 100 \times 10^{-6} \times 100 \times 10^3$$

$$\Rightarrow |\Delta Q| = 5\pi$$

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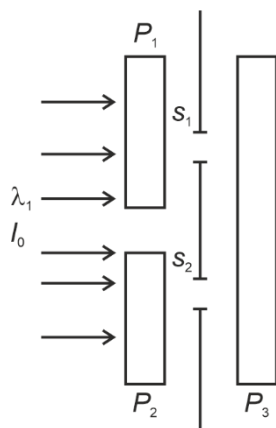
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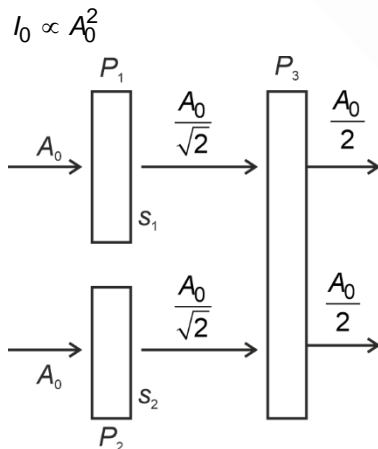
32. In a Young's double slit experiment, three polarizers are kept as shown in the figure. The transmission axes of  $P_1$  and  $P_2$  are orthogonal to each other. The polarizer  $P_3$  covers both the slits with its transmission axis at  $45^\circ$  to those of  $P_1$  and  $P_2$ . An unpolarized light of wavelength  $\lambda$  and intensity  $I_0$ , is incident on  $P_1$  and  $P_2$ . The intensity at a point after  $P_3$  where the path difference between the light waves from  $s_1$  and  $s_2$  is  $\frac{\lambda}{3}$ , is



- (1)  $\frac{I_0}{3}$  (2)  $\frac{I_0}{4}$   
(3)  $\frac{I_0}{2}$  (4)  $I_0$

**Answer (2)**

**Sol.** Incident amplitude is  $A_0$  then



Now, path difference is  $\frac{\lambda}{3}$  so phase difference is  $\frac{2\pi}{3}$

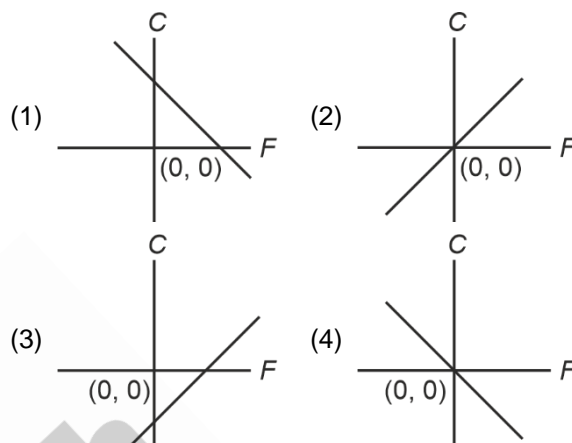
$$A^2 = A_1^2 + A_2^2 + 2A_1A_2 \cos \theta$$

$$= \frac{A_0^2}{4} + \frac{A_0^2}{4} + 2 \frac{A_0^2}{4} \cos \left( \frac{2\pi}{3} \right)$$

$$\Rightarrow A^2 = \frac{A_0^2}{4}$$

$$\text{so, } I = \frac{I_0}{4}$$

33. Which of the following figure represents the relation between Celsius and Fahrenheit temperatures?



**Answer (3)**

**Sol.** We know  $F = 32 + \left( \frac{180}{100} \right) C$

$$\Rightarrow \frac{180}{100} C = F - 32$$

$$\Rightarrow C = \left( \frac{100}{180} \right) F - \frac{160}{9}$$

Clearly slope is +ve and intercept is -ve

34. Given below are two statements. One is labelled as **Assertion (A)** and the other is labelled as **Reason (R)**.

**Assertion (A) :** A electron in a certain region of uniform magnetic field is moving with constant velocity in a straight line path.

**Reason (R) :** The magnetic field in that region is along the direction of velocity of the electron.

In the light of the above statements, choose the correct answer from the options given below

- (1) (A) is false but (R) is true  
(2) Both (A) and (R) are true and (R) is the correct explanation of (A)  
(3) Both (A) and (R) are true but (R) is NOT the correct explanation of (A)  
(4) (A) is true but (R) is false

**Answer (2)**

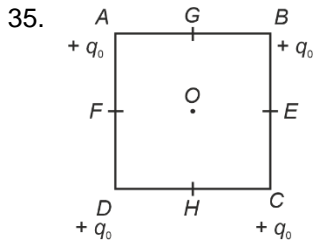
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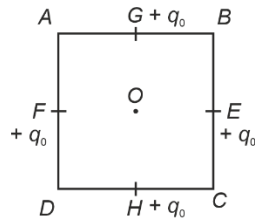
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**Sol.** If the electron's velocity is along the direction of magnetic field then magnetic force on electron is zero and it will not accelerate.



Configuration (1)



Configuration (2)

In the first configuration (1) as shown in the figure, four identical charges ( $q_0$ ) are kept at the corners A, B, C and D of square of side length 'a'. In the second configuration (2), the same charges are shifted to mid points G, E, H and F, of the square.

If  $K = \frac{1}{4\pi\epsilon_0}$ , the difference between the potential energies of configuration (2) and (1) is given by

- (1)  $\frac{Kq_0^2}{a}(3\sqrt{2}-2)$       (2)  $\frac{Kq_0^2}{a}(4\sqrt{2}-2)$   
(3)  $\frac{Kq_0^2}{a}(4-2\sqrt{2})$       (4)  $\frac{Kq_0^2}{a}(3-\sqrt{2})$

**Answer (1)**

**Sol.**  $u_1 = \left( 2 \frac{Kq_0}{a} + \frac{Kq_0}{\sqrt{2}a} \right) q_0 \times 2$

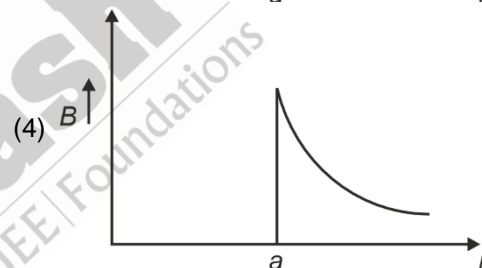
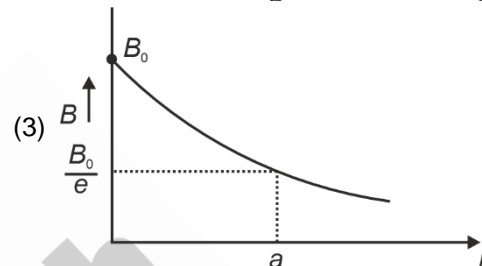
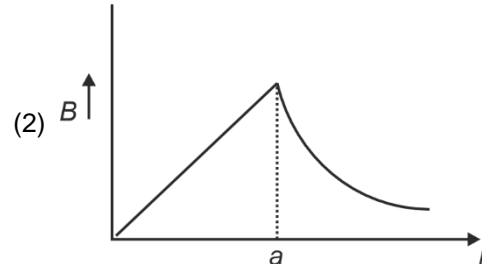
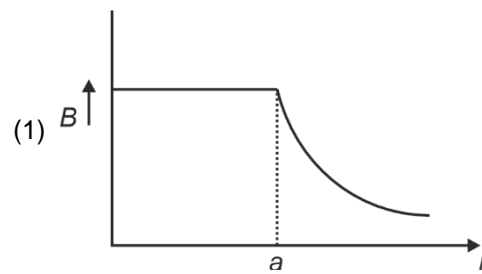
$u_2 = \left( 2 \frac{Kq_0\sqrt{2}}{a} + \frac{Kq_0}{a} \right) q_0 \times 2$

So,  $\Delta u = u_2 - u_1 = 2q_0 \frac{Kq_0}{a} \left[ 2\sqrt{2} + 1 - 2 - \frac{1}{\sqrt{2}} \right]$

$\Rightarrow \Delta u = \frac{2q_0^2}{4\pi\epsilon_0 a} \left[ \frac{4 - \sqrt{2} - 1}{\sqrt{2}} \right] = \frac{2q_0^2}{4\pi\epsilon_0 a} \frac{(3 - \sqrt{2})}{\sqrt{2}}$

$\Rightarrow \Delta u = \frac{2Kq_0^2}{a} \left[ \frac{3 - \sqrt{2}}{\sqrt{2}} \right] = \frac{Kq_0^2}{a} (3\sqrt{2} - 2)$

36. A long straight wire of a circular cross-section with radius 'a' carries a steady current  $I$ . The current  $I$  is uniformly distributed across this cross-section. The plot of magnitude of magnetic field  $B$  with distance  $r$  from the centre of the wire is given by

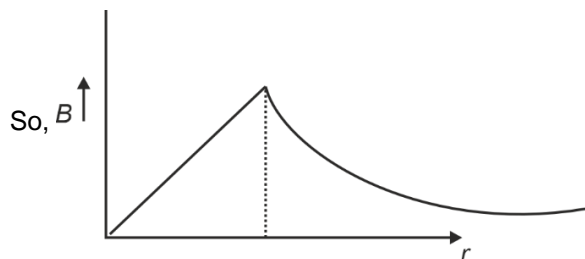


**Answer (2)**

**Sol.** We know inside the wire

$B = \frac{\mu_0 I}{2\pi R^2} \cdot r \quad (0 < r < R)$

And  $B = \frac{\mu_0 I}{2\pi r} \quad \text{for } (R < r)$



Option (2) is correct answer.

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37 Young's double slit interference apparatus is immersed in a liquid of refractive index 1.44. It has slit separation of 1.5 mm. The slits are illuminated by a parallel beam of light whose wavelength in air is 690 nm. The fringe-width on a screen placed behind the plane of slits at a distance of 0.72 m, will be :

- (1) 0.63 mm (2) 0.23 mm  
(3) 0.33 mm (4) 0.46 mm

**Answer (2)**

**Sol.**  $\Delta W = \frac{\lambda D}{d \cdot \mu} = \frac{690 \times 10^{-9} \times 0.72}{1.5 \times 10^{-3} \times 1.44}$

$\Rightarrow \Delta W = 2.3 \times 10^{-4} \text{ m} = 0.23 \text{ mm}$

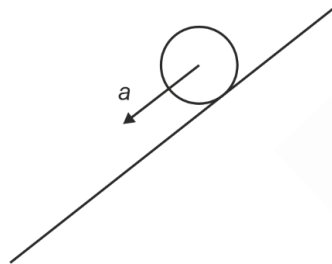
Option (2) is correct answer.

38. A solid sphere and a hollow sphere of the same mass and of same radius are rolled on an inclined plane. Let the time taken to reach the bottom by the solid sphere and the hollow sphere be  $t_1$  and  $t_2$ , respectively, then

- (1)  $t_1 < t_2$  (2)  $t_1 = 2t_2$   
(3)  $t_1 > t_2$  (4)  $t_1 = t_2$

**Answer (1)**

**Sol.**



$mgR \sin \theta = I \frac{a}{R} \Rightarrow a = \frac{mgR^2 \sin \theta}{I}$

For solid sphere  $I_s = \frac{7}{5} mR^2$

So,  $a_s = \frac{mgR^2 \sin \theta}{7/5 mR^2} = \frac{5g}{7} \sin \theta$

For  $a_H = \frac{mgR^2 \sin \theta}{\frac{5}{3} mR^2} = \frac{3}{5} g \sin \theta$

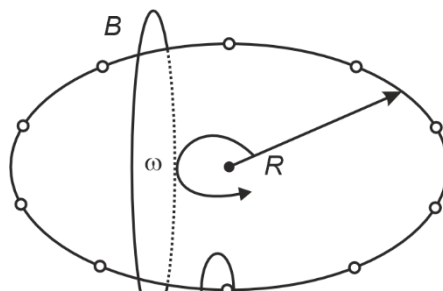
So,  $\frac{1}{2} a_s t_1^2 = \frac{1}{2} a_H t_2^2$

$\Rightarrow \left( \frac{t_1}{t_2} \right)^2 = \frac{3 \times 7}{5 \times 5} = \frac{21}{25}$

Clearly  $t_2 > t_1$

Option (1) is correct answer.

39.



$N$  equally spaced charges each of value  $q$ , are placed on a circle of radius  $R$ . The circle rotates about its axis with an angular velocity  $\omega$  as shown in the figure. A bigger Amperian loop  $B$  encloses the whole circle where as a smaller Amperian loop  $A$  encloses a small segment. The different enclosed currents,  $I_A - I_B$ , for the given Amperian loops is

- (1)  $\frac{N^2}{2\pi} q\omega$  (2)  $\frac{N}{2\pi} q\omega$   
(3)  $\frac{2\pi}{N} q\omega$  (4)  $\frac{N}{\pi} q\omega$

**Answer (2)**

**Sol.**  $I = \frac{Nq\omega}{2\pi}$

Now for bigger Amperian loop (loop  $B$ )

$I_{B(\text{enclosed})} = 0$

And for smaller Amperian loop (loop  $A$ )

$|I_{A(\text{enclosed})}| = I = \frac{Nq\omega}{2\pi}$

So,  $|I_A - I_B| = \frac{Nq\omega}{2\pi}$

Option (2) is correct answer.

40. A small uncharged conducting sphere is placed in contact with an identical sphere but having  $4 \times 10^{-8} \text{ C}$  charge and then removed to a distance such that the force of repulsion between them is  $9 \times 10^{-3} \text{ N}$ . The distance between them is (Take

$\frac{1}{4\pi\epsilon_0}$  as  $9 \times 10^9$  in SI units)

- (1) 3 cm (2) 2 cm  
(3) 4 cm (4) 1 cm

**Answer (2)**

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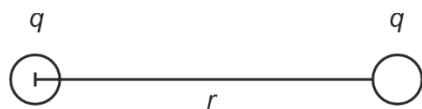
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**Sol.** Charges will be shared equally

$$q = \frac{Q}{2}$$



$$F_{(\text{rep})} = \frac{kq^2}{r^2} = \frac{1}{4\pi\epsilon_0} \frac{q^2}{r^2} = 9 \times 10^{-3}$$

$$\Rightarrow \frac{9 \times 10^9 \times 4 \times 10^{-16}}{r^2} = 9 \times 10^{-3}$$

$$\Rightarrow r^2 = \frac{4 \times 10^{-7}}{10^{-3}} = 4 \times 10^{-4}$$

$$\Rightarrow r = 2 \times 10^{-2} \text{ m} = 2 \text{ cm}$$

Option (2) is correct answer.

41. The energy  $E$  and momentum  $p$  of a moving body of mass  $m$  are related by some equation. Given that  $c$  represents the speed of light, identify the correct equation

(1)  $E^2 = p^2 c^2 + m^2 c^4$

(2)  $E^2 = p^2 c^2 + m^2 c^2$

(3)  $E^2 = pc^2 + m^2 c^4$

(4)  $E^2 = pc^2 + m^2 c^2$

**Answer (1)**

**Sol.** We need to check the dimensions only.

With momentum the dimension

$$E^2 = p^2 c^2$$

And with mass  $E^2 = m^2 c^4$

So  $E^2 = p^2 c^2 + m^2 c^4$  (dimensionally)

42. Given below are two statements. One is labelled as Assertion (A) and the other is labelled as Reason (R).

**Assertion (A):** In an insulated container, a gas is adiabatically shrunk to half of its initial volume. The temperature of the gas decreases.

**Reason (R):** Free expansion of an ideal gas is an irreversible and an adiabatic process.

In the light of the above statements, choose the correct answer from the options given below:

- (1) Both (A) and (R) are true but (R) is NOT the correct explanation of (A)
- (2) (A) is true but (R) is false
- (3) (A) is false but (R) is true
- (4) Both (A) and (R) are true and (R) is the correct explanation of (A)

**Answer (3)**

**Sol.** If the container is insulated then temperature is expected to increase in adiabatic compression. So (A) is wrong.

And free expansion is irreversible and adiabatic process. So (R) is correct.

43. In photoelectric effect, the stopping potential ( $V_0$ ) v/s frequency ( $\nu$ ) curve is plotted. ( $h$  is the Planck's constant and  $\phi_0$  is work function of metal)

(A)  $V_0$  v/s  $\nu$  is linear

(B) The slope of  $V_0$  v/s  $\nu$  curve =  $\frac{\phi_0}{h}$

(C)  $h$  constant is related to the slope of  $V_0$  v/s  $\nu$  line


(D) The value of electric charge of electron is not required to determine  $h$  using the  $V_0$  v/s  $\nu$  curve.

(E) The work function can be estimated without knowing the value of  $h$ .


Choose the correct answer from the options given below :

- (1) (A), (B) and (C) only
- (2) (D) and (E) only
- (3) (A), (C) and (E) only
- (4) (C) and (E) only

**Answer (3)**




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**Sol.** We know  $h\nu - \phi_0 = eV_0$

$$\Rightarrow V_0 = \left(\frac{h}{e}\right)\nu - \frac{\phi_0}{e}$$

So slope is constant =  $\frac{h}{e}$

and intercept is  $-ve \left(\frac{\phi_0}{e}\right)$

$\Rightarrow$  Option (A) is correct, option (B) is wrong.

$\Rightarrow$  Option (C) is correct, option (D) is wrong.

$\Rightarrow$  Option (E) is correct.

(A), (C) & (E) are correct.

44. Arrange the following in the ascending order of wavelength ( $\lambda$ ):

(A) Microwaves ( $\lambda_1$ )

(B) Ultraviolet rays ( $\lambda_2$ )

(C) Infrared rays ( $\lambda_3$ )

(D) X-rays ( $\lambda_4$ )

Choose the most appropriate answer from the options given below :

(1)  $\lambda_3 < \lambda_4 < \lambda_2 < \lambda_1$  (2)  $\lambda_4 < \lambda_3 < \lambda_1 < \lambda_2$

(3)  $\lambda_4 < \lambda_3 < \lambda_2 < \lambda_1$  (4)  $\lambda_4 < \lambda_2 < \lambda_3 < \lambda_1$

**Answer (4)**

**Sol.** X-ray ( $\lambda_4$ ) is shortest wavelength

then ultraviolet is ( $\lambda_2$ ) is longer than X-ray.

then infrared ( $\lambda_3$ ) is longer than ultraviolet

then microwaves ( $\lambda_1$ ) is longer than infrared

So  $\lambda_4 < \lambda_2 < \lambda_3 < \lambda_1$

45. The position vector of a moving body at any instant of time is given as  $\vec{r} = (5t^2\hat{i} - 5t\hat{j})$  m. The magnitude and direction of velocity at  $t = 2$  s is,

(1)  $5\sqrt{17}$  m/s, making an angle of  $\tan^{-1} 4$  with  $-ve$  Y axis

(2)  $5\sqrt{17}$  m/s, making an angle of  $\tan^{-1} 4$  with  $+ve$  X axis

(3)  $5\sqrt{15}$  m/s, making an angle of  $\tan^{-1} 4$  with  $+ve$  X axis

(4)  $5\sqrt{15}$  m/s, making an angle of  $\tan^{-1} 4$  with  $-ve$  Y axis

**Answer (1)**

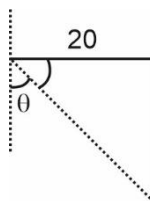
**Sol.**  $\vec{r} = (5t^2\hat{i} - 5t\hat{j})$

$$\text{So } \frac{d\vec{r}}{dt} = \vec{v} = (10t\hat{i} - 5\hat{j})$$

At ( $t = 2$  second)

$$\vec{v}(t = 2) = (20\hat{i} - 5\hat{j})$$

$$|\vec{v}| = 5\sqrt{16+1} = 5\sqrt{17} \text{ m/s}$$

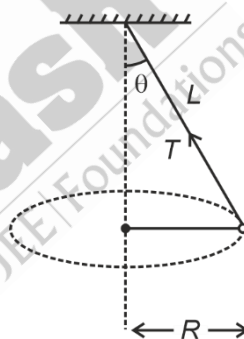


$$\text{With } -ve \text{ y-axis } \tan\theta = \frac{20}{5} = 4$$

### SECTION - B

**Numerical Value Type Questions:** This section contains 5 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

46.



A string of length  $L$  is fixed at one end and carries a mass of  $M$  at the other end. The mass makes  $\left(\frac{3}{\pi}\right)$

rotations per second about the vertical axis passing through end of the string as shown. The tension in the string is \_\_\_\_\_ ML.

**Answer (36)**

$$\text{Sol. } \omega = \frac{3}{\pi} \times 2\pi = 6 \text{ rad/s}$$

$$R = L\sin\theta$$

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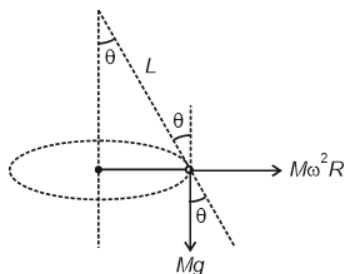
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$$\text{and } T = M\sqrt{g^2 + \omega^4 R^2}$$

$$\text{Also, } T \sin \theta = M\omega^2 \cdot L \sin \theta$$

$$\Rightarrow T = M(36) L$$

$$\Rightarrow T = 36 ML$$

47. The ratio of the power of a light source  $S_1$  to that the light source  $S_2$  is 2.  $S_1$  is emitting  $2 \times 10^{15}$  photons per second at 600 nm. If the wavelength of the source  $S_2$  is 300 nm, then the number of photons per second emitted by  $S_2$  is \_\_\_\_\_  $\times 10^{14}$ .

**Answer (5)**

$$\text{Sol. } p_1 = \frac{2 \times 10^{15} \times E_1}{1 \text{ sec}} = \frac{2 \times 10^{15} \times hc}{\lambda_1}$$

$$p_2 = \frac{N \times hc}{\lambda_2}$$

$$\frac{p_1}{p_2} = \frac{2 \times 10^{15} \times hc \times 300}{600 \times N \times hc} = 2$$

$$\Rightarrow N = \frac{10^{15}}{2} = 5 \times 10^{14} \text{ per second}$$

48. The increase in pressure required to decrease the volume of a water sample by 0.2% is  $P \times 10^5 \text{ Nm}^{-2}$ . Bulk modulus of water is  $2.15 \times 10^9 \text{ Nm}^{-2}$ . The value of  $P$  is \_\_\_\_\_.

**Answer (43)**

$$\text{Sol. We know } \frac{\Delta P}{\Delta V/V} = -\beta$$

$$\Rightarrow \Delta P = -\beta \cdot \frac{\Delta V}{V}$$

$$\Rightarrow |\Delta P| = 2.15 \times 10^9 \times \frac{2}{1000} = 4.3 \times 10^6 \text{ N/m}^2$$

$$\Rightarrow \Delta P = 43 \times 10^5 \text{ N/m}^2$$

49. Acceleration due to gravity on the surface of earth is 'g'. If the diameter of earth is reduced to one third of its original value and mass remains unchanged, then the acceleration due to gravity on the surface of the earth is \_\_\_\_\_ g.

**Answer (9)**

$$\text{Sol. } g = \frac{GM}{R^2}$$

$$\text{Now, } g' = \frac{GM}{\left(\frac{R}{3}\right)^2} = \frac{9GM}{R^2} = 9g$$

50. A tightly wound long solenoid carries a current of 1.5 A. An electron is executing uniform circular motion inside the solenoid with a time period of 75 ns. The number of turns per metre in the solenoid is \_\_\_\_\_.

[Take mass of electron  $m_e = 9 \times 10^{-31} \text{ kg}$ , charge of electron  $|q_e| = 1.6 \times 10^{-19} \text{ C}$ ,  $\mu_0 = 4\pi \times 10^{-7} \frac{\text{N}}{\text{A}^2}$ ,  $1 \text{ ns} = 10^{-9} \text{ s}$ ]

**Answer (250)**

**Sol.** We know,

$$\beta = \mu_0 \eta I \text{ and } T = \frac{2\pi m}{e\beta}$$

$$\Rightarrow \frac{2\pi m}{eT} = \mu_0 \eta I$$

$$\Rightarrow \eta = \frac{2\pi m}{eT\mu_0 I}$$

$$= \frac{2\pi \times 9 \times 10^{-31}}{1.6 \times 10^{-19} \times 75 \times 10^{-9} \times 4\pi \times 10^{-7} \times 1.5}$$

$$\Rightarrow \eta = \frac{9 \times 10^{-31}}{1.6 \times 10^{-19} \times 75 \times 10^{-9} \times 2 \times 10^{-7} \times 1.5}$$

$$\Rightarrow \eta = \frac{9 \times 10^4}{360} = 250 \text{ per meter}$$



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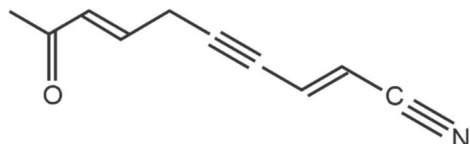
## CHEMISTRY

### SECTION - A

**Multiple Choice Questions:** This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

**Choose the correct answer :**

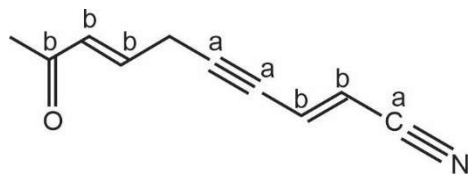
51. In the given structure, number of  $sp$  and  $sp^2$  hybridized carbon atoms present respectively are:



- (1) 3 and 6                      (2) 4 and 6  
(3) 4 and 5                      (4) 3 and 5

**Answer (4)**

**Sol.** The given structure is



Number of  $sp$  hybridized C-atoms(a) = 3

Number of  $sp^2$  hybridized C-atoms(b) = 5

52. Identify correct statement/s:

- (A)  $-\text{OCH}_3$  and  $-\text{NHCOCH}_3$  are activating group.  
(B)  $-\text{CN}$  and  $-\text{OH}$  are meta directing group.  
(C)  $-\text{CN}$  and  $-\text{SO}_3\text{H}$  are meta directing group.  
(D) Activating groups act as ortho- and para directing groups.  
(E) Halides are activating groups.

Choose the correct answer from the options given below:

- (1) (A), (C) and (D) only  
(2) (A) and (C) only  
(3) (A) only  
(4) (A), (B) and (E) only

**Answer (1)**

**Sol.**  $-\text{OCH}_3$ ,  $\text{NHCOCH}_3$  and  $-\text{OH}$  are activating groups because the atom directly bonded to benzene ring activates the ring by +R effect using its lone pair of electrons. Activating groups are ortho- and para directing groups.

$-\text{CN}$  and  $-\text{SO}_3\text{H}$  are deactivating groups because the atom directly bonded to benzene is bonded to more electronegative atom through multiple bonds and they are meta directing groups due to  $-\text{R}$  effect. Halides are deactivating groups due to  $-\text{I}$  effect.

Correct statements are (A), (C) and (D) only.

53. The conditions and consequence that favours the  $t_{2g}^3 e_g^1$  configuration in a metal complex are:

- (1) strong field ligand, high spin complex  
(2) weak field ligand, high spin complex  
(3) weak field ligand, low spin complex  
(4) strong field ligand, low spin complex

**Answer (2)**

**Sol.** The conditions and consequence that favour  $t_{2g}^3 e_g^1$  configuration in a metal complex are

- (i) weak field ligand, and  
(ii) high spin complex

For weak field ligands, splitting energy ( $\Delta_0$ ) is lower than pairing energy (P). As a result distribution of electrons for  $3d^4$  will be  $t_{2g}^3 e_g^1$ . It results in high spin complex due to maximum number of unpaired electrons.

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54. Given below are two statements:

**Statement (I):** The first ionization energy of Pb is greater than that of Sn.

**Statement (II):** The first ionization energy of Ge is greater than that of Si.

In the light of the above statements, choose the correct answer from the options given below:

- (1) **Statement I** is false but **Statement II** is true
- (2) **Statement I** is true but **Statement II** is false
- (3) Both **Statement I** and **Statement II** are false
- (4) Both **Statement I** and **Statement II** are true

**Answer (2)**

**Sol.** First ionization energy of Lead =  $715 \text{ kJ mol}^{-1}$

First ionization energy of Tin =  $708 \text{ kJ mol}^{-1}$

( $IE_1$ ) of Lead is greater than that of Tin due to ineffective shielding of d- and f-electrons.

Therefore **Statement-I** is true.

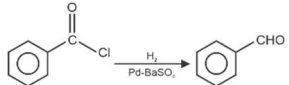
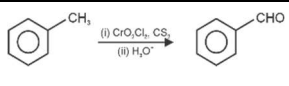
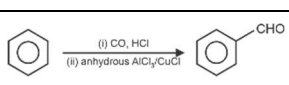
First ionization energy of Germanium =  $761 \text{ kJ mol}^{-1}$

First ionization energy of Silicon =  $786 \text{ kJ mol}^{-1}$

( $IE_1$ ) of Germanium is lower than that of Silicon as the effect of higher atomic radius of Ge outweighs the increase in nuclear charge from Si to Ge and effective shielding of inner electrons.

Therefore **Statement-II** is false.

55. Match **List-I** with **List-II**.

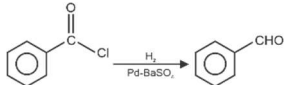
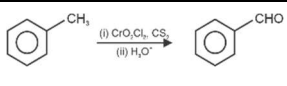
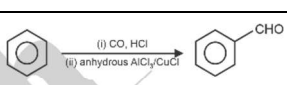
	List-I		List-II
(A)	$\text{RCN} \xrightarrow[\text{(ii) } \text{H}_3\text{O}^+]{\text{(i) } \text{SnCl}_2, \text{HCl}} \text{RCHO}$	(I)	Etard reaction
(B)		(II)	Gatterman-Koch reaction
(C)		(III)	Rosenmund reduction
(D)		(IV)	Stephen reaction

Choose the **correct** answer from the options given below:

- (1) (A)-(I), (B)-(III), (C)-(II), (D)-(IV)
- (2) (A)-(III), (B)-(IV), (C)-(II), (D)-(I)
- (3) (A)-(IV), (B)-(III), (C)-(I), (D)-(II)
- (4) (A)-(III), (B)-(IV), (C)-(I), (D)-(II)

**Answer (3)**

**Sol.**

	List-I		List-II
(A)	$\text{RCN} \xrightarrow[\text{(ii) } \text{H}_3\text{O}^+]{\text{(i) } \text{SnCl}_2, \text{HCl}} \text{RCHO}$	(IV)	Stephen reaction
(B)		(III)	Rosenmund reduction
(C)		(I)	Etard reaction
(D)		(II)	Gatterman-Koch reaction

Correct match: (A)-(IV), (B)-(III), (C)-(I), (D)-(II)

56. The successive 5 ionisation energies of an element are 800, 2427, 3658, 25024 and 32824 kJ/mol, respectively. By using the above values predict the group in which the above element is present:

- (1) Group 14
- (2) Group 4
- (3) Group 13
- (4) Group 2

**Answer (3)**

**Sol.** The successive 5 ionisation energies of an element are 800, 2427, 3658, 25024 and 32824 kJ/mol, respectively.

$$\frac{IE_2}{IE_1} = \frac{2427}{800} = 3.03$$

$$\frac{IE_3}{IE_2} = \frac{3658}{2427} = 1.51$$

$$\frac{IE_4}{IE_3} = \frac{25024}{3658} = 6.84$$



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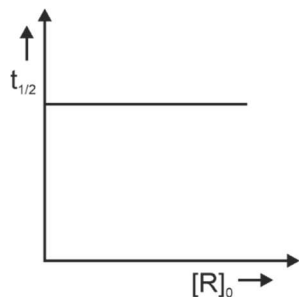
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$$\frac{IE_5}{IE_4} = \frac{32824}{25024} = 1.31$$

Since  $(IE_4 / IE_3)$  value is maximum, the element belongs to group 13.

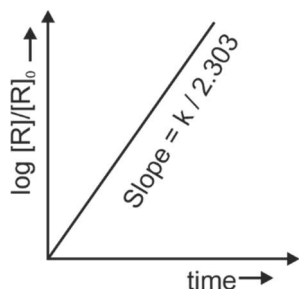
57. Given below are two statements:

**Statement (I):**



is valid for first order reaction.

**Statement (II):**



is valid for first order reaction.

In the light of the above statements, choose the correct answer from the options given below:

- (1) **Statement I** is true but **Statement II** is false
- (2) Both **Statement I** and **Statement II** are false
- (3) **Statement I** is false but **Statement II** is true
- (4) Both **Statement I** and **Statement II** are true

**Answer (1)**

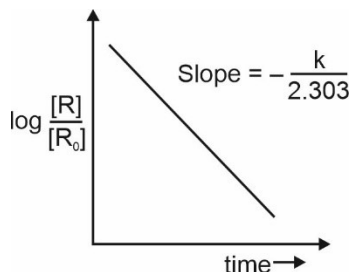
**Sol.** Half life ( $t_{1/2}$ ) of a first order reaction does not depend on initial concentration of the reactant  $[R]_0$ . Therefore **Statement I** is true. Rate constant ( $k$ ) of a first order reaction is given by

$$k = \frac{2.303}{t} \log \frac{[R]_0}{[R]}$$

$$\log \frac{[R]}{[R]_0} = -\left(\frac{k}{2.303}\right)t$$

Plot of  $\log \frac{[R]}{[R]_0}$  versus time is linear having

$$\text{slope} = -\frac{k}{2.303}$$



$\therefore$  **Statement II** is false.

58. Given below are two statements:

**Statement (I):** Experimentally determined oxygen-oxygen bond lengths in the  $O_3$  are found to be same and the bond length is greater than that of a  $O=O$  (double bond) but less than that of a single ( $O-O$ ) bond.

**Statement (II):** The strong lone pair-lone pair repulsion between oxygen atoms is solely responsible for the fact that the bond length in ozone is smaller than that of a double bond ( $O=O$ ) but more than that of a single bond ( $O-O$ ).

In the light of the above statements, choose the correct answer from the options given below :

- (1) **Statement I** is false but **Statement II** is true
- (2) Both **Statement I** and **Statement II** are true
- (3) **Statement I** is true but **Statement II** is false
- (4) Both **Statement I** and **Statement II** are false

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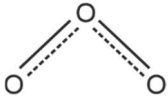
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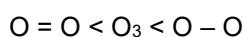


**Answer (3)****Sol.**

Bond	(O – O) Bond order
(O – O)	1.0
	1.5
O = O	2.0

$$\text{Bond length} \propto \frac{1}{\text{Bond order}}$$

Order of O – O bond length

 $\therefore$  **Statement I** is true.

Lone pair-lone pair repulsion between O-atoms is not solely responsible for the correct order of O–O bond length. Bond order also should be considered.

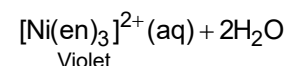
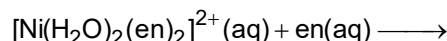
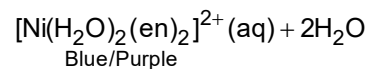
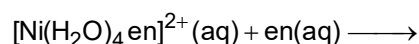
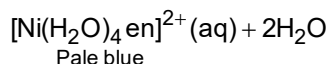
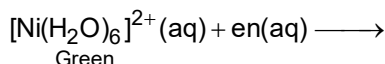
 $\therefore$  **Statement II** is false.

59. When Ethane-1,2-diamine is added progressively to an aqueous solution of Nickel (II) chloride, the sequence of colour change observed will be:

- (1) Green  $\rightarrow$  Pale blue  $\rightarrow$  Blue  $\rightarrow$  Violet
- (2) Pale blue  $\rightarrow$  Blue  $\rightarrow$  Violet  $\rightarrow$  Green
- (3) Pale blue  $\rightarrow$  Blue  $\rightarrow$  Green  $\rightarrow$  Violet
- (4) Violet  $\rightarrow$  Blue  $\rightarrow$  Pale blue  $\rightarrow$  Green

**Answer (1)**

**Sol.** If ethane-1,2-diamine (en) is added progressively to an aqueous solution of  $\text{NiCl}_2$  in the molar ratios en : Ni 1 : 1, 2 : 1 and 3 : 1, the following series of reactions and their associated colour changes occur. [Ref : NCERT (XII) Part-1, p 260]

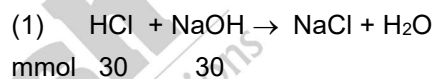


60. Which of the following mixing of 1 M base and 1 M acid leads to the largest increase in temperature?

- (1) 30 mL HCl and 30 mL NaOH
- (2) 30 mL  $\text{CH}_3\text{COOH}$  and 30 mL NaOH
- (3) 45 mL  $\text{CH}_3\text{COOH}$  and 25 mL NaOH
- (4) 50 mL HCl and 20 mL NaOH

**Answer (1)**

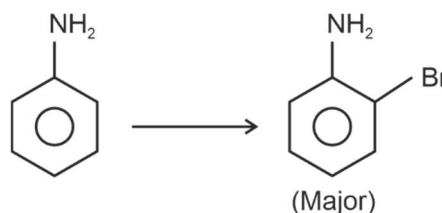
**Sol.** The rise in temperature of neutralization reaction will be maximum for maximum number of moles of strong acid and strong base neutralized and lower volume of final solution.



Final volume of solution = 60 mL

Option (2) and (3) have weak acids and in option (4) only 20 mmol of HCl will be neutralized with 70 mL final volume.

61. For reaction



The correct order of set of reagents for the above conversion is :

- (1)  $\text{Br}_2$  |  $\text{FeBr}_3$ ,  $\text{H}_2\text{O}(\Delta)$ , NaOH
- (2)  $\text{Ac}_2\text{O}$ ,  $\text{Br}_2$ ,  $\text{H}_2\text{O}(\Delta)$ , NaOH
- (3)  $\text{H}_2\text{SO}_4$ ,  $\text{Ac}_2\text{O}$ ,  $\text{Br}_2$ ,  $\text{H}_2\text{O}(\Delta)$ , NaOH
- (4)  $\text{Ac}_2\text{O}$ ,  $\text{H}_2\text{SO}_4$ ,  $\text{Br}_2$ , NaOH

**Answer (3)**



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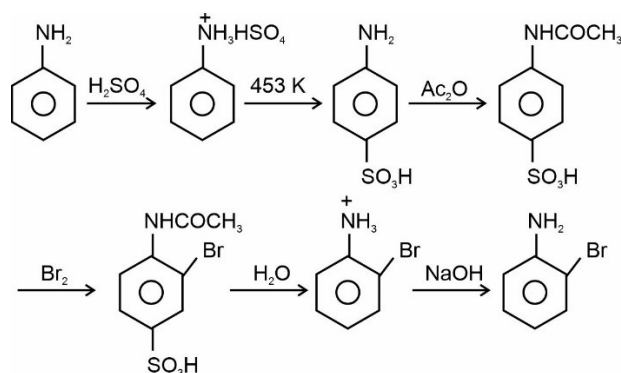
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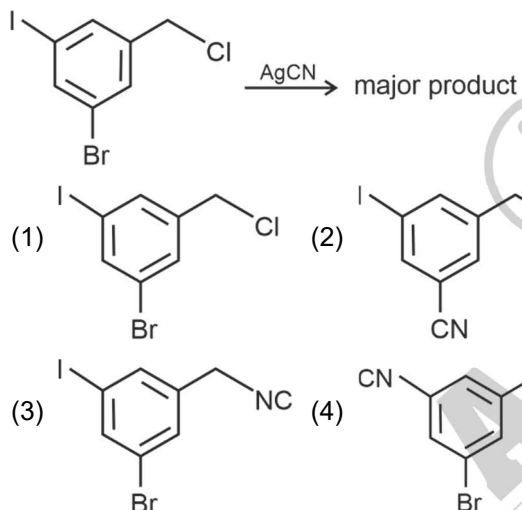
**Sol.**



Correct sequence of reagents

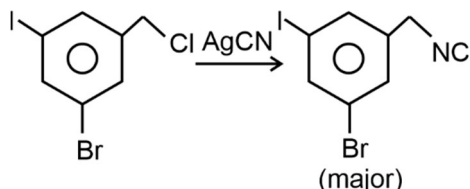
$\text{H}_2\text{SO}_4$ ,  $\text{Ac}_2\text{O}$ ,  $\text{Br}_2$ ,  $\text{H}_2\text{O}(\Delta)$ ,  $\text{NaOH}$

62. The structure of the major product formed in the following reaction is :

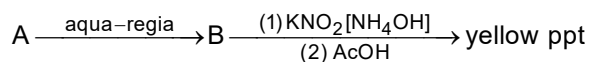


**Answer (3)**

**Sol.** Haloalkanes react with  $\text{AgCN}$  to give isocyanide as major product and haloarenes do not react with  $\text{AgCN}$ .



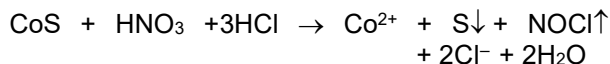
63. Find the compound 'A' from the following reaction sequences.



- (1)  $\text{CoS}$  (2)  $\text{MnS}$   
(3)  $\text{NiS}$  (4)  $\text{ZnS}$

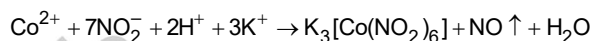
**Answer (1)**

**Sol.** Compound (A) in the given reaction sequence is likely to be  $\text{CoS}$ .



The above solution is neutralised with  $\text{NH}_4\text{OH}$ .

To a neutral solution of  $\text{Co}^{2+}$ , acetic acid and saturated solution of  $\text{KNO}_2$  are added which results in the formation of yellow precipitate of  $\text{K}_3[\text{Co}(\text{NO}_2)_6]$



64. The elemental composition of a compound is 54.2% C, 9.2% H and 36.6% O. If the molar mass of the compound is  $132 \text{ g mol}^{-1}$ , the molecular formula of the compound is:

[Given: The relative atomic mass of C : H : O = 12 : 1 : 16]

- (1)  $\text{C}_6\text{H}_{12}\text{O}_6$  (2)  $\text{C}_4\text{H}_8\text{O}_2$   
(3)  $\text{C}_4\text{H}_9\text{O}_3$  (4)  $\text{C}_6\text{H}_{12}\text{O}_3$

**Answer (4)**

**Sol.**

Element	Mass %	Mole %	Molar ratio
C	54.2	4.52	2
H	9.2	9.2	4
O	36.6	2.28	1

Empirical formula of compound is  $\text{C}_2\text{H}_4\text{O}$

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Molecular mass of compound =  $132 \text{ g mol}^{-1}$

Molecular formula of compound is  $(\text{C}_2\text{H}_4\text{O})_n$

$$n = \frac{\text{Molecular mass}}{\text{EF mass}} = \frac{132}{44} = 3$$

$\therefore$  Molecular formula of compound is  $\text{C}_6\text{H}_{12}\text{O}_3$

65. For hydrogen atom, the orbital/s with lowest energy is/are:

- (A) 4s  
(B) 3p<sub>x</sub>  
(C)  $3d_{x^2-y^2}$   
(D)  $3d_{z^2}$

(E) 4p<sub>z</sub>

Choose the **correct** answer from the options given below:

- (1) (A) and (E) only  
(2) (A) only  
(3) (B) only  
(4) (B), (C) and (D) only

#### Answer (4)

**Sol.** For hydrogen atom and one electron species, the energy of orbitals is decided by the value of principal quantum number. Higher the value of principal quantum number, higher will be the energy of orbital.

- (A) 4s  $n = 4$   
(B) 3p<sub>x</sub>  $n = 3$   
(C)  $3d_{x^2-y^2}$   $n = 3$   
(D)  $3d_{z^2}$   $n = 3$   
(E) 4p<sub>z</sub>  $n = 4$

$\therefore$  (B), (C) and (D) have orbitals with the lowest energy.

66. Based on the data given below:

$$E^\circ_{\text{Cr}_2\text{O}_7^{2-}/\text{Cr}^{3+}} = 1.33\text{V} \quad E^\circ_{\text{Cl}_2/\text{Cl}^-} = 1.36\text{V}$$

$$E^\circ_{\text{MnO}_4^-/\text{Mn}^{2+}} = 1.51\text{V} \quad E^\circ_{\text{Cr}^{3+}/\text{Cr}} = -0.74\text{V}$$

The strongest reducing agent is:

- (1)  $\text{Cl}^-$  (2) Cr  
(3)  $\text{MnO}_4^-$  (4)  $\text{Mn}^{2+}$

#### Answer (2)

$$\text{Sol. } E^\circ_{\text{Cr}_2\text{O}_7^{2-}/\text{Cr}^{3+}} = 1.33\text{V} \quad E^\circ_{\text{Cl}_2/\text{Cl}^-} = 1.36\text{V}$$

$$E^\circ_{\text{MnO}_4^-/\text{Mn}^{2+}} = 1.51\text{V} \quad E^\circ_{\text{Cr}^{3+}/\text{Cr}} = -0.74\text{V}$$

The species which has the most negative value of standard reduction potential will be the strongest reducing agent. Since  $\text{Cr}^{3+}/\text{Cr}$  has SRP value of  $-0.74\text{V}$ , Cr is the strongest reducing agent.

67. Match List – I with List – II

List – I (Transition metal ion)		List – II (Spin only magnetic moment (B.M.))	
(A)	$\text{Ti}^{3+}$	(I)	3.87
(B)	$\text{V}^{2+}$	(II)	0.00
(C)	$\text{Ni}^{2+}$	(III)	1.73
(D)	$\text{Sc}^{3+}$	(IV)	2.84

Choose the correct answer from the options given below:

- (1) (A)-(III), (B)-(I), (C)-(II), (D)-(IV)  
(2) (A)-(IV), (B)-(II), (C)-(III), (D)-(I)  
(3) (A)-(III), (B)-(I), (C)-(IV), (D)-(II)  
(4) (A)-(II), (B)-(IV), (C)-(I), (D)-(III)

#### Answer (3)

**Sol.**

Transition Metal ion	Electronic configuration	No. of unpaired electrons (BM)	Magnetic moment
(A) $\text{Ti}^{3+}$	$3d^1$	1	1.73
(B) $\text{V}^{2+}$	$3d^3$	3	3.87
(C) $\text{Ni}^{2+}$	$3d^8$	2	2.84
(D) $\text{Sc}^{3+}$	$3d^0$	0	0.00



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Krishna Sai Shishir  
2 Year Classroom

JEE (Main) 2024



**AIR 78**  
Abhishek Jain  
2 Year Classroom

JEE (Main) 2024



**AIR 93**  
Hardik Aggarwal  
2 Year Classroom

JEE (Main) 2024



**AIR 95**  
Ujjwal Singh  
2 Year Classroom

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**AIR 98**  
Rishit Aggarwal  
2 Year Classroom

JEE (Main) 2024



**AIR 100**  
Sanku Jain  
2 Year Classroom

JEE (Main) 2024



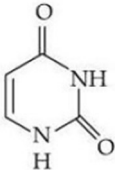
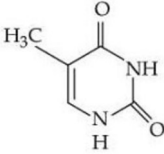
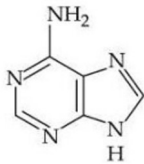
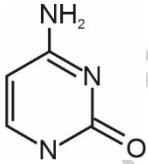
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2 Year Classroom

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Rishi Shekher Shukla  
2 Year Classroom

68. Match List-I with List-II

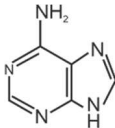
List-I		List-II	
(A)	Adenine	(I)	
(B)	Cytosine	(II)	
(C)	Thymine	(III)	
(D)	Uracil	(IV)	

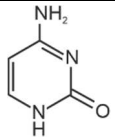
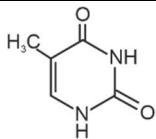
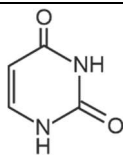
Choose the correct answer from the options given below:

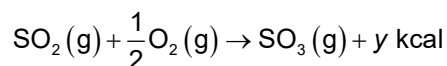
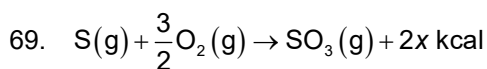
- (1) (A)-(III), (B)-(I), (C)-(IV), (D)-(II)
- (2) (A)-(IV), (B)-(III), (C)-(II), (D)-(I)
- (3) (A)-(III), (B)-(IV), (C)-(II), (D)-(I)
- (4) (A)-(III), (B)-(IV), (C)-(I), (D)-(II)

**Answer (3)**

**Sol.**

Compound		Structure	
(A)	Adenine	III.	

(B)	Cytosine	IV.	
(C)	Thymine	II.	
(D)	Uracil	I.	

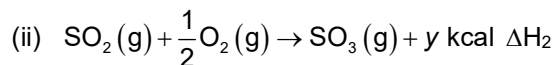
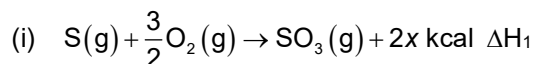


The heat of formation of  $SO_2(g)$  is given by:

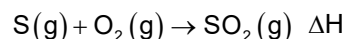
- (1)  $\frac{2x}{y} \text{ kcal}$
- (2)  $y - 2x \text{ kcal}$
- (3)  $x + y \text{ kcal}$
- (4)  $2x + y \text{ kcal}$

**Answer (2)**

**Sol.**



(i) - (ii)



$\Delta H = \Delta H_1 - \Delta H_2$

$= -2x - (-y) = (y - 2x) \text{ kcal}$



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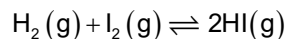
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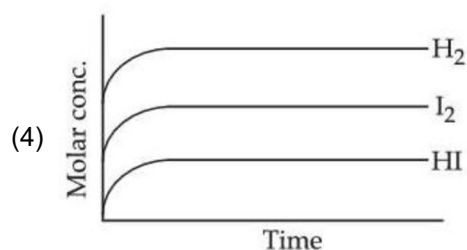
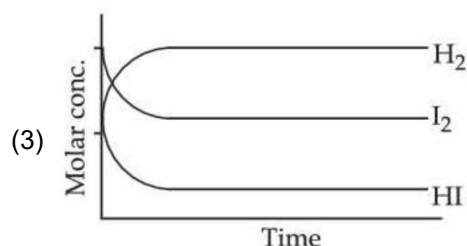
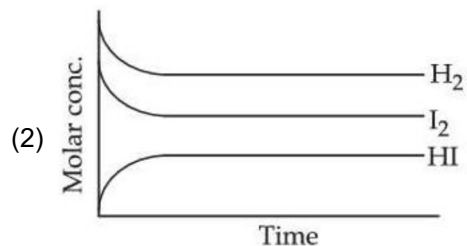
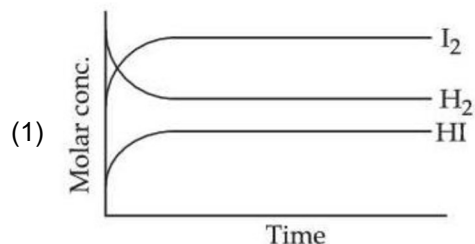
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70. For the reaction,

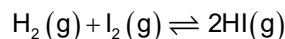


Attainment of equilibrium is predicted correctly by:

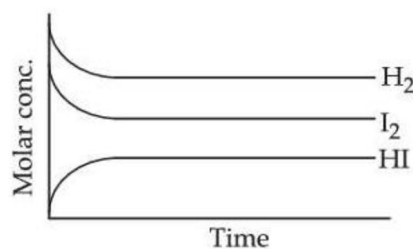


**Answer (2)**

**Sol.**



Concentrations of  $\text{H}_2(\text{g})$  and  $\text{I}_2(\text{g})$  decrease with time while concentration of  $\text{HI}(\text{g})$  increases with time. At equilibrium  $\text{H}_2(\text{g})$ ,  $\text{I}_2(\text{g})$  and  $\text{HI}(\text{g})$  attain constant values. Correct plot of molar concentration with time is



71. Consider a complex reaction taking place in three steps with rate constants  $k_1$ ,  $k_2$  and  $k_3$  respectively. The overall rate constant  $k$  is given by the expression  $k = \sqrt{\frac{k_1 k_3}{k_2}}$ . If the activation energies of the three steps are 60, 30 and 10  $\text{kJ mol}^{-1}$  respectively, then the overall energy of activation in  $\text{kJ mol}^{-1}$  is \_\_\_\_\_. (Nearest integer)

**Answer (20)**

**Sol.**  $k_1$ ,  $k_2$  and  $k_3$  are given as rate constants of three steps of a complex reaction. Rate constant ( $k$ ) of the overall reaction is given as

$$k = \sqrt{\frac{k_1 k_3}{k_2}}$$

Activation energies of the three steps are given as

$$E_{a_1} = 60 \text{ kJ mol}^{-1}, E_{a_2} = 30 \text{ kJ mol}^{-1},$$

$$E_{a_3} = 10 \text{ kJ mol}^{-1}$$

From Arrhenius equation, we know that

$$k = Ae^{-E_a/RT}$$

If  $E_a$  is the activation energy of the overall reaction, then

$$E_a = \frac{1}{2} [E_{a_1} + E_{a_3} - E_{a_2}]$$

$$= \frac{1}{2} [60 + 10 - 30] = 20 \text{ kJ mol}^{-1}$$



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Rashit Aggarwal  
2 Year Classroom

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2 Year Classroom

**Telangana Topper**



**AIR 15**  
M Sai Divya Teja Reddy  
2 Year Classroom

**Telangana Topper**



**AIR 19**  
Rishi Shekher Shukla  
2 Year Classroom



72. In Carius method of estimation of halogen, 0.25 g of an organic compound gave 0.15 g of silver bromide (AgBr). The percentage of Bromine in the organic compound is \_\_\_\_\_  $\times 10^{-1}$  % (Nearest integer).

(Given: Molar mass of Ag is 108 and Br is 80 g mol<sup>-1</sup>)

**Answer (255)**

**Sol.** Mass of organic compound = 0.25 g

Mass of AgBr = 0.15 g

$$\text{No. of moles of Br} = \text{No. of moles of AgBr} = \frac{0.15}{188}$$

$$\text{Mass of Br} = \frac{0.15 \times 80}{188} \text{ g}$$

$$\% \text{ of Br} = \frac{0.15 \times 80 \times 100}{188 \times 0.25}$$

$$= 25.5 \%$$

$$= 255 \times 10^{-1} \%$$

73. The observed and normal molar masses of compound MX<sub>2</sub> are 65.6 and 164 respectively. The percent degree of ionisation of MX<sub>2</sub> is \_\_\_\_\_ %. (Nearest integer)

**Answer (75)**

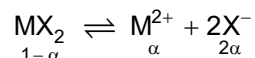
**Sol.** Normal molar mass of MX<sub>2</sub> = 164.0 g mol<sup>-1</sup>

Observed molar mass of MX<sub>2</sub> = 65.6 g mol<sup>-1</sup>

$$\text{Van't Hoff factor (i)} = \frac{\text{Normal molar mass}}{\text{Observed molar mass}}$$

$$= \frac{164}{65.6} = 2.5$$

If  $\alpha$  is the degree of ionisation, then



$$i = 1 - \alpha + \alpha + 2\alpha = 1 + 2\alpha$$

$$1 + 2\alpha = 2.5$$

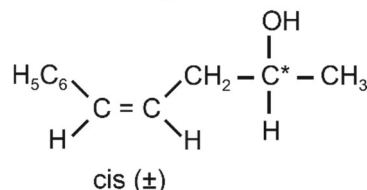
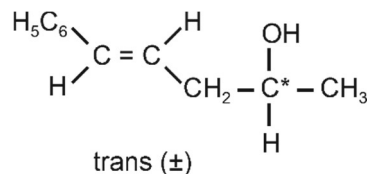
$$\alpha = 0.75$$

$$\therefore \text{Percent degree of ionisation} = 75\%$$

74. The possible number of stereoisomers for 5-phenylpent-4-en-2-ol is \_\_\_\_\_.

**Answer (4)**

**Sol.** The given compound is 5-phenylpent-4-en-2-ol. Possible stereoisomers are



$\therefore$  4 possible stereoisomers

75. The hydrocarbon (X) with molar mass 80 g mol<sup>-1</sup> and 90% carbon has \_\_\_\_\_ degree of unsaturation.

**Answer (3)**

**Sol.**

Element	Mass %	Mole %	Molar ratio
C	90	7.5	1
H	10	10	1.33

$\therefore$  Empirical formula is C<sub>3</sub>H<sub>4</sub>

Molecular mass = 80 g mol<sup>-1</sup>.

Molecular formula = (C<sub>3</sub>H<sub>4</sub>)<sub>n</sub>

$$n = \frac{\text{Molecular mass}}{\text{EF mass}} = \frac{80}{40} = 2$$

$\therefore$  Molecular formula is C<sub>6</sub>H<sub>8</sub>

$$\text{Degree of unsaturation} = \frac{2 \times 6 + 2 - 8}{2} = 3$$





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