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Memory Based Answers & Solutions

Time : 3 hrs. M.M. : 300

JEE (Main)-2024 (Online) Phase-2

(Physics, Chemistry and Mathematics)

IMPORTANT INSTRUCTIONS:

- (1) The test is of **3 hours** duration.
- (2) This test paper consists of 90 questions. Each subject (PCM) has 30 questions. The maximum marks are 300.
- (3) This question paper contains **Three Parts**. **Part-A** is Physics, **Part-B** is Chemistry and **Part-C** is **Mathematics**. Each part has only two sections: **Section-A** and **Section-B**.
- (4) Section A: Attempt all questions.
- (5) **Section B**: Attempt any 05 questions out of 10 Questions.
- (6) Section A (01 20) contains 20 multiple choice questions which have only one correct answer. Each question carries +4 marks for correct answer and -1 mark for wrong answer.
- (7) Section B (21 30) contains 10 Numerical value based questions. The answer to each question should be rounded off to the **nearest integer**. Each question carries +4 marks for correct answer and -1 mark for wrong answer.

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1 AIR JEE (Adv. 2020



PHYSICS

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer:

- There are two fixed charged spheres P and Q repelling each other with force of 16 N. A third neutral sphere is placed between the charged spheres. The new force between spheres is (assuming all three spheres are insulating spheres)
 - (1) 8 N
 - (2) 32 N
 - (3) 16 N
 - (4) 4 N

Answer (3)

- **Sol.** Electric force between two charges doesn't depend on intervening medium.
- 2. A tree branch holds a weight of 200 N by a uniform chain of mass 10 kg. The force applied by branch to hold this weight is (take $g = 10 \text{ m/s}^2$)
 - (1) 150 N
 - (2) 100 N
 - (3) 200 N
 - (4) 300 N

Answer (4)

Sol. F = 200 + 100 = 300 N

- 3. If kinetic energy of a block of mass *m* increases 36 times. By what percentage will the momentum increase?
 - (1) 6%
 - (2) 600%
 - (3) 60%
 - (4) 500%

Answer (4)

Sol.
$$k = \frac{P^2}{2m}$$

$$36k = \frac{P_1^2}{2m} \Rightarrow \boxed{P_1 = 6P}$$
 (Increased by 500%)

- 4. A ball is projected vertically upward from a building. Time taken to reach ground is T₁. Another ball is projected downward from the same building with same speed. Time taken to reach ground is T₂. If a third ball is released from the building, time taken to reach ground is
 - (1) $\sqrt{T_1T_2}$
- (2) $\sqrt{T_1^2 + T_2^2}$
- (3) $\sqrt{T_1^2 T_2^2}$
- (4) $2\sqrt{T_1T_2}$

Answer (1)

Sol.
$$-H = V_0 T_1 - \frac{1}{2} g T_1^2$$

$$-H = -V_0T_2 - \frac{1}{2}gT_2^2$$

$$H = \frac{1}{2}g\left(\frac{T_1 + T_2}{2}\right)^2 - \frac{1}{2}g\left(\frac{T_1 - T_2}{2}\right)^2$$

$$T = \sqrt{\frac{2H}{g}}$$

$$\Rightarrow \quad T = \sqrt{T_1 T_2}$$

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5. The weight of an object measured on the surface of earth is 300 N. What will be weight of the same object at depth $\frac{R}{4}$ inside the earth?

(R = radius of earth)

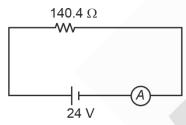
- (1) 220 N
- (2) 225 N
- (3) 200 N
- (4) 210 N

Answer (2)

Sol. $W_1 = mg = 300 \text{ N}$

$$W_2 = mg' = mg\left(1 - \frac{d}{R}\right)$$
$$= mg\left(\frac{3}{4}\right)$$
$$= 225 \text{ N}$$

6. An ammeter consists of 240 Ω galvanometer and 10 Ω shunt resistance is connected in circuit as shown. Reading of ammeter is



- (1) 0.18 A
- (2) 0.16 A
- (3) 0.32 A
- (4) 3.2 A

Answer (2)

Sol.
$$R_A = \frac{10 \times 240}{250} = 9.6 \ \Omega$$

$$R = 140.4 + 9.6 = 150 \Omega$$

$$i = \frac{24}{150} = 0.16$$

- 7. An isolated system contains one mole of helium, given a heat of 48 J. If the temperature of system changes by 2°C, then find work done. (take R = 8.35/mole-K)
 - (1) 32.20 J
 - (2) 37.34 J
 - (3) 40.74 J
 - (4) 41.74 J

Answer (4)

Sol. Q = 48 J

$$\Delta Q = \Delta V + \Delta W$$

$$48 = 1 \times \frac{3R}{2}(2) + W$$

$$W = 48 - \frac{3}{4} (8.35)$$

- Find the longest wavelength of Paschen series for hydrogen atom. (Rydberg constant = 10⁷/m)
 - (1) 2.06 μm
 - (2) 20.6 μm
 - (3) 4.86 μm
 - (4) 48.6 μm

Answer (1)

Sol.
$$\frac{1}{\lambda} = R\left(\frac{1}{3^2} - \frac{1}{4^2}\right)$$

$$\lambda = \frac{144}{7 \times 10^7} = 20.57 \times 10^{-7}$$

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- 9. Find net kinetic energy (maximum possible) associated with 20 diatomic molecules (Here k_B is Boltzmann constant and T is absolute temperature of diatomic gas).
 - (1) $35 k_B T$
 - (2) $70 k_B T$
 - (3) $60 k_B T$
 - (4) $30 k_B T$

Answer (2)

Sol.
$$E_i = (5+2)\frac{1}{2}kT$$

= $\frac{7}{2}kT$

$$E_T = 20 \times \frac{7}{2} kT$$
$$= 70 \ k_B T$$

10. **Statement-I**: Dimensions of specific heat capacity is $[L^2T^{-2}K^{-1}]$

Statement-II: Dimensions of universal gas constant is [ML²T⁻¹K⁻¹]

- (1) Both statements are incorrect
- (2) Both statements are correct
- (3) Statement-I is correct but statement-II is incorrect
- (4) Statement-I is incorrect but statement-II is correct

Answer (3)

Sol.
$$S = \frac{Q}{m\Delta T} = \frac{ML^2T^{-2}}{mK} = [L^2T^{-2}K^{-1}]$$

 $R = \frac{ML^2T^{-2}}{K} = [ML^2T^{-2}K^{-1}]$

- 11. The displacement (x) of a particle vary as $x^2 = 1 + \ell^2$ and acceleration is given function of x as x^{-n} , then find n.
 - (1) 1

(2) 3

(3) 4

(4) 2

Answer (2)

Sol.
$$x = \sqrt{1 + t^2}$$

$$v = \frac{1}{2}(1+t^2)^{-\frac{1}{2}}(2t)$$

$$=\frac{t}{\sqrt{a+1+t^2}}$$

$$a=\frac{1}{x^3}=x^{-3}$$

- 12.
- 13.
- 14.
- 15.
- 16.
- 17.
- 18.
- 19.
- 20.

SECTION - B

Numerical Value Type Questions: This section contains 10 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. A convex lens has a focal length of f = 20 cm, $R_1 = 15$ cm, $R_2 = 30$ cm. The refractive index of the lens is $\frac{x}{2}$. The value of x is ______.

Answer (3)

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Sol.
$$\frac{1}{f} = (\mu - 1) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$\Rightarrow \frac{1}{20} = (\mu - 1) \left(\frac{1}{15} + \frac{1}{30} \right) = (\mu - 1) \frac{3}{30}$$

$$\Rightarrow \mu - 1 = \frac{1}{2} \Rightarrow \mu = 1.5$$

22. For a device, power consumed = 110 W and voltage supplied is 220 V. The number of electrons that flow in 1 s is $\frac{x}{4} \times 10^{17}$. Find x.

Answer (125)

Sol.
$$P = VI$$

$$\Rightarrow I = 0.5 A$$

⇒ Number of electrons

$$= \frac{0.5 \times 1}{1.6 \times 10^{-19}}$$
$$= \frac{1000}{32} \times 10^{17}$$

$$= 31.25 \times 10^{17}$$

23. In a photoelectric setup, work function of the material is 2.13 eV, wavelength used in 300 nm. If hc = 1240 eV.nm, stopping potential for the set-up is _______V.

Answer (2)

Sol.
$$\frac{hc}{\lambda} - \phi = eV_s$$

 $\Rightarrow (4.13 - 2.13) \text{ eV} = eV_s$
 $\Rightarrow V_s = 2 \text{ Volts}$

24. A car of mass 800 kg is moving in a circular path of radius 300 m on a banked road with angle 30°. Coefficient of friction between the car and road is 0.2. Find the maximum safe speed (to the nearest integer in m/s) with which the car can travel.

$$\left(\text{Take }\sqrt{3}=1.7\right)$$

Answer (52)

Sol.
$$V_{\text{max}} = \sqrt{\frac{rg(\mu + \tan \theta)}{1 - \mu \tan \theta}} = \sqrt{\frac{300 \times 10(0.2 + \tan 30)}{1 - 0.2 \tan 30}}$$

$$V_{\text{max}} = \sqrt{\frac{2680}{1 - 100}} = \frac{100 \times 10(0.2 + \tan 30)}{1 - 0.2 \tan 30}$$

25. Two sources produce, individually, intensities of I and 4I at a location. If they are coherent, then difference between I_{max} and I_{min} is nI. Find n.

Answer (8)

Sol.
$$I_{\text{max}} = \left(\sqrt{I_1} + \sqrt{I_2}\right)^2 = 9I$$

$$I_{\min} = \left(\sqrt{I_1} - \sqrt{I_2}\right)^2 = I$$

$$\Rightarrow n = 8$$

26. An object of mass 30 kg and relative density 5 is immersed inside water. The weight of the object inside water is 10x N. Find the value of x.

Answer (24)

Sol.
$$W = mg - V_{\text{object}} \times \rho_{\text{water}} \cdot g$$

$$W = 300 - \frac{m_{\text{object}}}{\rho_{\text{object}}} \rho_{\text{water}} \cdot g$$

$$W = 300 - \frac{30}{5} \times 1 \times 10$$

$$W = 240 N$$

- 27.
- 28.
- 29.
- 30.

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CHEMISTRY

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer:

- The molarity of NaCl solution is 3 M. Calculate the molality of the solution. [Given density of the solution = 1.25 g/mL]
 - (1) 2.9
- (2) 2.79
- (3) 1.85
- (4) 3.85

Answer (2)

Sol. Given molarity of solution = 3 M means 3 moles of NaCl is present in 1000 mL of solution.

Mass of solution = $d \times v$

$$= 1.25 \times 1000$$

$$= 1250 g$$

Mass of solute = $3 \times 58.5 = 175.5 \text{ g}$

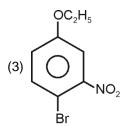
2. Identify the major product formed in the following reaction.

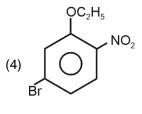
Answer (3)

Sol.

Product B is:

$$(1) \bigcup_{NO_2}^{OC_2H_5} Br$$
 (2)





OC₂H₅

NO₂

Answer (A)

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JEE (Main)-2024: Phase-2 (06-04-2024)-Evening



Sol.
$$OC_2H_5$$
 OC_2H_5 OC_2H_5

$$OC_2H_5$$
 OC_2H_5
 OC_2H_5
 OC_2H_5
 OC_2H_5
 OC_2H_5
 OC_2
 $OC_$

Product P is:

4.



Answer (3)

- 5. Which of the following *d*-block elements has maximum unpaired electron in ground state electronic configuration?
 - (1) Ti(22)
- (2) V(23)
- (3) Mn(25)
- (4) Cr(24)

Answer (4)

Sol. $Ti(22) = [Ar] 3d^24s^2$

n = 2

 $V(23) = [Ar] 3d^34s^2$

n = 3

 $Mn(25) = [Ar] 3a^54s^2$

n = 5

 $Cr(24) = [Ar] 3a^54s^1$

n = 6

Cr(24) has maximum unpaired electron i.e., 6.

- Find out shortest wavelength of Paschen series for H-atom.
 - (1) $\frac{9}{R}$

- (2) $\frac{16}{R}$
- (3) $\frac{144}{7R}$
- (4) $\frac{7R}{144}$

Answer (1)

Sol. $\frac{1}{\lambda} = R(1)^2 \left(\frac{1}{9} - \frac{1}{\infty}\right)$

 $\frac{1}{\lambda} = R\left(\frac{1}{9}\right)$

 $\lambda = \frac{9}{R}$

7. Match the column.

Column-I (Compounds)

Column-II (Configurations)

- A. TiCl₄
- (1) $e^3t_2^3$
- B. FeO₄²⁻
- (2) $e^2t_2^0$
- C. FeCl₄²⁻
- (3) $e^2t_2^3$
- D. $MnCl_4^{2-}$
- (4) $e^0 t_2^0$

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- (1) A(4), B(2), C(1), D(3)
- (2) A(4), B(3), C(2), D(1)
- (3) A(1), B(2), C(3), D(4)
- (4) A(2), B(4), C(3), D(1)

Answer (1)

Sol. $TiCl_4 \Rightarrow Ti^{4+} \Rightarrow e^0t_2^0$

$$FeO_4^{2-} \Rightarrow Fe^{6+} \Rightarrow e^2t_2^0$$

$$FeCl_4^{2-} \Rightarrow Fe^{2+} \Rightarrow e^3t_2^3$$

$$MnCl_4^{2-} \Rightarrow Mn^{2+} \Rightarrow e^2t_2^3$$

8. $CH_3COOH \xrightarrow{\text{LiAIH}_4} A \xrightarrow{\text{PCC}} B \xrightarrow{\text{(i)}CN^-} C \xrightarrow{\text{Hydrolysis}} D$

Select the correct option

- (3) B is CH₃CH₂OH (4) C is CH₃CH₂CO₂H

Answer (2)

Sol.
$$CH_3COOH \xrightarrow{LiAlH_4} CH_3CH_2OH \xrightarrow{PCC} CH_3CHO$$

$$(A) \qquad (B)$$

$$(i) \mid CN^-$$

$$(iii) \mid H^+$$

$$CH_3 - CH \xrightarrow{Hydrolysis} CH_3 - CH$$

$$CO_2H \qquad CN$$

$$(C)$$

- Which of the following statement is incorrect-
 - (1) Enzymes are biocatalyst
 - (2) Enzymes are not specific
 - (3) Enzymes are globular protein
 - (4) Oxidase enzymes catalyse the oxidation of C-N and C-O bonds

Answer (2)

- **Sol.** (1) Enzymes are biocatalyst that catalyse numerous biological process.
 - (2) They are very specific in nature
 - (3) Enzymes are mainly globular proteins
 - (4) Oxidase are enzymes specific to oxidation reduction reactions involving oxidation of C-N and C-O bonds
- 10. Find relation between KP and KC for given reaction:

$$C(s) + \frac{1}{2}O_2(g) \longrightarrow CO(g)$$

- (1) $K_P = K_C(RT)^1$
- (2) $K_P = K_C(RT)^{-1}$
- (3) $K_P = K_C(RT)^{1/2}$
- (4) $K_P = K_C(RT)^{-1/2}$

Answer (3)

Sol. $K_P = K_C(RT)^{\Delta n_g}$

$$\Delta n_g = \frac{1}{2}$$

$$K_P = K_C(RT)^{1/2}$$

 $\Delta n_g = \frac{1}{2}$ $K_P = K_C(RT)^{1/2}$ 11. Given for two first order reactions $\frac{t_{1/2}^1}{t_{1/2}^2} = \frac{2}{5}.$

Then
$$\frac{t_{2/3}^1}{t_{4/5}^2} = ?$$

- (1) 0.273
- (2) 0.468
- (3) 0.318
- (4) 2.55

Answer (1)

Sol.
$$\frac{K_2}{K_1} = \frac{2}{5}$$

$$t_{2/3}^1 = \frac{2.303}{K_1} log 3$$

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$$t_{4/5}^2 = \frac{2.303}{K_2} log 5$$

$$\frac{t_{2/3}^1}{t_{4/5}^2} = \frac{K_2 \log 3}{K_1 \log 5}$$

$$=\frac{2}{5} \times \frac{0.477}{0.699}$$

$$= 0.273$$

- 12. Among the following anions, identify the anion which gives pale yellow precipitate with aq. AgNO₃. The precipitate is partially soluble in aq. NH₄OH solution.
 - (1) I-

- (2) CI-
- (3) Br-
- (4) NO_2^-

Answer (3)

Sol.
$$I^- + Ag^+ \longrightarrow AgI$$

(Yellow ppt.)

$$Cl^- + Ag^+ \longrightarrow AgCl$$
 (White ppt.)

$$Br^- + Ag^+ \longrightarrow AgBr$$

(Pale yellow ppt.)

$$NO_2^- + Ag^+ \longrightarrow AgNO_2$$
 (White ppt.)

AgBr is partially soluble in aq. NH₄OH solution whereas AgI is insoluble in ag. NH₄OH solution.

13. Arrange the following compounds in increasing order of electrophilic aromatic substitution.









(i)

(ii)

(iii)

- (1) (iv) < (iii) < (ii) < (i)
- (2) (ii) < (iii) < (iv) < (i)
- (3) (iv) < (ii) < (iii) < (i)
- (4) (i) < (ii) < (iii) < (iv)

Answer (1)

Sol. Rate of EAS is

- (i) is activated due to resonance and (ii) due to hyperconjugation, (iv) is deactivated due to reverse hyperconjugation.
- 14. IUPAC name of complex compound $[Pt(Br)_2(PPh_3)_2].$
 - (1) Dibromido di(triphenyl phosphine) platinum(II)
 - (2) Dibromido bis(triphenyl phosphine) platinum(II)
 - (3) bis(triphenyl phosphine) dibromide platinum(II)
 - (4) bis(triphenyl phosphine) dibromide platinate(II)

Answer (2)

- **Sol.** Dibromido bis(triphenyl phosphine) platinum(II) is the correct IUPAC name of given complex compound.
- 15.
- 16.
- 17.
- 18.
- 19. 20.

SECTION - B

Numerical Value Type Questions: This section contains 10 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. For a certain reaction, Δ_rH is 400 kJ/mol and $\Delta S = 0.2 \text{ kJ/mol} \text{ K}$. Above what minimum temperature in kelvin, the reaction become spontaneous

Answer (2000)

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Sol. For reaction to be spontaneous,

 $\Delta G < O$

 $\Delta H - T\Delta S < O$

$$T > \frac{\Delta H}{\Delta S} = \frac{400}{0.2} = 2000 \text{ K}$$

Minimum temperature for spontaneity = 2000 K

 The number of compounds having central atom is sp² hybridised

Answer (5)

$$\begin{array}{ccc}
O \\
H - C - H & \Rightarrow & sp^{2} \\
H & C = C & \Rightarrow & sp^{2}
\end{array}$$

$$\bigcirc S \Rightarrow sp^2$$

$$\begin{array}{ccc} & & & & \\ & & \\ & & & \\ & & & \\ & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\$$

$$\begin{array}{ccc} H & & & \\ & & \\ & & & \\ & & & \\ & & & \\ & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\$$

Sol.

$$-B_F^{\prime} \Rightarrow sp$$

$$SiO_2(s)$$
 \Rightarrow sp^2

$$\begin{array}{c}
H \\
C \\
C \\
CI
\end{array}$$

$$\Rightarrow sp^3$$

If steric number is 3, then hybridisation is sp^2 .

23. Among the following, how many metal ions act as oxidising agents?

Answer (2)

- **Sol.** Due to inert pair effect, Pb²⁺ is more stable than Pb⁴⁺ and Tl⁺ is more stable than Tl³⁺. Therefore, Pb⁴⁺ and Tl³⁺ only will act as oxidising agents
- 24. Calculate the magnetic moment in B.M. of the one from VO_2^{\oplus} , MnO_4^{\ominus} and $Cr_2O_7^{2-}$ which is having least oxidizing property

Answer (0)

Sol. For 3-d transition series,

Oxidizing power $V^{+5} < Cr^{+6} < Mn^{-7}$

 μ_{spin} of V+5 :

 $V^{+5} \rightarrow [Ar] 4s^0 3d^0$

Number of unpaired $e^- = 0$

 $\mu_{\text{spin}} = 0$

25. How many geometrical isomers are there in but-2-ene?

Answer (2)

Sol. But-2-ene has one stereogenic centre and it has two geometrical isomer as given below.

cis but-2-ene

$$C = C$$
 CH_3

trans but-2-ene

- 26.
- 27.
- 28.
- 29.
- 30.

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MATHEMATICS

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer:

1. If $\int \frac{dx}{a^2 \sin^2 x + b^2 \cos^2 x} = \frac{1}{12} \tan^{-1} (3 \tan x) + c$

then the maximum value of asinx + bcosx is

- $(1) \sqrt{10}$
- (2) $\sqrt{20}$
- (3) $2\sqrt{10}$
- (4) 2√5

Answer (3)

Sol.
$$I = \int \frac{\sec^2 x dx}{b^2 + a^2 \tan^2 x}$$

 $tanx = t \Rightarrow sec^2xdx = dt$

$$I = \int \frac{dt}{b^2 + a^2 t^2} = \frac{1}{ba} \tan^{-1} \left(\frac{at}{b} \right)$$

- $\Rightarrow I = \frac{1}{ab} \tan^{-1} \left(\frac{a}{b} \tan x \right) + c$
- \Rightarrow ab = 12 \Rightarrow a² = 36

 - $\frac{a}{b} = 3$ \Rightarrow $b^2 = 4$
- \Rightarrow Maximum value of $a\sin x + b\cos x$ is

$$\sqrt{a^2+b^2}=\sqrt{40}=2\sqrt{10}$$

- 2. Range of $\frac{1}{7 \sin 5x}$ equals to

 - (1) $\left[\frac{1}{7}, \frac{1}{5}\right]$ (2) $\left[\frac{1}{7}, \frac{1}{6}\right]$

 - $(3) \left[\frac{1}{8}, \frac{1}{5} \right] \qquad (4) \left[\frac{1}{8}, \frac{1}{6} \right]$

Answer (4)

Sol. We know that,

- $-1 \le \sin 5x \le 1$
- $-1 < -\sin 5x < 1$
- $6 \le 7 \sin 5x \le 8$

$$\frac{1}{8} \le \frac{1}{7 - \sin 5x} \le \frac{1}{6}$$

- \therefore Range is $\left[\frac{1}{8}, \frac{1}{6}\right]$
- 3. There are letters to be delivered to 5 different location, then find the probability that letter is delivered to exactly 2 correct address assuming each letter is delivered to unique address.

Answer (3)

Sol. ⇒ Select any two correct address

$$\Rightarrow$$
 $({}^{5}C_{2})$

Remaining 3 have to be dearranged

$$\Rightarrow 3! \left(1 - \frac{1}{1!} + \frac{1}{2!} - \frac{1}{3!}\right)$$

$$= 6\left(1-1+\frac{1}{2}-\frac{1}{6}\right)=3-1=2$$
 ways

$$\Rightarrow$$
 ${}^5C_2 \cdot 2 = 10$

Probability =
$$\frac{10}{5!} = \frac{1}{12}$$

- The 315th word in dictionary arranged in order for the word 'NAGPUR' is
 - (1) NRAGPU
- (2) NRPGUA
- (3) NPRGUA
- (4) NRAPGU

Answer (4)

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Sol. Letters N,A,G,P,U,R.

Total words start with letter A

5! = 120

Words start with G

5! = 120

Words with N at first place and A at 2nd place

4! = 24

Words with N at first and G at 2nd place

4! = 24

Words with N at first and P at 2nd place

4! = 24

So total words 120 + 120 + (24)3

= 312

313th word = NRAGPU

314th word = NRAGUP

315th word = NRAPGU

So. 315th word = NRAPGU

- Let A = [1, 2, 3, 4, 5], m be the number of relation such as 4x < 5y XRY and n be the minimum number of elements to be added from $A \times A$ to make symmetric relation. Then the value of n + m.
 - (1) 26

(2) 25

(3) 24

(4) 23

Answer (2)

Sol. A = [1, 2, 3, 4, 5]

XRY when 4x < 5y

So $R = \{(1, 1), (1, 2), (1, 3), (1, 4), (1, 5), (2, 2), (2,$

(2, 3), (2, 4), (2, 5), (3, 3), (3, 4), (3, 5), (4, 4), (4, 5),

(5, 4), (5, 5)

m = 16

As $(1, 2) \in R$ then (2, 1) is to be added

 $(1, 3) \in R$ So (3, 1) will be added

 $(1, 4) \in R$ So $(4, 1) \in R$

 $(1,5) \in R \text{ So } (5,1) \in R$

- $(2, 3) \in R \text{ So } (3, 2) \in R$
- $(2, 4) \in R$ So $(4, 2) \in R$
- $(2, 5) \in R$ So $(5, 2) \in R$
- $(3, 4) \in R \text{ So } (4, 3) \in R$
- $(3, 5) \in R \text{ So } (5, 3) \in R$

to make R symmetric

So n = 9

m + n = 25

6. If the area bounded by the region (x, y) such that

 $\left\{ (x, y) \left| \frac{a}{v^2} < y < \frac{1}{x} \right| \text{ such that } 1 < x < 2, \ 0 < a < 1 \right\} \right\}$

is $\left(\ln 2 - \frac{2}{7}\right)$ sq. units then (7a - 3) is equal to

(1) 0

(2) 1

(3) 2

(4) 4

Answer (2)

Sol. $\Rightarrow \int_{1}^{2} \left(\frac{1}{x} - \frac{a}{x^2}\right) dx = \left(\ln|x| + \frac{a}{x}\right)^2$

 $\left(\ln 2 + \frac{a}{2}\right) - \left(\ln 1 + a\right) = \ln 2 - \frac{a}{2}$

 $= \ln 2 - \frac{2}{7} = \ln 2 - \frac{a}{2}$

 \Rightarrow 7a – 3 = 1

If the function $f(x) = \left(\frac{1}{x}\right)^{2x} x > 0$, attains the maximum value of $x = \frac{1}{2}$, then

- (1) $e^{\pi} < \pi^{e}$
- (2) $e^{2\pi} < (2\pi)^e$
- (3) $(2e)^{\pi} > (\pi)^{2e}$ (4) $e^{\pi} > \pi^{e}$

Answer (4)

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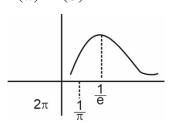
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Sol. $f\left(\frac{1}{\pi}\right) < f\left(\frac{1}{e}\right)$



$$(\pi)^{\frac{2}{\pi}} < e^{\frac{2}{e}} \Rightarrow \pi^{2e} < e^{2\pi}$$
 $e^{\pi} > \pi^{e}$

- 8. If $\vec{a} = 2\hat{i} \hat{j} + \hat{k}$ and $\vec{b} = ((\vec{a} \times (\hat{i} + \hat{j}) \times \hat{i}) \times \hat{i})$ then the square of projection of \vec{a} on \vec{b} is
 - (1) $\frac{1}{3}$

(2) 2

(3) $\frac{1}{2}$

 $(4) \frac{2}{5}$

Answer (4)

Sol.
$$\vec{a} \times (\hat{i} + \hat{j}) = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & -1 & 1 \\ 1 & 1 & 0 \end{vmatrix}$$
$$= -\hat{i} + \hat{j} + 3\hat{k}$$

$$\left(\left(\vec{a}\times\left(\hat{i}+\hat{j}\right)\right)\times\hat{i}\right)=-\hat{k}+3\hat{j}$$

$$\left(\left(\left(\vec{a}\times\left(\hat{i}+\hat{j}\right)\right)\times\hat{i}\right)\times\hat{i}\right)=-\hat{j}-3\hat{k}\left(\vec{b}\right)$$

.. Projection of
$$\vec{a}$$
 on $\vec{b} = \frac{\vec{a} \cdot \vec{b}}{|\vec{b}|}$
$$= \frac{-2}{\sqrt{10}}$$

Square of projection = $\frac{4}{10} = \frac{2}{5}$

9.
$$\lim_{n\to\infty} \frac{\sum (n^4 - 2n^3 + n^2)}{\sum ((3n)^4 + n^3 - n^2)}$$
 is equal to

(1) $\frac{1}{81}$

- (2) $\frac{1}{72}$
- (3) $\frac{1}{57}$
- (4) $\frac{1}{93}$

Answer (1)

Sol.
$$\lim_{n \to \infty} \frac{\sum (n^4 - 2n^3 + n^2)}{\sum ((3n)^4 + n^3 - n^2)} = \lim_{n \to \infty} \frac{\sum n^4}{\sum (3n)^4}$$

(As $\sum n^2$ will dominate and has highest powers of n)

$$= \lim_{n \to \infty} \frac{1}{34} \frac{\sum n^4}{\sum n^4}$$

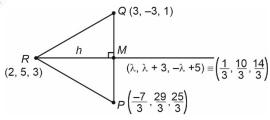
$$=\frac{1}{81}$$

- 10. If (α, β, γ) is the mirror image of Q (3, -3, 1) in the line $\frac{x-0}{1} = \frac{y-3}{1} = \frac{z-5}{-1}$ and R (2, 5, 3). If the area of Δ PQR is λ , then $\frac{\lambda^2}{546}$ equals to
 - (1) $\frac{125}{81}$
- (2) $\frac{25}{81}$
- (3) $\frac{1}{81}$

(4) $\frac{5}{81}$

Answer (1)

Sol.



$$(\lambda - 3) + 1 (\lambda + 6) - 1(-\lambda + 4) = 0$$

$$3\lambda - 1 = 0 \implies \lambda = \frac{1}{3}$$

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Our Stars

Chirag Falor
4 Year Classroom
AIR
JEE (Adv.)
2020





Area of $\triangle PQR = 2 \times \frac{1}{2} (QM \cdot MR)$

$$(QM)(MR) = \left(\sqrt{\left(3 - \frac{1}{3}\right)^2 + \left(-3 - \frac{10}{3}\right)^2 + \left(1 - \frac{14}{3}\right)^2}\right)$$

$$\left(\sqrt{\left(2-\frac{1}{3}\right)^2 + \left(5-\frac{10}{3}\right)^2 + \left(3-\frac{14}{3}\right)^2}\right)$$

$$(QM)(MR) = \frac{1}{9} \left(\sqrt{64 + 19^2 + 11^2} \right) \left(\sqrt{25 + 25 + 25} \right)$$

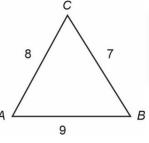
$$=\frac{\sqrt{546\times125}}{9}$$

$$= \frac{5}{9}\sqrt{546 \times 5}$$

- 11. Sides of a triangle are AB = 9, BC = 7, AC = 8. Then cos 3C equals to
 - (1) $\frac{-262}{343}$

Answer (1)

Sol.



$$\cos C = \frac{8^2 + 7^2 - 9^2}{2 \times 8 \times 7} = \frac{32}{2 \times 8 \times 7} = \frac{2}{7}$$

 $\cos 3C = 4 \cos^3 C - 3\cos C$

$$=4\times\frac{8}{343}-\frac{6}{7}=\frac{32-6\times49}{343}$$

$$=\frac{-262}{343}$$

12. The locus of P such that the ratio of distance P from A(3, 1) and B(1, 2) is 5 : 4 is

(1)
$$81x^2 - 92x + 81y^2 - 180y = 35$$

(2)
$$81x^2 + 92x + 81y^2 - 19y = 35$$

(3)
$$81x^2 - 48x + 81y^2 + 20y = 35$$

(4)
$$81x^2 - 90x + 81y^2 - 180y = 35$$

Answer (4)

Sol. Take point P(x, y)

$$\frac{5}{(3, 1)} \frac{P}{(1, 2)}$$
$$x = \frac{5+12}{9}, y = \frac{10+4}{9}$$

$$P = \left(\frac{17}{9}, \frac{14}{9}\right)$$
 (internally)

for externally division.

$$x=-\frac{7}{9}, y=\frac{6}{9}$$

$$P' = \left(\frac{-7}{9}, \frac{6}{9}\right)$$

Locus of P is the circle whose diameter is PP'

$$\left(x - \frac{-17}{9}\right)\left(x + \frac{7}{9}\right) + \left(y - \frac{14}{9}\right)\left(y - \frac{6}{9}\right) = 0$$

$$(9x - 17)(9x + 7) + (9y - 14)(9y - 6) = 0$$

So
$$81x^2 - 90x + 81y^2 - 180y = 35$$

13. If
$$\left| \frac{z_1 - 2z_2}{\frac{1}{2} - \overline{z}_1 z_2} \right| = 2$$
 then

- (1) z_1 lie on circle with radius 1 and z_2 lie on circle with radius 2
- (2) z_1 lie on circle with radius 1 and z_2 lie on circle with radius 1
- (3) z_1 lie on circle with radius $\frac{1}{2}$ and z_2 lie on circle with radius 1
- (4) z_1 lie on circle with radius 1 and z_2 lie on circle with radius $\frac{1}{2}$

Answer (4)

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Sol.
$$|z_1 - 2z_2| = |1 - 2\overline{z}_1 z_2|$$

$$\Rightarrow (z_1 - 2z_2)(\overline{z}_1 - 2\overline{z}_2) = (1 - 2\overline{z}_1z_2)(1 - 2z_1\overline{z}_2)$$

$$\Rightarrow |z_1|^2 + 4|z_2|^2 - 2z_1\overline{z}_2 - 2\overline{z}_1z_2$$

=
$$1 - 2z_1\overline{z}_2 - 2\overline{z}_1z_2 + 4|z_1|^2|z_2|^2$$

$$\Rightarrow |z_1|^2 + 4|z_2|^2 - 4|z_1|^2|z_2|^2 - 1 = 0$$

$$(|z_1|^2 - 1)(4|z_2|^2 - 1) = 0$$

$$\Rightarrow$$
 $|z_1| = 1$ and $|z_2| = \frac{1}{2}$

14. If the orthocentre of triangle formed by (8, 3), (5, 1) and (h, k) is (6, 1), then (h, k) lie on

(1)
$$x^2 + y^2 = 64$$

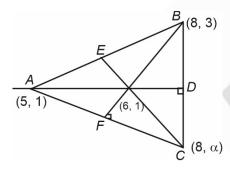
(2)
$$x^2 + y^2 = 68$$

(3)
$$x^2 + y^2 = 65$$

(4)
$$x^2 + y^2 = 71$$

Answer (2)

Sol.

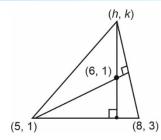


Slope of BF = 1

$$\Rightarrow$$
 Slope of $AC = \left(\frac{\alpha - 1}{8 - 5}\right) = -1$

$$\Rightarrow \alpha - 1 = -3$$

$$\Rightarrow \alpha = -2$$



$$(h, k)$$
 lie on $(y-1) = \frac{-3}{2}(x-6)$

$$2y-2+3x-18=0$$

$$2y + 3x = 20$$
 ...(1)

(h, k) lies on circumcircle eg. of circumcircle is $x^2 + v^2 = 68$

16.

18.

20.

SECTION - B

Numerical Value Type Questions: This section contains 10 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. If α , β are the roots of the equation $x^2 - \sqrt{2}x - 8 = 0$ and $A_n = \alpha^n + \beta^n$, $n \in \mathbb{N}$, then the value of $\frac{A_{10} - \sqrt{2}A_9}{2A_0}$

Answer (4)

Sol.
$$x^2 - \sqrt{2}x - 8 = 0$$

$$A_{10} - \sqrt{2} \cdot A_9 - 8A_8 = 0$$

$$\Rightarrow \frac{A_{10} - \sqrt{2} \cdot A_9}{A_8} = 8$$

$$\Rightarrow \frac{A_{10} - \sqrt{2} \cdot A_9}{2 \cdot A_8} = 4$$

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22. If $^{n+1}C_{r+1}$: $^{n}C_{r}$: $^{n-1}C_{r-1} = 55:35:21$

The value of n + r is

Answer (16)

Sol. $\frac{n+1}{r+1} \times {}^{n}C_{r} : {}^{n}C_{r} : \frac{r}{n} {}^{n}C_{r} = 55 : 35 : 21$

$$\Rightarrow \frac{n+1}{r+1} = \frac{55}{35} \text{ and } \frac{n}{r} = \frac{35}{21}$$

$$\Rightarrow \frac{n+1}{r+1} = \frac{11}{7}$$
 and $\frac{n}{r} = \frac{5}{3}$

$$\Rightarrow$$
 7n + 7 = 11r + 11

$$7n - 11r = 4$$

$$3n - 5r = 0$$

Solving (1) and (2)

$$r = 6$$
 and $n = 7$

$$\Rightarrow$$
 $n + r = 10 + 6 = 16$

23. If the order of matrix A is 3 and |A| = 3 then the value of $det(adj(-4adj(-3adj(2A^{-1}))))$ is 2^m . 3^n . The value of m + 2n =

Answer (44)

Sol. |adj(-4adj(-3adj(2A⁻¹)))|

$$= |-4adj(-3adj(2A^{-1}))|^2$$

$$=4^{6}|-3adj(2A^{-1})|^{4}$$

$$=4^{6}.3^{12} |adj(2A^{-1})|^{4}$$

$$=4^{6}.3^{12}|2A^{-1}|^{8}$$

$$=4^6.3^{12}.2^{24} |A^{-1}|^8$$

$$=4^{6}.3^{12}.2^{24}. \frac{1}{|A|^{8}}=3^{12}.\frac{2^{36}}{3^{8}}$$

$$= 3^4. 2^{36}$$

$$m = 36 \ n = 4 \Rightarrow m + 2n = 36 + 8 = 44$$

24. If
$$\int_{0}^{3} \left[x^{2} \right] + \left[\frac{x^{2}}{2} \right] dx$$

= $a + b\sqrt{2} + c\sqrt{6} - \sqrt{3} - \sqrt{5} - \sqrt{7}$ (a, b, $c \in I$) then (a + b + c) equals

Answer (23.00)

Sol.
$$\int_{0}^{3} \left[[x^{2}] + \left[\frac{x^{2}}{2} \right] \right] dx = \int_{0}^{1} 0 dx + \int_{1}^{\sqrt{2}} 1 dx + \int_{\sqrt{2}}^{\sqrt{3}} 3 dx + \int_{\sqrt{3}}^{2} 4 dx + \int_{2}^{\sqrt{5}} 6 dx + \int_{\sqrt{5}}^{\sqrt{6}} 7 dx + \int_{\sqrt{6}}^{\sqrt{9}} 9 dx + \int_{\sqrt{7}}^{\sqrt{8}} 10 dx + \int_{\sqrt{8}}^{3} 12 dx$$
$$= 31 - 6\sqrt{2} - \sqrt{3} - \sqrt{5} - \sqrt{7} - 2\sqrt{6}$$

$$\Rightarrow$$
 a = 31, b = -6, c = -2

$$\Rightarrow a - 31, b - 0, c - 23$$

$$\Rightarrow a + b + c = 23$$

25.

26.

27.

28.

29.

30.

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