

Date: 18/05/2025



# Aakash

Medical | IIT-JEE | Foundations

Corporate Office : AESL, 3rd Floor, Incuspaze Campus-2, Plot-13, Sector-18, Udyog Vihar,  
Gurugram, Haryana-122015

Time : 3 hrs.

## Answers & Solutions

Max. Marks: 180

for

## JEE (Advanced)-2025 (Paper-1)

### PART-I : MATHEMATICS

#### SECTION 1 (Maximum Marks : 12)

- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated **according to the following marking scheme:**

Full Marks : +3 If **ONLY** the correct option is chosen;

Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);

Negative Marks : -1 In all other cases.

1. Let  $\mathbb{R}$  denote the set of all real numbers. Let  $a_i, b_i \in \mathbb{R}$  for  $i \in \{1, 2, 3\}$ .

Define the functions  $f : \mathbb{R} \rightarrow \mathbb{R}$ ,  $g : \mathbb{R} \rightarrow \mathbb{R}$ , and  $h : \mathbb{R} \rightarrow \mathbb{R}$  by

$$f(x) = a_1 + 10x + a_2x^2 + a_3x^3 + x^4,$$

$$g(x) = b_1 + 3x + b_2x^2 + b_3x^3 + x^4,$$

$$h(x) = f(x + 1) - g(x + 2).$$

If  $f(x) \neq g(x)$  for every  $x \in \mathbb{R}$ , then the coefficient of  $x^3$  in  $h(x)$  is

- (A) 8 (B) 2  
(C) -4 (D) -6

Answer (C)

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 SHREYAS LOHIYA AIR 6 100 Overall Uttar Pradesh Topper	 KUSHAGRA BAINGAHA AIR 7 100 Overall Uttar Pradesh Topper	 HARSSH A GUPTA AIR 15 100 Overall Telangana Topper	 HARSH JHA AIR 23 100 Overall Bihar (NCET) Topper	 DEVYA RUSTAGI AIR 28 100 Physics Haryana Topper	 AMOGH BANSAL AIR 29 100 Overall Haryana Topper
 SARVESH ANAND S AIR 42 100 Overall Haryana Topper	 KRISHNA AGRAWAL AIR 48 100 Physics Haryana Topper	 DISHAANTH BASU AIR 50 100 Physics Haryana Topper	 YASH KUMAR AIR 76 100 Physics Haryana Topper	 ADITYA KUMAR AIR 79 100 Physics Haryana Topper	 GURURAJ S SAJJAN AIR 92 100 Overall Haryana Topper

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### OUR JEE Champions

 Chirag Falor 4 Year Classroom 1 AIR JEE (Adv.) 2020	 Tanishka Kabra 4 Year Classroom 1 AIR-16 CRL JEE (Adv.) 2022 ALL INDIA FEMALE TOPPER	 Sanvi Jain 4 Year Classroom 1 AIR-34 CRL JEE (Main) 2024 ALL INDIA FEMALE TOPPER
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**Sol.**  $f(x+1) = a_1 + 10(x+1) + a_2(x+1)^2 + a_3(x+1)^3 + (x+1)^4$

Coefficient of  $x^3$  in  $f(x+1) = a_3 + 4$

$g(x+2) = b_1 + 3(x+2) + b_2(x+2)^2 + b_3(x+2)^3 + (x+2)^4$

Coefficient of  $x^3$  in  $g(x+2) = b_3 + 8$

$\Rightarrow$  Coefficient of  $x^3$  in  $h(x) = f(x+1) - g(x+2)$

is  $a_3 + 4 - b_3 - 8 = a_3 - b_3 - 4$

But  $f(x) \neq g(x) \forall x$

$\Rightarrow f(x) - g(x) \neq 0$

$\Rightarrow f(x) - g(x) = 0$  have no real roots

$(a_1 - b_1) + 7x + (a_2 - b_2)x^2 + (a_3 - b_3)x^3 = 0$  have no real roots

$\Rightarrow a_3 - b_3 = 0$

$\Rightarrow$  Coefficient of  $x^3$  in  $h(x) = -4$

Option (C) is correct.

2. Three students  $S_1, S_2,$  and  $S_3$  are given a problem to solve. Consider the following events:

$U$ : At least one of  $S_1, S_2,$  and  $S_3$  can solve the problem,

$V$ :  $S_1$  can solve the problem, given that neither  $S_2$  nor  $S_3$  can solve the problem,

$W$ :  $S_2$  can solve the problem and  $S_3$  cannot solve the problem,

$T$ :  $S_3$  can solve the problem.

For any event  $E$ , let  $P(E)$  denote the probability of  $E$ . If

$P(U) = \frac{1}{2}, P(V) = \frac{1}{10},$  and  $P(W) = \frac{1}{12},$

then  $P(T)$  is equal to

(A)  $\frac{13}{36}$

(B)  $\frac{1}{3}$

(C)  $\frac{19}{60}$

(D)  $\frac{1}{4}$

**Answer (A)**

**Sol.** Let  $\left. \begin{matrix} P(S_1) = a \\ P(S_2) = b \\ P(S_3) = c \end{matrix} \right\}$  they are independently solving

$U = S_1 \cup S_2 \cup S_3 \Rightarrow U^c = (\bar{S}_1 \cap \bar{S}_2 \cap \bar{S}_3)$

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<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92

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**OUR JEE Champions**

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$$\Rightarrow P(U) = 1 - P(U^c) = 1 - [(1-a)(1-b)(1-c)] = \frac{1}{2}$$

$$\Rightarrow (1-a)(1-b)(1-c) = \frac{1}{2}$$

$$P(V) = P\left(\frac{S_1}{S_2 \cap S_3}\right) = \frac{P(S_1 \cap \bar{S}_2 \cap \bar{S}_3)}{P(\bar{S}_2 \cap \bar{S}_3)} = P(S_1) = a = \frac{1}{10}$$

$$P(W) = P(S_2 \cap \bar{S}_3) = b(1-c) = \frac{1}{12}$$

$$\left(1 - \frac{1}{10}\right)(1-b)(1-c) = \frac{1}{2} \Rightarrow (1-b)(1-c) = \frac{5}{9}$$

$$\frac{b}{1-b} = \frac{1}{12} \times \frac{9}{5} = \frac{3}{20} \Rightarrow b = \frac{3}{23}$$

$$\frac{3}{23}(1-c) = \frac{1}{12} \Rightarrow 1-c = \frac{23}{36}$$

$$\Rightarrow c = \frac{13}{36}$$

$$P(T) = P(S_3) = c = \frac{13}{36}$$

3. Let  $\mathbb{R}$  denote the set of all real numbers. Define the function  $f: \mathbb{R} \rightarrow \mathbb{R}$  by

$$f(x) = \begin{cases} 2 - 2x^2 - x^2 \sin \frac{1}{x} & \text{if } x \neq 0, \\ 2 & \text{if } x = 0. \end{cases}$$

Then which one of the following statements is TRUE?

- (A) The function  $f$  is **NOT** differentiable at  $x = 0$
- (B) There is a positive real number  $\delta$ , such that  $f$  is a decreasing function on the interval  $(0, \delta)$
- (C) For any positive real number  $\delta$ , the function  $f$  is **NOT** an increasing function on the interval  $(-\delta, 0)$
- (D)  $x = 0$  is a point of local minima of  $f$

Answer (B)

Sol.  $f(x) = \begin{cases} 2 - 2x^2 - x^2 \sin \frac{1}{x} & x \neq 0 \\ 2 & x = 0 \end{cases}$

### Aakashians Rise High in JEE (Main) 2025

SHREYAS LOHIYA AIR 6 100 Overall	KUSHAGRA BAINGAHA AIR 7 100 Overall	HARSH A GUPTA AIR 15 100 Overall	HARSH JHA AIR 23 100 Overall	DEVYA RUSTAGI AIR 28 100 Overall	AMOGH BANSAL AIR 29 100 Overall
SARVESH ANAND S AIR 42 100 Maths	KRISHNA AGRAWAL AIR 48 100 Physics	DISHAANTH BASU AIR 50 100 Physics	YASH KUMAR AIR 76 100 Physics	ADITYA KUMAR AIR 79 100 Physics	GURURAJ S SAJJAN AIR 92 100 Overall

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### OUR JEE Champions

Chirag Falor 4 Year Classroom 1 AIR JEE (Adv.) 2020	Tanishka Kabra 4 Year Classroom 1 AIR-16 CRL JEE (Adv.) 2022 ALL INDIA FEMALE TOPPER	Sanvi Jain 4 Year Classroom 1 AIR-36 CRL JEE (Main) 2024 ALL INDIA FEMALE TOPPER
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$$\lim_{x \rightarrow 0} f(x) = 2 = f(0) \quad \therefore f(x) \text{ is continuous}$$

$$f'(0) = \lim_{h \rightarrow 0} \frac{f(h) - f(0)}{h}$$

$$\lim_{h \rightarrow 0} \frac{2 - 2h^2 - h^2 \sin\left(\frac{1}{h}\right) - 2}{h}$$

$$\lim_{h \rightarrow 0} \frac{-2h - h \sin\left(\frac{1}{h}\right)}{1} = 0$$

$$\therefore f'(0) = 0$$

$\therefore f(x)$  is differentiable at  $x = 0$

$$\text{RHD} = \lim_{h \rightarrow 0^+} -h \left( 2 + \sin\left(\frac{1}{h}\right) \right) < 0$$

$$\text{LHD} = \lim_{h \rightarrow 0^-} -h \left( 2 + \sin\left(\frac{1}{h}\right) \right) > 0$$

$\therefore x = 0$  is a point of maxima

$\therefore$  In  $(0, \delta)$  function is decreasing ( $\delta > 0$ )

Option (B) is correct

In  $(-\delta, 0)$  function will be increasing ( $\delta > 0$ )

Option (C) is incorrect

4. Consider the matrix

$$P = \begin{pmatrix} 2 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 3 \end{pmatrix}$$

Let the transpose of a matrix  $X$  be denoted by  $X^T$ . Then the number of  $3 \times 3$  invertible matrices  $Q$  with integer entries, such that  $Q^{-1} = Q^T$  and  $PQ = QP$ ,

(A) 32

(B) 8

(C) 16

(D) 24

**Answer (C)**

**Sol.** As  $PQ = QP$

$$\therefore \begin{bmatrix} 2 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 3 \end{bmatrix} \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} 2 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 3 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} 2a & 2b & 2c \\ 2d & 2e & 2f \\ 3g & 3h & 3i \end{bmatrix} = \begin{bmatrix} 2a & 2b & 3c \\ 2d & 2e & 3f \\ 2g & 2h & 3i \end{bmatrix}$$

## Aakashians Rise High in JEE (Main) 2025

<b>SHREYAS LOHIYA</b> AIR 6 100 Overall	<b>KUSHAGRA BAINGAHA</b> AIR 7 100 Overall	<b>HARSSH A GUPTA</b> AIR 15 100 Overall	<b>HARSH JHA</b> AIR 23 100 Overall	<b>DEVYA RUSTAGI</b> AIR 28 100 Overall	<b>AMOGH BANSAL</b> AIR 29 100 Overall
<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92 100 Overall

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$$\Rightarrow c = 0, f = 0, h = 0, g = 0$$

$$\text{We get } Q = \begin{bmatrix} a & b & 0 \\ c & d & 0 \\ 0 & 0 & e \end{bmatrix}$$

$$\text{Given } QQ^T = I$$

$$\Rightarrow \begin{bmatrix} a & b & 0 \\ c & d & 0 \\ 0 & 0 & e \end{bmatrix} \begin{bmatrix} a & c & 0 \\ b & d & 0 \\ 0 & 0 & e \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} a^2 + b^2 & ac + bd & 0 \\ ac + bd & c^2 + d^2 & 0 \\ 0 & 0 & e^2 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\Rightarrow a^2 + b^2 = 1, ac + bd = 0, c^2 + d^2 = 1, e^2 = 1$$

**Case I:**  $(a, b) = (0, 1)$  or  $(0, -1)$ ,  $(c, d) = (1, 0)$  or  $(-1, 0)$

**Case II:**  $(a, b) = (1, 0)$  or  $(-1, 0)$ ,  $(c, d) = (0, 1)$  or  $(0, -1)$

Therefore total possible  $Q = 16$

**SECTION 2 (Maximum Marks : 12)**

- This section contains **THREE (03)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated **according to the following marking scheme:**

<i>FULL MARKS</i>	: +4	<b>ONLY</b> if (all) the correct option(s) is(are) chosen;
<i>Partial Marks</i>	: +3	If all the four options are correct but <b>ONLY</b> three options are chosen;
<i>Partial Marks</i>	: +2	If three or more options are correct but <b>ONLY</b> two options are chosen, both of which are correct;
<i>Partial Marks</i>	: +1	If two or more options are correct but <b>ONLY</b> one option is chosen and it is a correct option;
<i>Zero Marks</i>	: 0	If none of the options is chosen (i.e. the question is unanswered);
<i>Negative Marks</i>	: -2	In all other cases.

5. Let  $L_1$  be the line of intersection of the planes given by the equations

$$2x + 3y + z = 4 \text{ and } x + 2y + z = 5.$$

Let  $L_2$  be the line passing through the point  $P(2, -1, 3)$  and parallel to  $L_1$ . Let  $M$  denote the plane given by the equation

$$2x + y - 2z = 6$$

Suppose that the line  $L_2$  meets the plane  $M$  at the point  $Q$ . Let  $R$  be the foot of the perpendicular drawn from  $P$  to the plane  $M$ .

**Aakashians Rise High in JEE (Main) 2025**

<b>SHREYAS LOHIYA</b> AIR 6 <small>Overall Rank</small>	<b>KUSHAGRA BAINGAHA</b> AIR 7 <small>Overall Rank</small>	<b>HARSSH A GUPTA</b> AIR 15 <small>Overall Rank</small>	<b>HARSH JHA</b> AIR 23 <small>Overall Rank</small>	<b>DEVYA RUSTAGI</b> AIR 28 <small>Overall Rank</small>	<b>AMOGH BANSAL</b> AIR 29 <small>Overall Rank</small>
<b>SARVESH ANAND S</b> AIR 42 <small>Overall Rank</small>	<b>KRISHNA AGRAWAL</b> AIR 48 <small>Overall Rank</small>	<b>DISHAANTH BASU</b> AIR 50 <small>Overall Rank</small>	<b>YASH KUMAR</b> AIR 76 <small>Overall Rank</small>	<b>ADITYA KUMAR</b> AIR 79 <small>Overall Rank</small>	<b>GURURAJ S SAJJAN</b> AIR 92 <small>Overall Rank</small>

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**OUR JEE Champions**

<b>Chirag Falor</b> 4 Year Classroom AIR-1 JEE (Adv.) 2020 <small>ALL INDIA FEMALE TOPPER</small>	<b>Tanishka Kabra</b> 4 Year Classroom AIR-16 CRL JEE (Adv.) 2022 <small>ALL INDIA FEMALE TOPPER</small>	<b>Sanvi Jain</b> 4 Year Classroom AIR-36 CRL JEE (Main) 2024 <small>ALL INDIA FEMALE TOPPER</small>
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Then which of the following statements is (are) TRUE?

- (A) The length of the line segment  $PQ$  is  $9\sqrt{3}$
- (B) The length of the line segment  $QR$  is 15
- (C) The area of  $\Delta PQR$  is  $\frac{3}{2}\sqrt{234}$
- (D) The acute angle between the line segments  $PQ$  and  $PR$  is  $\cos^{-1}\left(\frac{1}{2\sqrt{3}}\right)$

**Answer (A, C)**

**Sol.**  $L_1 : 2x + 3y + z = 4$   
 $x + 2y + z = 5$

$\therefore$  line  $L_1$  in standard form is

$$\frac{x+7}{1} = \frac{y-6}{-1} = \frac{z}{1}$$

and equation of line  $L_2$  is:

$$\frac{x-2}{1} = \frac{y+1}{-1} = \frac{z-3}{1}$$

Equation of plane  $M : 2x + y - 2z = 6$ .

Let coordinate of  $Q = (\lambda + 2, -\lambda - 1, \lambda + 3)$ .

$\therefore Q$  lies on plane  $M$

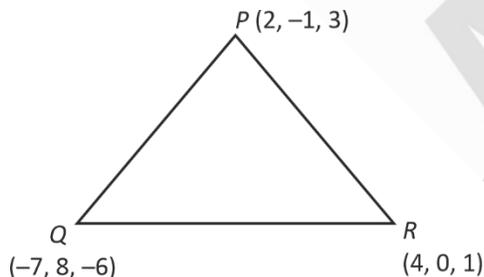
$$\therefore \lambda = -9$$

$\therefore$  coordinate of  $Q = (-7, 8, -6)$ .

For foot of perpendicular  $R(x_1, y_1, z_1)$

$$\frac{x_1-2}{2} = \frac{y_1+1}{1} = \frac{z_1-3}{-2} = \frac{-(4-1-6-6)}{9}$$

$\therefore$  Coordinate of  $R = (4, 0, 1)$



$$\therefore PQ = 9\sqrt{3} \text{ units}$$

$$QR = \sqrt{234} \text{ units}$$

$$PR = 3 \text{ units}$$

## Aakashians Rise High in JEE (Main) 2025

<b>SHREYAS LOHIYA</b> AIR 6 100 Overall	<b>KUSHAGRA BAINGAHA</b> AIR 7 100 Overall	<b>HARSSH A GUPTA</b> AIR 15 100 Overall	<b>HARSH JHA</b> AIR 23 100 Overall	<b>DEVYA RUSTAGI</b> AIR 28 100 Overall	<b>AMOGH BANSAL</b> AIR 29 100 Overall
<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92 100 Overall

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### OUR JEE Champions

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Let  $\theta$  be acute angle between  $PQ$  and  $PR$ , then

$$\cos\theta = \frac{1}{3\sqrt{3}} \text{ and } \sin\theta = \sqrt{\frac{26}{27}}$$

$$\text{Area of } \Delta PQR = \frac{1}{2} \cdot PQ \cdot PR \cdot \sin\theta = \frac{3}{2}\sqrt{234} \text{ sq. units}$$

6. Let  $\mathbb{N}$  denote the set of all natural numbers, and  $\mathbb{Z}$  denote the set of all integers. Consider the functions  $f: \mathbb{N} \rightarrow \mathbb{Z}$  and  $g: \mathbb{Z} \rightarrow \mathbb{N}$  defined by

$$f(n) = \begin{cases} (n+1)/2 & \text{if } n \text{ is odd,} \\ (4-n)/2 & \text{if } n \text{ is even,} \end{cases}$$

and

$$g(n) = \begin{cases} 3+2n & \text{if } n \geq 0, \\ -2n & \text{if } n < 0. \end{cases}$$

Define  $(g \circ f)(n) = g(f(n))$  for all  $n \in \mathbb{N}$ , and  $(f \circ g)(n) = f(g(n))$  for all  $n \in \mathbb{Z}$ .

Then which of the following statements is (are) TRUE?

- (A)  $g \circ f$  is **NOT** one-one and  $g \circ f$  is **NOT** onto  
 (B)  $f \circ g$  is **NOT** one-one but  $f \circ g$  is onto  
 (C)  $g$  is one-one and  $g$  is onto  
 (D)  $f$  is **NOT** one-one but  $f$  is onto

Answer (A, D)

Sol.  $f(n) = \begin{cases} \frac{n+1}{2}, & n=2k+1 \\ \frac{4-n}{2}, & n=2k \end{cases} = \begin{cases} k+1, & k \in \mathbb{N} \cup \{0\} \\ 2-k, & k \in \mathbb{N} \end{cases}$

at  $k=0, f(1) = 1 = f(2) = 1 \Rightarrow f$  is not one-one

$2-k$  covers all integers  $\{1, 0, -1, \dots\}$

$k+1$  covers  $\{1, 2, 3, \dots\}$

$\Rightarrow f(n)$  covers all integers  $\Rightarrow f(n)$  is onto but not one-one

$$g(n) = \begin{cases} 3+2n, & n \geq 0 \\ -2n, & n < 0 \end{cases}$$

Notice that  $1 \notin \text{range of } g(x)$  as  $3+2n \neq 1, n \geq 0$   
 and  $-2n \neq 1, n < 0$

$\Rightarrow g(n)$  is not onto

$$g(f(n)) = \begin{cases} 3+2f(n), & f(n) \geq 0 \\ -2f(n), & f(n) < 0 \end{cases} = \begin{cases} 3+2\left(\frac{n+1}{2}\right), & n=2k+1 \\ 3+2\left(\frac{4-n}{2}\right), & n=2k \end{cases}$$

$$= \begin{cases} n+4, & n=2k+1 \\ 7-n, & n=2k \end{cases}$$

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$g(f(n))$  is always odd  $\Rightarrow$  not onto

at  $g(f(1)) = 5 = g(f(2)) \Rightarrow 0$  not one-one

$$f(g(n)) = \begin{cases} \frac{g(n)+1}{2}, & g(n) \text{ is odd natural} \\ \frac{4-g(n)}{2}, & g(n) \text{ is even natural} \end{cases} = \begin{cases} n+2, & n \geq 0 \\ n+2, & n < 0 \end{cases}$$

$\Rightarrow (n+2) \forall n \Rightarrow f(g(n))$  is one-one

7. Let  $\mathbb{R}$  denote the set of all real numbers. Let  $z_1 = 1 + 2i$  and  $z_2 = 3i$  be two complex numbers, where  $i = \sqrt{-1}$ . Let  $S = \{(x, y) \in \mathbb{R} \times \mathbb{R} : |x + iy - z_1| = 2|x + iy - z_2|\}$ .

Then which of the following statements is (are) TRUE?

(A)  $S$  is a circle with centre  $\left(-\frac{1}{3}, \frac{10}{3}\right)$

(B)  $S$  is a circle with centre  $\left(\frac{1}{3}, \frac{8}{3}\right)$

(C)  $S$  is a circle with radius  $\frac{\sqrt{2}}{3}$

(D)  $S$  is a circle with radius  $\frac{2\sqrt{2}}{3}$

**Answer (A, D)**

**Sol.**  $|x + iy - (1 + 2i)| = 2|x + iy - (3i)|$   
 $\Rightarrow |x - 1 + (y - 2)i| = 2|x + (y - 3)i|$   
 $\Rightarrow \sqrt{(x-1)^2 + (y-2)^2} = 2\sqrt{x^2 + (y-3)^2}$   
 $\Rightarrow (x-1)^2 + (y-2)^2 = 4(x^2 + (y-3)^2)$   
 $\Rightarrow x^2 + y^2 - 2x - 4y + 5 = 4(x^2 + y^2 - 6y + 9)$   
 $\Rightarrow 3x^2 + 3y^2 + 2x - 20y + 31 = 0$   
 $\Rightarrow x^2 + y^2 + \frac{2x}{3} - \frac{20y}{3} + \frac{31}{3} = 0$   
 $\Rightarrow \text{Centre} \equiv \left(-\frac{1}{3}, \frac{10}{3}\right)$

Radius =  $\sqrt{\left(-\frac{1}{3}\right)^2 + \left(\frac{10}{3}\right)^2 - \frac{31}{3}} = \sqrt{\frac{8}{9}}$   
 $= \frac{2\sqrt{2}}{3}$

**Aakashians Rise High in JEE (Main) 2025**

<b>SHREYAS LOHIYA</b> AIR 6 100 Overall	<b>KUSHAGRA BAINGAHA</b> AIR 7 100 Overall	<b>HARSH A GUPTA</b> AIR 15 100 Overall	<b>HARSH JHA</b> AIR 23 100 Overall	<b>DEVYA RUSTAGI</b> AIR 28 100 Overall	<b>AMOGH BANSAL</b> AIR 29 Haranya Topper
<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92

\*Aakash Invictus Contact Program and many more...

**OUR JEE Champions**

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SECTION 3 (Maximum Marks : 24)

- This section contains **SIX (06)** questions.
- The answer to each question is a **NUMERICAL VALUE**.
- For each question, enter the correct numerical value of the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- If the numerical value has more than two decimal places, **truncate/round-off** the value to **TWO** decimal places.
- Answer to each question will be evaluated **according to the following marking scheme**:

Full Marks : +4 If **ONLY** the correct numerical value is entered in the designated place;  
 Zero Marks : 0 In all other cases.

8. Let the set of all relations  $R$  on the set  $\{a, b, c, d, e, f\}$ , such that  $R$  is reflexive and symmetric, and  $R$  contains exactly 10 elements, be denoted by  $\mathcal{S}$ .

Then the number of elements in  $\mathcal{S}$  is \_\_\_\_\_.

**Answer (105.00)**

**Sol.** Let  $A = \{a, b, c, d, e, f\}$

$R \subset A \times A$ ,  $R$  is reflexive,  $\Rightarrow (x, x) \in R \forall x \in R$

$\Rightarrow \binom{6}{C_1} \Rightarrow 6$  elements

We need 4 elements but since  $R$  is symmetric, we want to pairs  $(\alpha, \beta)$  and  $(\gamma, \delta)$  such that

$(\alpha, \beta) \in R$  and  $(\gamma, \delta) \Rightarrow (\beta, \alpha) \in R$  and  $(\delta, \gamma) \in R$

$\Rightarrow$  We need to choose the pairs

$(\alpha, \beta)$  and  $(\gamma, \delta)$

$\Rightarrow$  Total unordered pairs

$\Rightarrow \binom{6}{C_2} = 15$  pairs

Out of these we need two pairs

$\Rightarrow \binom{15}{C_2} = \frac{15 \times 14}{2} = 105$

9. For any two points  $M$  and  $N$  in the  $XY$ -plane, let  $\overline{MN}$  denote the vector from  $M$  to  $N$ , and  $\vec{0}$  denote the zero vector. Let  $P, Q$  and  $R$  be three distinct points in the  $XY$ -plane. Let  $S$  be a point inside the triangle  $\Delta PQR$  such that

$$\overline{SP} + 5\overline{SQ} + 6\overline{SR} = \vec{0}.$$

Let  $E$  and  $F$  be the mid-points of the sides  $PR$  and  $QR$ , respectively. Then the value of

$$\frac{\text{length of the line segment } EF}{\text{length of the line segment } ES}$$

is \_\_\_\_\_.

**Answer (01.20)**

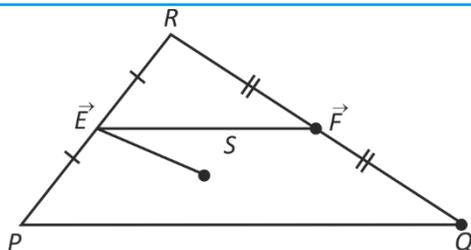
**Aakashians Rise High in JEE (Main) 2025**

<b>SHREYAS LOHIYA</b> AIR 6 All India Topper 100 Overall	<b>KUSHAGRA BAINGAHA</b> AIR 7 All India Topper 100 Overall	<b>HARSH A GUPTA</b> AIR 15 All India Topper 100 Overall	<b>HARSH JHA</b> AIR 23 All India Topper 100 Overall	<b>DEVYA RUSTAGI</b> AIR 28 All India Topper 100 Overall	<b>AMOGH BANSAL</b> AIR 29 All India Topper 100 Overall
<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92 100 Overall

**OUR JEE Champions**

<b>Chirag Falor</b> 4 Year Classroom 1 AIR JEE (Adv.) 2020	<b>Tanishka Kabra</b> 4 Year Classroom 1 AIR-16 CRL JEE (Adv.) 2022 ALL INDIA FEMALE TOPPER	<b>Sanvi Jain</b> 4 Year Classroom 1 AIR-36 CRL JEE (Main) 2024 ALL INDIA FEMALE TOPPER
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Sol.



$$\vec{SP} + 5\vec{SQ} + 6\vec{SR} = \vec{0}$$

$$\vec{P} - \vec{S} + 5(\vec{Q} - \vec{S}) + 6(\vec{R} - \vec{S}) = \vec{0}$$

$$\vec{P} + 5\vec{Q} + 6\vec{R} - 12\vec{S} = \vec{0}$$

$$|\vec{EF}| = \frac{1}{2}|\vec{PQ}| = |\vec{F} - \vec{E}| = \left| \frac{\vec{Q} + \vec{R}}{2} - \frac{\vec{R} + \vec{P}}{2} \right| = \left| \frac{\vec{P} - \vec{Q}}{2} \right|$$

$$|\vec{ES}| = |S - \vec{E}| = \left| \frac{\vec{P} + \vec{R}}{2} - \vec{S} \right|$$

$$= \left| \frac{\vec{P} + \vec{R}}{2} - \left( \frac{\vec{P} + 5\vec{Q} + 6\vec{R}}{12} \right) \right|$$

$$= \left| \frac{6\vec{P} + 6\vec{R} - \vec{P} - 5\vec{Q} - 6\vec{R}}{12} \right| = \left| \frac{5\vec{P} - 5\vec{Q}}{12} \right|$$

$$\Rightarrow \frac{|\vec{EF}|}{|\vec{ES}|} = \frac{\frac{|\vec{P} - \vec{Q}|}{2}}{\frac{5}{12}|\vec{P} - \vec{Q}|} = \frac{6}{5} = \frac{12}{10} = 0.120$$

10. Let  $S$  be the set of all seven-digit numbers that can be formed using the digits 0, 1 and 2. For example, 2210222 is in  $S$ , but 0210222 is **NOT** in  $S$ .

Then the number of elements  $x$  in  $S$  such that at least one of the digits 0 and 1 appears exactly twice in  $x$ , is equal to \_\_\_\_\_.

Answer (762.00)

Sol. A : 0 exactly twice

B : 1 exactly twice

C : 0 and 1 exactly twice

$$\Rightarrow n(A) = {}^6C_2 \cdot 2^5 \quad [0 \text{ can't be leftmost digit}]$$

$$= 480$$

### Aakashians Rise High in JEE (Main) 2025

<b>SHREYAS LOHIYA</b> AIR 6 100 Overall	<b>KUSHAGRA BAINGAHA</b> AIR 7 100 Overall	<b>HARSH A GUPTA</b> AIR 15 100 Overall	<b>HARSH JHA</b> AIR 23 100 Overall	<b>DEVYA RUSTAGI</b> AIR 28 100 Overall	<b>AMOGH BANSAL</b> AIR 29 100 Overall
<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92 100 Overall

### OUR JEE Champions

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B : (1 at leftmost place)  $\cup$  (1 is not at leftmost place)

$$= {}^6C_1 \cdot 2^5 + {}^6C_2 \cdot 2^4 = 432$$

C : 0011222, no. of valid 7 digit number

$$\Rightarrow \frac{7!}{3!2!2!} - \frac{6!}{3!2!} = 150$$

$$\Rightarrow \text{Total numbers} = 480 + 432 - 150$$

$$\Rightarrow 762$$

11. Let  $\alpha$  and  $\beta$  be the real numbers such that

$$\lim_{x \rightarrow 0} \frac{1}{x^3} \left( \frac{\alpha}{2} \int_0^x \frac{1}{1-t^2} dt + \beta x \cos x \right) = 2.$$

Then the value of  $\alpha + \beta$  is \_\_\_\_\_.

**Answer (02.40)**

Sol.  $\lim_{x \rightarrow 0} \frac{1}{x^3} \left( \frac{\alpha}{2} \int_0^x \frac{1}{1-t^2} dt + \beta x \cos x \right) = 2$   $\left( \left[ \frac{0}{0} \right] \text{ form} \right)$

$$\lim_{x \rightarrow 0} \frac{\frac{\alpha}{2} \cdot \left( \frac{1}{1-x^2} \right) \cdot 1 + \beta \cos x - \beta x \sin x}{3x^2}$$

$$\Rightarrow \boxed{\frac{\alpha}{2} + \beta = 0}$$

Again differentiate,

$$\lim_{x \rightarrow 0} \frac{\frac{\alpha}{2} (-1)(1-x^2)^{-2} (-2x) - \beta \sin x - \beta \sin x - \beta x \cos x}{6x}$$

Again differentiate,

$$\lim_{x \rightarrow 0} \frac{\alpha(-2)(1-x^2)^{-3}(-2x)^2 + \alpha(1-x^2)^{-2} - 2\beta \cos x - \beta \cos x + \beta x \sin x}{6}$$

$$\Rightarrow \frac{\alpha - 2\beta - \beta}{6} = 2$$

$$\Rightarrow \alpha - 3\beta = 12$$

## Aakashians Rise High in JEE (Main) 2025

<b>SHREYAS LOHIYA</b> AIR 6 100 Overall	<b>KUSHAGRA BAINGAHA</b> AIR 7 100 Overall	<b>HARSH A GUPTA</b> AIR 15 100 Overall	<b>HARSH JHA</b> AIR 23 100 Overall	<b>DEVYA RUSTAGI</b> AIR 28 100 Overall	<b>AMOGH BANSAL</b> AIR 29 100 Overall
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$$\alpha + 2\beta = 0$$

$$-5\beta = 12$$

$$\beta = \frac{-12}{5} \text{ \& } \alpha = \frac{24}{5}$$

$$\alpha + \beta = \frac{12}{5} = 2.40$$

12. Let  $\mathbb{R}$  denote the set of all real numbers. Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  be a function such that  $f(x) > 0$  for all  $x \in \mathbb{R}$ , and  $f(x+y) = f(x)f(y)$  for all  $x, y \in \mathbb{R}$ . Let the real numbers  $a_1, a_2, \dots, a_{50}$  be in an arithmetic progression. If  $f(a_{31}) = 64f(a_{25})$  and

$$\sum_{i=1}^{50} f(a_i) = 3(2^{25} + 1),$$

then the value of

$$\sum_{i=6}^{30} f(a_i)$$

is \_\_\_\_\_.

**Answer (96.00)**

**Sol.**  $f(x) = a^x \forall x, y \in \mathbb{R}$

$a_r = a_1 + (r-1)d$ . {Let  $d$  is common difference of A. P}

$$\sum_{i=1}^{50} f(a_i) = \sum_{i=1}^{50} a^{a_1 + (i-1)d}$$

$$= a^{a_1 - d} \sum_{i=1}^{50} a^{id} = a^{a_1 - d} = \frac{a^d (1 - (a^d)^{50})}{1 - a^d}$$

$$= a^{a_1 - d} \cdot \frac{a^d (1 - a^{50d})}{1 - a^d}$$

$$\Rightarrow a^{a_1} \cdot \frac{(1 - a^{50d})}{1 - a^d} = 3(2^{25} + 1) \quad \dots(i)$$

$$f(a_{31}) = 64f(a_{25})$$

$$\Rightarrow a^{a_1 + 30d} = 64 \cdot a^{a_1 + 24d}$$

$$\Rightarrow a^{6d} = 64 = 2^6$$

$$a^d = 2 \quad \dots(ii)$$

Using (i) and (ii)

$$\Rightarrow \frac{a^{a_1} (1 - 2^{50})}{1 - 2} = 3(2^{25} + 1)$$

## Aakashians Rise High in JEE (Main) 2025

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\*Aakash Invicta Contact Program and many more...

### OUR JEE Champions

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$$\Rightarrow a^{a^1} (2^{25} - 1)(2^{25} + 1) = 3(2^{25} + 1)$$

$$\Rightarrow a^{a^1} = \frac{3}{2^{25} - 1} \quad \dots\text{(iii)}$$

$$\begin{aligned} \text{Now, } \sum_{i=6}^{30} f(a_i) &= a^{a^1-d} \sum_{i=6}^{30} a^{id} = a^{a^1-d} \cdot \frac{a^{6d}(a^{25d} - 1)}{(a^d - 1)} \\ &= a^{a^1} \cdot (a^d)^5 \frac{|(a^d)^{25} - 1|}{a^d - 1} \\ &= \frac{3}{2^{25} - 1} \times \frac{2^5 \cdot (2^{25} - 1)}{2 - 1} \\ &= \boxed{96.00} \end{aligned}$$

13. For all  $x > 0$ , let  $y_1(x)$ ,  $y_2(x)$ , and  $y_3(x)$  be the functions satisfying

$$\begin{aligned} \frac{dy_1}{dx} - (\sin x)^2 y_1 &= 0, y_1(1) = 5, \\ \frac{dy_2}{dx} - (\cos x)^2 y_2 &= 0, y_2(1) = \frac{1}{3}, \\ \frac{dy_3}{dx} - \left(\frac{2-x^3}{x^3}\right) y_3 &= 0, y_3(1) = \frac{3}{5e}, \end{aligned}$$

respectively. Then

$$\lim_{x \rightarrow 0^+} \frac{y_1(x)y_2(x)y_3(x) + 2x}{e^{3x} \sin x}$$

is equal to \_\_\_\_\_.

Answer (02.00)

Sol.  $\frac{dy_1}{dx} - (\sin^2 x)y_1 = 0$

$$\Rightarrow \int \frac{dy_1}{y_1} = \int \sin^2 x dx$$

$$\Rightarrow \int \frac{dy_1}{y_1} = \int \frac{1 - \cos 2x}{2} dx$$

$$\Rightarrow \ln|y_1| = \frac{1}{2} \left( x - \frac{\sin 2x}{2} \right) + C_1$$

$$\Rightarrow y_1 = e^{\frac{1}{2} \left( x - \frac{\sin 2x}{2} \right) + C_1}$$

$$\therefore y_1(1) = 5$$

$$\Rightarrow C_1 = \ln 5 - \frac{1}{2} + \frac{\sin 2}{4}$$

## Aakashians Rise High in JEE (Main) 2025

<b>SHREYAS LOHIYA</b> AIR 6 100 Overall	<b>KUSHAGRA BAINGAHA</b> AIR 7 100 Overall	<b>HARSH A GUPTA</b> AIR 15 100 Overall	<b>HARSH JHA</b> AIR 23 100 Overall	<b>DEVYA RUSTAGI</b> AIR 28 100 Overall	<b>AMOGH BANSAL</b> AIR 29 100 Overall
<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92 100 Physics

\*Aakash Invictus Contact Program and many more...

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$$\Rightarrow y_1 = e^{2\left(x - \frac{\sin 2x}{2}\right) + \ln 5 - \frac{1}{2} + \frac{\sin 2}{4}} \dots(1)$$

and  $\frac{dy_2}{dx} = (\cos^2 x)y_2$

$$\Rightarrow \int \frac{dy_2}{y_2} = \int \cos^2 x dx = \int \frac{1 + \cos 2x}{2} dx$$

$$\Rightarrow \ln|y_2| = \frac{1}{2}\left(x + \frac{\sin 2x}{2}\right) + C_2$$

$$\therefore y_2(1) = \frac{1}{3}$$

$$\Rightarrow C_2 = -\ln 3 - \frac{1}{2} - \frac{\sin 2}{4}$$

$$\Rightarrow y_2 = e^{2\left(x + \frac{\sin 2x}{2}\right) - \ln 3 - \frac{1}{2} - \frac{\sin 2}{4}} \dots(2)$$

and  $\frac{dy_3}{dx} = \left(\frac{2-x^3}{x^3}\right)y_3$

$$\Rightarrow \int \frac{dy_3}{y_3} = \int \left(\frac{2}{x^3} - 1\right) dx$$

$$\Rightarrow \ln|y_3| = -\frac{1}{x^2} - x + C_3$$

$$\therefore y_3(1) = \frac{3}{5e}$$

$$\Rightarrow C_3 = 1 + \ln 3 - \ln 5$$

$$\Rightarrow y_3 = e^{-\frac{1}{x^2} - x + 1 + \ln 3 - \ln 5} \dots(3)$$

From eq<sup>n</sup> (1), (2) and (3)

$$y_1(x) y_2(x) y_3(x) = e^{-\frac{1}{x^2}}$$

$$\therefore \lim_{x \rightarrow 0^+} \frac{y_1(x) y_2(x) y_3(x) + 2x}{e^{3x} \sin x}$$

$$= \lim_{x \rightarrow 0^+} \frac{e^{-\frac{1}{x^2}} + 2x}{e^{3x} \sin x}$$

## Aakashians Rise High in JEE (Main) 2025

<b>SHREYAS LOHIYA</b> AIR 6 100 Overall 100 Physics	<b>KUSHAGRA BAINGAHA</b> AIR 7 100 Overall 100 Physics	<b>HARSH A GUPTA</b> AIR 15 100 Overall 100 Physics	<b>HARSH JHA</b> AIR 23 100 Overall 100 Physics	<b>DEVYA RUSTAGI</b> AIR 28 100 Overall 100 Physics	<b>AMOGH BANSAL</b> AIR 29 100 Overall 100 Physics
<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92 100 Physics

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<b>Chirag Falor</b> 4 Year Classroom 1 AIR JEE (Adv.) 2020	<b>Tanishka Kabra</b> 4 Year Classroom 1 AIR-16 CRL JEE (Adv.) 2022 ALL INDIA FEMALE TOPPER	<b>Sanvi Jain</b> 4 Year Classroom 1 AIR-36 CRL JEE (Main) 2024 ALL INDIA FEMALE TOPPER
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$$= \lim_{x \rightarrow 0^+} \frac{\frac{1}{x} e^{-\frac{1}{x^2}} + 2}{e^{3x} \left( \frac{\sin x}{x} \right)}$$

$$= \frac{0 + 2}{1 \times 1} = 2$$

$$\therefore \lim_{x \rightarrow 0^+} \frac{1}{x} e^{-\frac{1}{x^2}} = 0$$

**SECTION 4 (Maximum Marks : 12)**

- This section contains **THREE (03)** Matching List Sets.
- Each set has **ONE** Multiple Choice Question.
- Each set has **TWO** lists: **List-I** and **List-II**.
- **List-I** has **Four** entries (P), (Q), (R) and (S) and **List-II** has **Five** entries (1), (2), (3), (4) and (5).
- **FOUR** options are given in each Multiple Choice Question based on **List-I** and **List-II** and **ONLY ONE** of these four options satisfies the condition asked in the Multiple Choice Question.
- Answer to each question will be evaluated **according to the following marking scheme:**

*Full Marks* : +4 **ONLY** if the option corresponding to the correct combination is chosen;

*Zero Marks* : 0 If none of the options is chosen (i.e. the question is unanswered);

*Negative Marks* : -1 In all other cases.

14. Consider the following frequency distribution:

Value	4	5	8	9	6	12	11
Frequency	5	$f_1$	$f_2$	2	1	1	3

Suppose that the sum of the frequencies is 19 and the median of this frequency distribution is 6.

For the given frequency distribution, let  $\alpha$  denote the mean deviation about the mean,  $\beta$  denote the mean deviation about the median, and  $\sigma^2$  denote the variance.

Match each entry in List-I to the correct entry in List-II and choose the correct option.

	List-I		List-II
(P)	$7f_1 + 9f_2$ is equal to	(1)	146
(Q)	$19\alpha$ is equal to	(2)	47
(R)	$19\beta$ is equal to	(3)	48
(S)	$19\alpha^2$ is equal to	(4)	145
		(5)	55

(A) (P) → (5) (Q) → (3) (R) → (2) (S) → (4)

(B) (P) → (5) (Q) → (2) (R) → (3) (S) → (1)

(C) (P) → (5) (Q) → (3) (R) → (2) (S) → (1)

(D) (P) → (3) (Q) → (2) (R) → (5) (S) → (4)

Answer (C)

**Aakashians Rise High in JEE (Main) 2025**

**SHREYAS LOHIYA** AIR 6 (100 Maths)  
**KUSHAGRA BAINGAHA** AIR 7 (100 Physics)  
**HARSSH A GUPTA** AIR 15 (100 Physics)  
**HARSH JHA** AIR 23 (100 Physics)  
**DEVYA RUSTAGI** AIR 28 (100 Maths)  
**AMOGH BANSAL** AIR 29 (Haranya Topper)  
**SARVESH ANAND S** AIR 42 (100 Maths)  
**KRISHNA AGRAWAL** AIR 48 (100 Physics)  
**DISHAANTH BASU** AIR 50 (100 Physics)  
**YASH KUMAR** AIR 76 (100 Physics)  
**ADITYA KUMAR** AIR 79 (100 Physics)  
**GURURAJ S SAJJAN** AIR 92 (and many more...)

**OUR JEE Champions**

**Chirag Falor** 4 Year Classroom AIR-16 CRL JEE (Adv.) 2020  
**Tanishka Kabra** 4 Year Classroom AIR-16 CRL JEE (Adv.) 2022 (ALL INDIA FEMALE TOPPER)  
**Sanvi Jain** 4 Year Classroom AIR-36 CRL JEE (Main) 2024 (ALL INDIA FEMALE TOPPER)

Sol.

Value ( $x_i$ )	$f_i$	$cf$	$f_i x_i$
4	5	5	20
5	$f_1$	$5 + f_1$	20
6	1	$6 + f_1$	6
8	$f_2$	$6 + f_1 + f_2$	24
9	2	$8 + f_1 + f_2$	18
11	3	$11 + f_1 + f_2$	33
12	1	$12 + f_1 + f_2$	12

$$12 + f_1 + f_2$$

$$\Sigma f_i x_i = 133$$

Given  $12 + f_1 + f_2 = 19$

Median = 6

$$\Rightarrow f_1 + f_2 = 7$$

$$\text{Median} = \left(\frac{N+1}{2}\right)^{\text{th}} \text{ term} = \left(\frac{19+1}{2}\right)^{\text{th}} \text{ term} = 10^{\text{th}} \text{ term}$$

$$\Rightarrow 6 + f_1 = 10 \Rightarrow f_1 = 4 \text{ and } f_2 = 3$$

$$\therefore 7f_1 + 9f_2 = 7 \times 4 + 9 \times 3$$

$$= 55 \Rightarrow P \rightarrow 5$$

$$\text{Mean } (\bar{X}) = \frac{\Sigma f_i x_i}{\Sigma f_i} = \frac{133}{19} = 7$$

$$\text{Mean deviation about mean } (\alpha) = \frac{\Sigma f_i |x_i - \bar{x}|}{\Sigma f_i}$$

$$= \frac{5(3) + 4(2) + 1(1) + 3(1) + 2(2) + 3(4) + 1(5)}{19} = \frac{48}{19}$$

$$\Rightarrow 19\alpha = 48 \quad Q \rightarrow 3$$

Mean deviation about median ( $\beta$ )

$$= \frac{\Sigma f_i |x_i - M|}{\Sigma f_i}$$

$$= \frac{5(2) + 4(1) + 1(0) + 3(2) + 2(3) + 3(5) + 1(6)}{19}$$

$$= \frac{47}{19}$$

$$19\beta = 47$$

$$R \rightarrow 2$$

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<b>SHREYAS LOHIYA</b> AIR 6 100 Overall 100 Physics	<b>KUSHAGRA BAINGAHA</b> AIR 7 100 Overall 100 Physics	<b>HARSH A GUPTA</b> AIR 15 100 Overall 100 Physics	<b>HARSH JHA</b> AIR 23 100 Overall 100 Physics	<b>DEVYA RUSTAGI</b> AIR 28 100 Overall 100 Physics	<b>AMOGH BANSAL</b> AIR 29 100 Overall 100 Physics
<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92 100 Physics

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$$\begin{aligned} \text{Variance } (\sigma^2) &= \frac{\sum f_i f_i^2}{\sum f_i} - (\bar{X})^2 \\ &= \frac{5 \times 16 + 4 \times 25 + 1 \times 36 + 3 \times 64 + 2 \times 81 + 3 \times 121 + 1 \times 144}{19} - (7)^2 \\ &= \frac{1077}{19} - 49 = \frac{146}{19} \\ \Rightarrow 19\sigma^2 &= 146 \\ S &\rightarrow 1 \\ P \rightarrow 5, Q \rightarrow 3, R \rightarrow 2, S \rightarrow 1 \end{aligned}$$

15. Let  $\mathbb{R}$  denote the set of all real numbers. For a real number  $x$ , let  $[x]$  denote the greatest integer less than or equal to  $x$ . Let  $n$  denote a natural number.

Match each entry in List-I to the correct entry in List-II and choose the correct option.

	List-I		List-II
(P)	The minimum value of $n$ for which the function $f(x) = \left[ \frac{10x^3 - 45x^2 + 60x + 35}{n} \right]$ is continuous on the interval $[1, 2]$ , is	(1)	8
(Q)	The minimum value of $n$ for which $g(x) = (2n^2 - 13n - 15)(x^3 + 3x)$ , $x \in \mathbb{R}$ , is an increasing function on $\mathbb{R}$ , is	(2)	9
(R)	The smallest natural number $n$ which is greater than 5, such that $x = 3$ is a point of local minima of $h(x) = (x^2 - 9)^n (x^2 + 2x + 3)$ , is	(3)	5
(S)	Number of $x_0 \in \mathbb{R}$ such that $l(x) = \sum_{k=0}^4 \left( \sin \left  x - k \right  + \cos \left  x - k + \frac{1}{2} \right  \right)$ , $x \in \mathbb{R}$ , is NOT differentiable at $x_0$ , is	(4)	6
		(5)	10

- (A) (P)  $\rightarrow$  (1) (Q)  $\rightarrow$  (3) (R)  $\rightarrow$  (2) (S)  $\rightarrow$  (5)
- (B) (P)  $\rightarrow$  (2) (Q)  $\rightarrow$  (1) (R)  $\rightarrow$  (4) (S)  $\rightarrow$  (3)
- (C) (P)  $\rightarrow$  (5); (Q)  $\rightarrow$  (1); (R)  $\rightarrow$  (4); (S)  $\rightarrow$  (3)
- (D) (P)  $\rightarrow$  (2); (Q)  $\rightarrow$  (3); (R)  $\rightarrow$  (1); (S)  $\rightarrow$  (5)

Answer (B)

Sol. (P) Let  $g(x) = 10x^3 - 45x^2 + 60x + 35$   
 $g'(x) = 30(x^2 - 3x + 2) = 30(x - 1)(x - 2)$

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<b>SARVESH ANAND S</b> AIR 42 All India Topper 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 All India Topper 100 Physics	<b>DISHAANTH BASU</b> AIR 50 All India Topper 100 Physics	<b>YASH KUMAR</b> AIR 76 All India Topper 100 Physics	<b>ADITYA KUMAR</b> AIR 79 All India Topper 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92 All India Topper 100 Physics

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$\Rightarrow g(x)$  is decreasing in  $[1, 2]$

Now,  $f(1) = \left[ \frac{g(1)}{n} \right] = \left[ \frac{60}{n} \right], f(2) = \left[ \frac{55}{n} \right]$

For  $f(x)$  to be continuous in  $[1, 2]$  its integral value should remain same in whole interval for  $n = 9, f(1) = 6, f(2) = 6$

(P)  $\rightarrow$  (2)

(Q)  $g'(x) = (2n^2 - 13n - 15)(3x^2 + 3)$

$= (2n - 15)(n + 1)(3x^2 + 3) > 0$



for  $g(x)$  to be increasing min  $n = 8$

$\Rightarrow Q \rightarrow 1$  matching

(R)  $h(x) = (x^2 - 9)^n(x^2 + 2x + 3)$

$h(3) = 0$  for  $n > 5$

at  $n = 6 \Rightarrow n(3 + \delta) > h(3)$

$n(3 - \delta) > n(3)$

$\Rightarrow h(x)$  has local minima at  $x = 3$  for  $n = 6$

R  $\rightarrow$  4 matching

(S)  $l(x) = \sin|x| + \cos\left|x + \frac{1}{2}\right| + \sin|x-1| + \cos\left|x - \frac{1}{2}\right|$

$+ \dots + \sin|x-4| + \cos\left|x - \frac{7}{2}\right|$

as  $\sin|x - a|$  is non differentiable at  $x = a$

but  $\cos|x - a|$  remains differentiable at  $x = a$

$\Rightarrow$  given  $l(x)$  is non-differentiable at

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<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92 100 Overall

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$x_0 = 0, 1, 2, 3, 4$  (5 points)

(S)  $\rightarrow$  (3) matching

(P)  $\rightarrow$  (2) (Q)  $\rightarrow$  (1) (R)  $\rightarrow$  (4) (S)  $\rightarrow$  (3)

16. Let  $\vec{w} = \hat{i} + \hat{j} - 2\hat{k}$ , and  $\vec{u}$  and  $\vec{v}$  be two vectors, such that  $\vec{u} \times \vec{v} = \vec{w}$  and  $\vec{v} \times \vec{w} = \vec{u}$ . Let  $\alpha, \beta, \gamma$ , and  $t$  be real numbers such that

$$\vec{u} = \alpha\hat{i} + \beta\hat{j} + \gamma\hat{k}, -t\alpha + \beta + \gamma = 0, \alpha - t\beta + \gamma = 0, \text{ and } \alpha + \beta - t\gamma = 0.$$

Match each entry in List-I to the correct entry in List-II and choose the correct option.

	List-I		List-II
(P)	$ \vec{v} ^2$ is equal to	(1)	0
(Q)	If $\alpha = \sqrt{3}$ , then $\gamma^2$ is equal to	(2)	1
(R)	If $\alpha = \sqrt{3}$ , then $(\beta + \gamma)^2$ is equal to	(3)	2
(S)	If $\alpha = \sqrt{2}$ , then $t + 3$ is equal to	(4)	3
		(5)	5

(A) (P)  $\rightarrow$  (2) (Q)  $\rightarrow$  (1) (R)  $\rightarrow$  (4) (S)  $\rightarrow$  (5)

(B) (P)  $\rightarrow$  (2) (Q)  $\rightarrow$  (4) (R)  $\rightarrow$  (3) (S)  $\rightarrow$  (5)

(C) (P)  $\rightarrow$  (2) (Q)  $\rightarrow$  (1) (R)  $\rightarrow$  (4) (S)  $\rightarrow$  (3)

(D) (P)  $\rightarrow$  (5) (Q)  $\rightarrow$  (4) (R)  $\rightarrow$  (1) (S)  $\rightarrow$  (3)

Answer (A)

Sol.  $\vec{u} \times \vec{v} = \vec{w}$  and  $\vec{v} \times \vec{w} = \vec{u}$

$\Rightarrow \vec{u}, \vec{v}$  and  $\vec{w}$  are mutually perpendicular.

$$(\vec{v} \times \vec{w}) \times \vec{v} = \vec{w}$$

$$\Rightarrow \vec{w}(\vec{v} \cdot \vec{v}) - \vec{v}(\vec{v} \cdot \vec{w}) = \vec{w}$$

$$\Rightarrow \vec{w}(|\vec{v}|^2 - 1) - \vec{v}(\vec{v} \cdot \vec{w}) = \vec{0}$$

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$$\Rightarrow |\vec{v}|^2 = 1 \text{ and } \vec{v} \cdot \vec{w} = 0$$

$$|\vec{u}| |\vec{v}| = |\omega| \Rightarrow |\vec{u}| = \sqrt{6}$$

$$\vec{u} \cdot \vec{w} = 0 \Rightarrow \alpha + \beta - 2\gamma = 0$$

$$\text{and } -t\alpha + \beta + \gamma = 0 \quad \dots(i)$$

$$\alpha - t\beta + \gamma = 0 \quad \dots(ii)$$

$$\alpha + \beta - t\gamma = 0 \quad \dots(iii)$$

$$(ii) - (i) \Rightarrow \alpha(1+t) = (t+1)\beta$$

$$(iii) - (ii) \Rightarrow \beta(1+t) = (1+t)\gamma$$

$$\Rightarrow \alpha(1+t) = \beta(1+t) = \gamma(1+t)$$

either  $t = -1$  or  $\alpha = \beta = \gamma$

$$\Rightarrow \sqrt{\alpha^2 + \alpha^2 + \alpha^2} = \sqrt{6}$$

$$\Rightarrow \alpha = \sqrt{2}, -t\alpha = -\alpha - \alpha$$

$$\Rightarrow t = 2$$

Since  $\alpha = \sqrt{3}$

$$\Rightarrow t = -1$$

$$\Rightarrow \alpha + \beta + \gamma = 0$$

$$\alpha + \beta - 2\gamma = 0$$

$$\Rightarrow \gamma = 0$$

(Q)  $\rightarrow 1$

$$\alpha + \beta = 0 \Rightarrow (\beta + \gamma) = -\alpha \Rightarrow (\beta + \gamma)^2 = \alpha^2 = 3, (R) \rightarrow 4$$

$$\Rightarrow |\vec{v}|^2 = 1 \rightarrow (P) \rightarrow 2$$

$$\text{If } \alpha = \sqrt{3} \Rightarrow \gamma^2 = 0 \rightarrow (Q) \rightarrow 1$$

$$\text{If } \alpha = \sqrt{3} \Rightarrow (\beta + \gamma)^2 = (\sqrt{3})^2 = 3, (R) \rightarrow 4$$

$$\text{If } \alpha = \sqrt{2}, t + 3 = (2) + 3 = 5, (S) \rightarrow 5$$

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<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92 100 Physics

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# PART-II : PHYSICS

## SECTION 1 (Maximum Marks : 12)

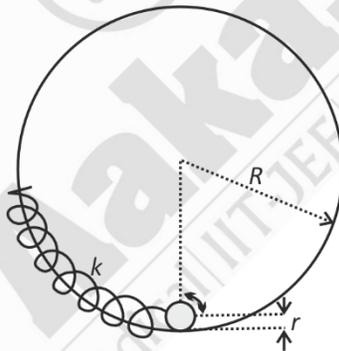
- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated **according to the following marking scheme:**

Full Marks : +3 If **ONLY** the correct option is chosen;

Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);

Negative Marks : -1 In all other cases.

1. The center of a disk of radius  $r$  and mass  $m$  is attached to a spring of spring constant  $k$ , inside a ring of radius  $R > r$  as shown in the figure. The other end of the spring is attached on the periphery of the ring. Both the ring and the disk are in the same vertical plane. The disk can only roll along the inside periphery of the ring, without slipping. The spring can only be stretched or compressed along the periphery of the ring, following the Hooke's law. In equilibrium, the disk is at the bottom of the ring. Assuming small displacement of the disc, the time period of oscillation of center of mass of the disk is written as  $T = \frac{2\pi}{\omega}$ . The correct expression for  $\omega$  is ( $g$  is the acceleration due to gravity):



(A)  $\sqrt{\frac{2}{3} \left( \frac{g}{R-r} + \frac{k}{m} \right)}$

(B)  $\sqrt{\frac{2g}{3(R-r)} + \frac{k}{m}}$

(C)  $\sqrt{\frac{1}{6} \left( \frac{g}{R-r} + \frac{k}{m} \right)}$

(D)  $\sqrt{\frac{1}{4} \left( \frac{g}{R-r} + \frac{k}{m} \right)}$

Answer (A)

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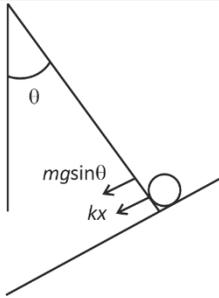
<b>SHREYAS LOHIYA</b> AIR 6 100 Overall	<b>KUSHAGRA BANGAHA</b> AIR 7 100 Overall	<b>HARSSH A GUPTA</b> AIR 15 100 Overall	<b>HARSH JHA</b> AIR 23 100 Overall	<b>DEVYA RUSTAGI</b> AIR 28 100 Overall	<b>AMOGH BANSAL</b> AIR 29 Haryana Topper
<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92 and many more...

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Sol.



$$\tau = rmgsin\theta + k(R-r)\theta r = \frac{3}{2}mr^2\alpha'$$

$$r\theta' = (R-r)\theta$$

$$\theta' = \left(\frac{R-r}{r}\right)\theta$$

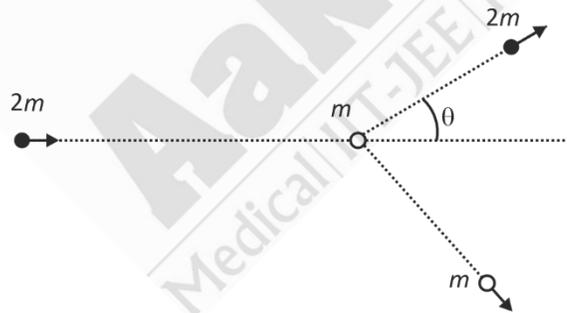
$$\alpha' = \left(\frac{R-r}{r}\right)\alpha$$

$$(rmg + k(R-r)r)\theta = \frac{3}{2}mr(R-r)\alpha$$

$$\alpha = \omega^2\theta$$

$$\omega = \sqrt{\frac{2}{3} \left[ \frac{k}{m} + \frac{g}{(R-r)} \right]}$$

2. In a scattering experiment, a particle of mass  $2m$  collides with another particle of mass  $m$ , which is initially at rest. Assuming the collision to be perfectly elastic, the maximum angular deviation  $\theta$  of the heavier particle, as shown in the figure, in radians is:



- (A)  $\pi$  (B)  $\tan^{-1}\left(\frac{1}{2}\right)$   
(C)  $\frac{\pi}{3}$  (D)  $\frac{\pi}{6}$

Answer (D)

**Aakashians Rise High in JEE (Main) 2025**

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<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92

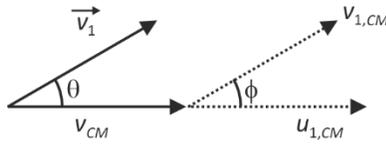
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Sol. Before collision  $\vec{v}_{CM} \rightarrow u_{1,CM}$

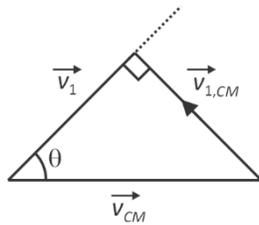
After collision



In centre of mass frame

Speed does not change only orientation does

For  $\theta$  to maximize



$$\vec{v}_{1,CM} \perp \vec{v}_1$$

$$\Rightarrow \sin\theta = \frac{v_{1,CM}}{v_{CM}}$$

$$v_{1,CM} = \frac{m_2 v_{12}}{m_1 + m_2} \Rightarrow \vec{v}_1 = \frac{m_2 \vec{u}_1}{m_1 + m_2}$$

$$v_{CM} = \frac{m_1 \vec{v}_1 + m_2 \vec{v}_2}{m_1 + m_2} = \frac{m_1 \vec{u}_1}{m_1 + m_2}$$

$$\Rightarrow \sin\theta = \frac{m_2}{m_1} \Rightarrow \sin\theta = \frac{m}{2m}$$

$$\theta = 30^\circ = \frac{\pi}{6}$$

## Aakashians Rise High in JEE (Main) 2025

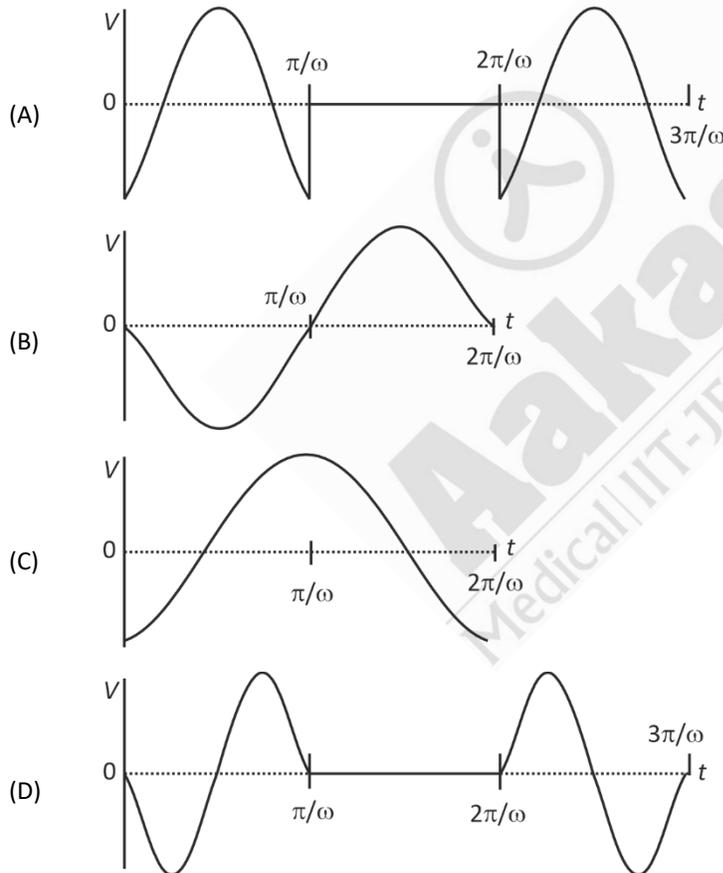
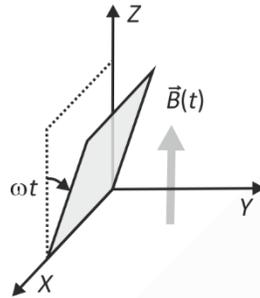
<b>SHREYAS LOHIYA</b> AIR 6 100 Overall (Other Pradesh) Topper	<b>KUSHAGRA BANGAHA</b> AIR 7 100 Overall (Other Pradesh) Topper	<b>HARSH A GUPTA</b> AIR 15 100 Overall (Other Pradesh) Topper	<b>HARSH JHA</b> AIR 23 100 Overall (Other Pradesh) Topper	<b>DEVYA RUSTAGI</b> AIR 28 100 Overall (Other Pradesh) Topper	<b>AMOGH BANSAL</b> AIR 29 100 Overall (Other Pradesh) Topper
<b>SARVESH ANAND S</b> AIR 42 100 Maths (Other Pradesh) Topper	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics (Other Pradesh) Topper	<b>DISHAANTH BASU</b> AIR 50 100 Physics (Other Pradesh) Topper	<b>YASH KUMAR</b> AIR 76 100 Physics (Other Pradesh) Topper	<b>ADITYA KUMAR</b> AIR 79 100 Physics (Other Pradesh) Topper	<b>GURURAJ S SAJJAN</b> AIR 92 100 Overall (Other Pradesh) Topper

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3. A conducting square loop initially lies in the  $XZ$  plane with its lower edge hinged along the  $X$ -axis. Only in the region  $y \geq 0$ , there is a time dependent magnetic field pointing along the  $Z$ -direction,  $\vec{B}(t) = B_0(\cos \omega t)\hat{k}$ , where  $B_0$  is a constant. The magnetic field is zero everywhere else. At time  $t = 0$ , the loop starts rotating with constant angular speed  $\omega$  about the  $X$  axis in the clockwise direction as viewed from the  $+X$  axis (as shown in the figure). Ignoring self-inductance of the loop and gravity, which of the following plots correctly represents the induced e.m.f. ( $V$ ) in the loop as a function of time:



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<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92 and many more...

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<b>Chirag Falor</b> 4 Year Classroom 1 AIR JEE (Adv.) 2020	<b>Tanishka Kabra</b> 4 Year Classroom 1 AIR-16 CRL JEE (Adv.) 2022 ALL INDIA FEMALE TOPPER	<b>Sanvi Jain</b> 4 Year Classroom 1 AIR-36 CRL JEE (Main) 2024 ALL INDIA FEMALE TOPPER
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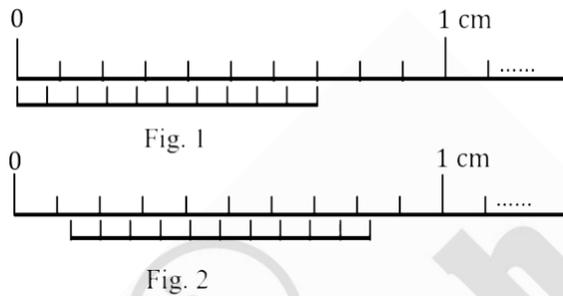
Answer (A)

Sol.  $\phi = B_0 \cos(\omega t) l^2 \sin(\omega t)$

$$\phi = \frac{B_0 l^2}{2} \sin(2\omega t)$$

$$\sum = \left| \frac{d\phi}{dt} \right| = B_0 \omega l^2 \cos(2\omega t) \text{ only for half rotation}$$

4. Figure 1 shows the configuration of main scale and Vernier scale before measurement. Fig. 2 shows the configuration corresponding to the measurement of diameter  $D$  of a tube. The measured value of  $D$  is:



- (A) 0.12 cm
- (B) 0.11 cm
- (C) 0.13 cm
- (D) 0.14 cm

Answer (C)

Sol. For (VS) 10 div = 7 mm

1 div = 0.7 mm

Reading: main scale = 1 mm

VS 1 marking matches with main scale div

So VS reads  $(1 - 0.7 \text{ mm}) = 0.3 \text{ mm}$

So total =  $1 + 0.3 \text{ mm} = 1.3 \text{ mm}$

⇒ 0.13 cm

**Aakashians Rise High in JEE (Main) 2025**

<b>SHREYAS LOHIYA</b> AIR 6 100 Overall 100 Physics	<b>KUSHAGRA BANGRAHA</b> AIR 7 100 Overall 100 Physics	<b>HARSH A GUPTA</b> AIR 15 100 Overall 100 Physics	<b>HARSH JHA</b> AIR 23 100 Overall 100 Physics	<b>DEVYA RUSTAGI</b> AIR 28 100 Overall 100 Physics	<b>AMOGH BANSAL</b> AIR 29 100 Overall 100 Physics
<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92 100 Physics

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**OUR JEE Champions**

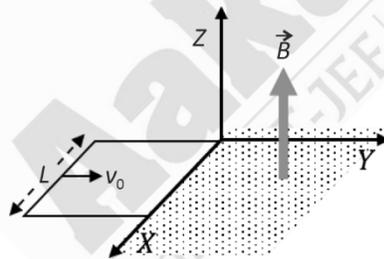
<b>Chirag Falor</b> 4 Year Classroom 1 AIR JEE (Adv.) 2020	<b>Tanishka Kabra</b> 4 Year Classroom 1 AIR-16 CRL JEE (Adv.) 2022 ALL INDIA FEMALE TOPPER	<b>Sanvi Jain</b> 4 Year Classroom 1 AIR-36 CRL JEE (Main) 2024 ALL INDIA FEMALE TOPPER
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**SECTION 2 (Maximum Marks : 12)**

- This section contains **THREE (03)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated **according to the following marking scheme:**

Full Marks	:	+4	<b>ONLY</b> if (all) the correct option(s) is(are) chosen;
Partial Marks	:	+3	If all the four options are correct but <b>ONLY</b> three options are chosen;
Partial Marks	:	+2	If three or more options are correct but <b>ONLY</b> two options are chosen, both of which are correct;
Partial Marks	:	+1	If two or more options are correct but <b>ONLY</b> one option is chosen and it is a correct option;
Zero Marks	:	0	If none of the options is chosen (i.e. the question is unanswered);
Negative Marks	:	-2	In all other cases.

5. A conducting square loop of side  $L$ , mass  $M$  and resistance  $R$  is moving in the  $XY$  plane with its edges parallel to the  $X$  and  $Y$  axes. The region  $y \geq 0$  has a uniform magnetic field,  $\vec{B} = B_0 \hat{k}$ . The magnetic field is zero everywhere else. At time  $t = 0$ , the loop starts to enter the magnetic field with an initial velocity  $v_0 \hat{j}$  m/s, as shown in the figure. Considering the quantity  $K = \frac{B_0^2 L^2}{RM}$  in appropriate units, ignoring self-inductance of the loop and gravity, which of the following statements is/are correct:



- (A) If  $v_0 = 1.5KL$ , the loop will stop before it enters completely inside the region of magnetic field
- (B) When the complete loop is inside the region of magnetic field, the net force acting on the loop is zero.
- (C) If  $v_0 = \frac{KL}{10}$ , the loop comes to rest at  $t = \left(\frac{1}{K}\right) \ln\left(\frac{5}{2}\right)$
- (D) If  $v_0 = 3KL$ , the complete loop enters inside the region of magnetic field at time  $t = \left(\frac{1}{K}\right) \ln\left(\frac{3}{2}\right)$

Answer (B, D)

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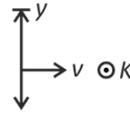
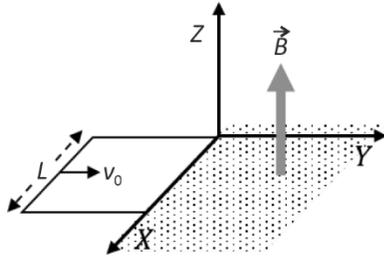
<b>SHREYAS LOHIYA</b> AIR 6 100 Overall	<b>KUSHAGRA BANGAHA</b> AIR 7 100 Overall	<b>HARSSH A GUPTA</b> AIR 15 100 Overall	<b>HARSH JHA</b> AIR 23 100 Overall	<b>DEVYA RUSTAGI</b> AIR 28 100 Physics	<b>AMOGH BANSAL</b> AIR 29 Maryana Topper
<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92 100 Overall

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**OUR JEE Champions**

<b>Chirag Falor</b> 4 Year Classroom 1 AIR JEE (Adv.) 2020	<b>Tanishka Kabra</b> 4 Year Classroom 1 AIR-16 CRL JEE (Adv.) 2022 ALL INDIA FEMALE TOPPER	<b>Sanvi Jain</b> 4 Year Classroom 1 AIR-36 CRL JEE (Main) 2024 ALL INDIA FEMALE TOPPER
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Sol.



$$K = \frac{B_0^2 L^2}{RM}$$

$$\varepsilon = vBL$$

$$I = \frac{vBL}{R}$$

$$F_{(\text{drag})} = -\frac{vBL}{R} \cdot LB$$

$$m \frac{dv}{dt} = -\frac{(B^2 L^2)v}{R}$$

$$m \frac{dv}{dx} \cdot v = -\frac{B^2 L^2}{R} \cdot v$$

$$m|v|_{v_0}^v = \frac{-B^2 L^2}{R} \cdot x|_0^x$$

$$\Rightarrow m(v - v_0) = \frac{-B^2 L^2 x}{R}$$

$$\Rightarrow v = v_0 - \frac{B^2 L^2}{mR} \cdot x$$

If  $v_0 = 1.5KL$  then for  $x = L$

$$v = \frac{3}{2}KL - KL = \frac{1}{2}KL$$

So, the loop will have some velocity and it will not stop.

If the loop completely gets inside then further no current flows and no force acts.

If  $v_0 = \frac{KL}{10}$  then for  $v = 0$

## Aakashians Rise High in JEE (Main) 2025

<b>SHREYAS LOHIYA</b> AIR 6 100 Overall Uttar Pradesh Topper	<b>KUSHAGRA BANGRAHAI</b> AIR 7 100 Overall Uttar Pradesh Topper	<b>HARSH A GUPTA</b> AIR 15 100 Overall Karnataka Topper	<b>HARSH JHA</b> AIR 23 100 Overall Delhi (NCT) Topper	<b>DEVYA RUSTAGI</b> AIR 28 100 Physics 1st Rank	<b>AMOGH BANSAL</b> AIR 29 100 Overall Haryana Topper
<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92 100 Overall

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### OUR JEE Champions

<b>Chirag Falor</b> 4 Year Classroom <b>1</b> AIR JEE (Adv.) 2020	<b>Tanishka Kabra</b> 4 Year Classroom <b>1</b> AIR-16 CRL JEE (Adv.) 2022 ALL INDIA FEMALE TOPPER	<b>Sanvi Jain</b> 4 Year Classroom <b>1</b> AIR-36 CRL JEE (Main) 2024 ALL INDIA FEMALE TOPPER
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$$\frac{dv}{dt} = -\frac{B^2 L^2}{mR} v$$

$$\int_{v_0}^v \frac{dv}{v} = \int_0^t -K \cdot dt \quad \Rightarrow \quad \ln \frac{v}{v_0} = -Kt$$

$$\frac{v}{v_0} = e^{-Kt} \text{ it will never stop}$$

If  $v_0 = 3KL$  then

$v$  at  $x = L$  is  $v = 3KL - KL = 2KL$

$$\Rightarrow \frac{2}{3} = e^{-Kt} \quad \Rightarrow \quad \frac{1}{K} \ln\left(\frac{3}{2}\right) = t$$

6. Length, breadth and thickness of a strip having a uniform cross section are measured to be 10.5 cm, 0.05 mm, and 6.0  $\mu\text{m}$ , respectively. Which of the following option(s) give(s) the volume of the strip in  $\text{cm}^3$  with correct significant figures :

- (A)  $3.2 \times 10^{-5}$  (B)  $32.0 \times 10^{-6}$   
(C)  $3.0 \times 10^{-5}$  (D)  $3 \times 10^{-5}$

**Answer (D)**

**Sol.**  $l = 10.5 \text{ cm} \rightarrow 3 \text{ SF}$

$$b = 0.05 \text{ mm} = 5 \times 10^{-3} \text{ cm} \rightarrow 1 \text{ SF}$$

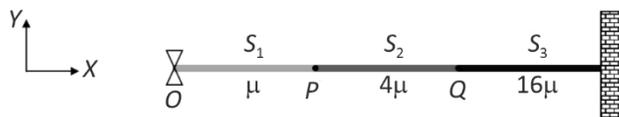
$$h = 6.0 \mu\text{m} \Rightarrow 6 \times 10^{-4} \text{ cm} \rightarrow 2 \text{ SF}$$

$$v = 315 \times 10^{-7}$$

$$v = 3.15 \times 10^{-5}$$

$$v = 3 \times 10^{-5} \quad 1 \text{ SF}$$

7. Consider a system of three connected strings,  $S_1$ ,  $S_2$  and  $S_3$  with uniform linear mass densities  $\mu \text{ kg/m}$ ,  $4\mu \text{ kg/m}$  and  $16\mu \text{ kg/m}$ , respectively, as shown in the figure.  $S_1$  and  $S_2$  are connected at the point  $P$ , whereas  $S_2$  and  $S_3$  are connected at the point  $Q$ , and the other end of  $S_3$  is connected to a wall. A wave generator  $O$  is connected to the free end of  $S_1$ . The wave from the generator is represented by  $y = y_0 \cos(\omega t - kx) \text{ cm}$ , where  $y_0$ ,  $\omega$  and  $k$  are constants of appropriate dimensions. Which of the following statements is/are correct :



**Aakashians Rise High in JEE (Main) 2025**

<b>SHREYAS LOHIYA</b> AIR 6 100 Overall	<b>KUSHAGRA BANGAHA</b> AIR 7 100 Overall	<b>HARSH A GUPTA</b> AIR 15 100 Overall	<b>HARSH JHA</b> AIR 23 100 Overall	<b>DEVYA RUSTAGI</b> AIR 28 100 Overall	<b>AMOGH BANSAL</b> AIR 29 100 Overall
<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92 100 Overall

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**OUR JEE Champions**

<b>Chirag Falor</b> 4 Year Classroom 1 AIR JEE (Adv.) 2020 ALL INDIA FEMALE TOPPER	<b>Tanishka Kabra</b> 4 Year Classroom 1 AIR-16 CRL JEE (Adv.) 2022 ALL INDIA FEMALE TOPPER	<b>Sanvi Jain</b> 4 Year Classroom 1 AIR-36 CRL JEE (Main) 2024 ALL INDIA FEMALE TOPPER
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- (A) When the wave reflects from  $P$  for the first time, the reflected wave is represented by  $y = \alpha_1 y_0 \cos(\omega t + kx + \pi)$  cm, where  $\alpha_1$  is a positive constant
- (B) When the wave transmits through  $P$  for the first time, the transmitted wave is represented by  $y = \alpha_2 y_0 \cos(\omega t - kx)$  cm, where  $\alpha_2$  is a positive constant
- (C) When the wave reflects from  $Q$  for the first time, the reflected wave is represented by  $y = \alpha_3 y_0 \cos(\omega t - kx + \pi)$  cm, where  $\alpha_3$  is a positive constant
- (D) When the wave transmits through  $Q$  for the first time, the transmitted wave is represented by  $y = \alpha_4 y_0 \cos(\omega t - 4kx)$  cm, where  $\alpha_4$  is a positive constant

**Answer (A, D)**

**Sol.** Reflection of wave in string from fixed end, reflected wave phase change by  $\pi$ .

And reflected wave from free (rarer) end No phase change.

$\therefore \omega = kV$

$\omega = k\sqrt{\frac{T}{\mu}}$  given  $y = y_0 \cos(\omega t - kx)$  cm

$\frac{\sqrt{T}}{\mu} = \text{const.}$  For medium  $PQ(S_2)$

$k_{S_2} = k_{PQ} = 2k$

For medium  $S_3$

$k_{S_3} = 4k$

Option (A) reflection from  $P$ , phase change by  $\pi$ ,

No change in ' $k$ '. Hence correct option.

In option (B)  $k_{S_2} = 2k$  but in option given  $k_s = k$

Hence wrong.

In option (C) direction of reflected wave in negative direction.

Hence wrong.

Option (D) no phase change in transmitted wave and given  $k_{S_3} = 4k$

**Aakashians Rise High in JEE (Main) 2025**

<b>SHREYAS LOHIYA</b> AIR 6 100 Overall	<b>KUSHAGRA BANGAHA</b> AIR 7 100 Overall	<b>HARSH A GUPTA</b> AIR 15 100 Overall	<b>HARSH JHA</b> AIR 23 100 Overall	<b>DEVYA RUSTAGI</b> AIR 28 100 Physics	<b>AMOGH BANSAL</b> AIR 29 Haryana Topper
<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92

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**OUR JEE Champions**

<b>Chirag Falor</b> 4 Year Classroom 1 AIR JEE (Adv.) 2020 ALL INDIA FEMALE TOPPER	<b>Tanishka Kabra</b> 4 Year Classroom 1 AIR-16 CRL JEE (Adv.) 2022 ALL INDIA FEMALE TOPPER	<b>Sanvi Jain</b> 4 Year Classroom 1 AIR-36 CRL JEE (Main) 2024 ALL INDIA FEMALE TOPPER
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**SECTION 3 (Maximum Marks : 24)**

- This section contains **SIX (06)** questions.
- The answer to each question is a **NUMERICAL VALUE**.
- For each question, enter the correct numerical value of the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- If the numerical value has more than two decimal places, **truncate/round-off** the value to **TWO** decimal places.
- Answer to each question will be evaluated **according to the following marking scheme:**  

Full Marks	:	+4	If ONLY the correct numerical value is entered in the designated place;
Zero Marks	:	0	In all other cases.

8. A person sitting inside an elevator performs a weighing experiment with an object of mass 50 kg. Suppose that the variation of the height  $y$  (in m) of the elevator, from the ground, with time  $t$  (in s) is given by  $y = 8 \left[ 1 + \sin\left(\frac{2\pi t}{T}\right) \right]$ , where  $T = 40\pi$  s. Taking acceleration due to gravity,  $g = 10 \text{ m/s}^2$ , the maximum variation of the object's weight (in N) as observed in the experiment is \_\_\_\_\_

**Answer (02.00)**

**Sol.**  $y = 8(1 + \sin(\omega t))$ ,

Acceleration of elevator

$$\omega = \frac{2\pi}{40\pi} = \frac{1}{20}$$

$$a = -8\omega^2 \sin(\omega t)$$

$$|a_{\max}| = 8 \times \frac{1}{400} = \frac{1}{50}$$

$$W_{\max} = m(g + a_{\max})$$

$$W_{\min} = m(g - a_{\max})$$

$$\Delta W = 2ma_{\max}$$

$$= 2 \times 50 \times \frac{1}{50}$$

$$= 2 \text{ N}$$

**Aakashians Rise High in JEE (Main) 2025**

<b>SHREYAS LOHIYA</b> AIR 6 100 Overall Other Pradesh Topper	<b>KUSHAGRA BANGAHA</b> AIR 7 100 Overall Other Pradesh Topper	<b>HARSH A GUPTA</b> AIR 15 100 Overall Vishakhapatnam Topper	<b>HARSH JHA</b> AIR 23 100 Overall Odisha (JEC) Topper	<b>DEVYA RUSTAGI</b> AIR 28 100 Maths & Physics All India Rank 1st	<b>AMOGH BANSAL</b> AIR 29 100 Overall Haryana Topper
<b>SARVESH ANAND S</b> AIR 42 100 Maths Vishakhapatnam	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics Vishakhapatnam	<b>DISHAANTH BASU</b> AIR 50 100 Physics Vishakhapatnam	<b>YASH KUMAR</b> AIR 76 100 Physics Vishakhapatnam	<b>ADITYA KUMAR</b> AIR 79 100 Physics Vishakhapatnam	<b>GURURAJ S SAJJAN</b> AIR 92 100 Overall Vishakhapatnam

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**OUR JEE Champions**

<b>Chirag Falor</b> 4 Year Classroom 1 AIR JEE (Adv.) 2020 ALL INDIA FEMALE TOPPER	<b>Tanishka Kabra</b> 4 Year Classroom 1 AIR-16 CRL JEE (Adv.) 2022 ALL INDIA FEMALE TOPPER	<b>Sanvi Jain</b> 4 Year Classroom 1 AIR-36 CRL JEE (Main) 2024 ALL INDIA FEMALE TOPPER
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9. A cube of unit volume contains  $35 \times 10^7$  photons of frequency  $10^{15}$  Hz. If the energy of all the photons is viewed as the average energy being contained in the electromagnetic waves within the same volume, then the amplitude of the magnetic field is  $\alpha \times 10^{-9}$  T. Taking permeability of free space  $\mu_0 = 4\pi \times 10^{-7}$  Tm/A, Planck's constant  $h = 6 \times 10^{-34}$  Js and  $\pi = \frac{22}{7}$ , the value of  $\alpha$  is \_\_\_\_\_

Answer (22.98)

Sol.  $E = N \cdot hf$

$$E = 35 \times 10^7 \times 6 \times 10^{-34} \times 10^{15}$$

$$\frac{B_0^2}{2\mu_0} = E$$

$$B_0^2 = 2 \times 4 \times \frac{22}{7} \times 10^{-7} \times 35 \times 10^7 \times 6 \times 10^{-34} \times 10^{15}$$

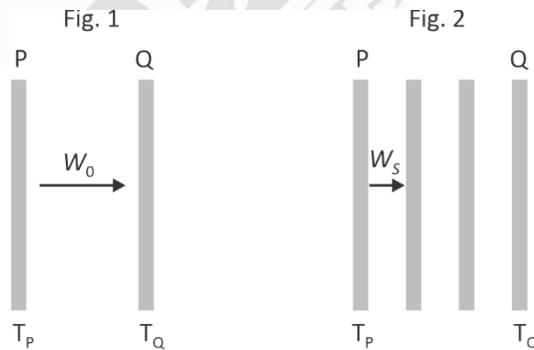
$$= 5280 \times 10^{-19}$$

$$B_0^2 = 528 \times 10^{-18}$$

$$B_0 = 22.978 \times 10^{-9}$$

$$\alpha = 22.98$$

10. Two identical plates P and Q, radiating as perfect black bodies, are kept in vacuum at constant absolute temperatures  $T_P$  and  $T_Q$ , respectively, with  $T_Q < T_P$ , as shown in Fig. 1. The radiated power transferred per unit area from P to Q is  $W_0$ . Subsequently, two more plates, identical to P and Q, are introduced between P and Q, as shown in Fig. 2. Assume that heat transfer takes place only between adjacent plates. If the power transferred per unit area in the direction from P to Q (Fig. 2) in the steady state is  $W_S$ , then the ratio  $\frac{W_0}{W_S}$  is \_\_\_\_\_



Answer (03.00)

**Aakashians Rise High in JEE (Main) 2025**

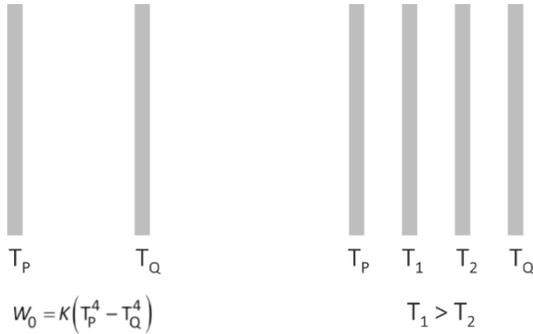
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Sol.



In the steady state

$$W_S = K(T_P^4 - T_1^4)$$

$T_1$  and  $T_2$  will remain constant

$$\Rightarrow (T_P^4 - T_1^4) = (T_1^4 - T_2^4) = (T_2^4 - T_P^4)$$

$$\Rightarrow T_P^4 + T_2^4 = 2T_1^4 \quad \dots(i)$$

$$T_1^4 + T_Q^4 = 2T_2^4 \quad \dots(ii)$$

2(i) + (ii)

$$\Rightarrow T_1^4 = \frac{2T_P^4 + T_Q^4}{3}$$

$$W_S = K \left[ T_P^4 - \frac{(2T_P^4 + T_Q^4)}{3} \right] = \frac{K(T_P^4 - T_Q^4)}{3}$$

$$\boxed{\frac{W_0}{W_S} = 3}$$

11. A solid glass sphere of refractive index  $n = \sqrt{3}$  and radius  $R$  contains a spherical air cavity of radius  $\frac{R}{2}$ , as shown in the figure. A very thin glass layer is present at the point O so that the air cavity (refractive index  $n = 1$ ) remains inside the glass sphere. An unpolarized, unidirectional and monochromatic light source S emits a light ray from a point inside the glass sphere towards the periphery of the glass sphere. If the light is reflected from the point O and is fully polarized, then the angle of incidence at the inner surface of the glass sphere is  $\theta$ . The value of  $\sin\theta$  is \_\_\_\_\_

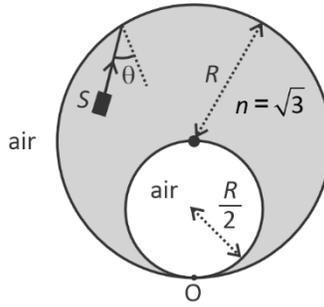
## Aakashians Rise High in JEE (Main) 2025

SHREYAS LOHIYA AIR 6 100 Overall	KUSHAGRA BANGAHA AIR 7 100 Overall	HARSH A GUPTA AIR 15 100 Overall	HARSH JHA AIR 23 100 Overall	DEVYA RUSTAGI AIR 28 100 Physics	AMOGH BANSAL AIR 29 Haryana Topper
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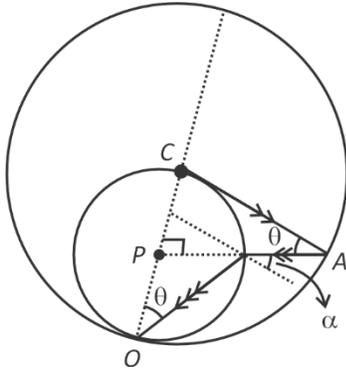
### OUR JEE Champions

Chirag Falor 4 Year Classroom 1 AIR JEE (Adv.) 2020	Tanishka Kabra 4 Year Classroom 1 AIR-16 CRL JEE (Adv.) 2022 ALL INDIA FEMALE TOPPER	Sanvi Jain 4 Year Classroom 1 AIR-36 CRL JEE (Main) 2024 ALL INDIA FEMALE TOPPER
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Answer (00.75)

Sol.



$\theta = 60^\circ$  because it is Brewster angle

At point X

Snell's law gives  $\alpha = 30^\circ$

$\Rightarrow AP$  is perpendicular to  $CO$

Therefore in  $\triangle CPA$

$$\sin \theta = \frac{CP}{CA} = \frac{3R/4}{R} = \frac{3}{4}$$

12. A single slit diffraction experiment is performed to determine the slit width using the equation,  $\frac{bd}{D} = m\lambda$ , where  $b$  is the slit width,  $D$  the shortest distance between the slit and the screen,  $d$  the distance between the  $m^{\text{th}}$  diffraction maximum and the central maximum, and  $\lambda$  is the wavelength.  $D$  and  $d$  are measured with scales of least count of 1 cm and 1 mm, respectively. The values of  $\lambda$  and  $m$  are known precisely to be 600 nm and 3, respectively. The absolute error (in  $\mu\text{m}$ ) in the value of  $b$  estimated using the diffraction maximum that occurs for  $m = 3$  with  $d = 5$  mm and  $D = 1$  m is

Answer (94.50)

### Aakashians Rise High in JEE (Main) 2025

<b>SHREYAS LOHIYA</b> AIR 6 100 Overall Other Fields: Topper	<b>KUSHAGRA BANGRAHA</b> AIR 7 100 Overall Other Fields: Topper	<b>HARSH A GUPTA</b> AIR 15 100 Overall All India Topper	<b>HARSH JHA</b> AIR 23 100 Overall India (JEE) Topper	<b>DEVYA RUSTAGI</b> AIR 28 100 Overall All India Topper	<b>AMOGH BANSAL</b> AIR 29 100 Overall Haryana Topper
<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92 100 Overall

\*Aakash Invictus Contact Program and many more...

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<b>Chirag Falor</b> 4 Year Classroom <b>1</b> AIR JEE (Adv.) 2020 ALL INDIA FEMALE TOPPER	<b>Tanishka Kabra</b> 4 Year Classroom <b>1</b> AIR-16 CRL JEE (Adv.) 2022 ALL INDIA FEMALE TOPPER	<b>Sanvi Jain</b> 4 Year Classroom <b>1</b> AIR-36 CRL JEE (Main) 2024 ALL INDIA FEMALE TOPPER
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Sol.  $b = \frac{m\lambda D}{d}$

$$b = \frac{3 \times 600 \times 1}{5} \times 10^{-6}$$

Case 1 with single dash and case 2 with double dash

$$\begin{cases} b' = \frac{3 \times 600 \times 1.01}{4} \times 10^{-6} & \frac{N^+}{D^-} \\ b'' = \frac{3 \times 600 \times 0.99}{6} \times 10^{-6} & \frac{N^-}{D^+} \end{cases}$$

$$\begin{cases} \frac{b'}{b} = \frac{5.05}{4} \\ \frac{b''}{b} = \frac{4.95}{6} \end{cases}$$

$$\begin{cases} (\Delta b)_1 = \left(\frac{5.05}{4} - 1\right)b \\ = \frac{1.05}{4}b \\ (\Delta b)_2 = \left(\frac{4.95}{6} - 1\right)b = \frac{1.05}{6}b \end{cases}$$

$$\begin{aligned} \Delta b_1 &= \frac{1.05}{4} \times \frac{3 \times 600}{5} \times 10^{-6} \\ &= \frac{90 \times 1.05 \times 10^{-6}}{9450} \end{aligned}$$

$$\Delta b_1 = 94.50 \mu\text{m}$$

13. Consider an electron in the  $n = 3$  orbit of a hydrogen-like atom with atomic number  $Z$ . At absolute temperature  $T$ , a neutron having thermal energy  $k_B T$  has the same de Broglie wavelength as that of this electron. If this temperature is given by

$$T = \frac{Z^2 h^2}{\alpha \pi^2 a_0^2 m_N k_B}$$

(where  $h$  is the Planck's constant,  $k_B$  is the Boltzmann constant,  $m_N$  is the mass of the neutron and  $a_0$  is

the first Bohr radius of hydrogen atom) then the value of  $\alpha$  is \_\_\_\_\_

Answer (72.00)

## Aakashians Rise High in JEE (Main) 2025

<b>SHREYAS LOHIYA</b> AIR 6 100 Overall 100 Physics	<b>KUSHAGRA BANGRAH</b> AIR 7 100 Overall 100 Physics	<b>HARSH A GUPTA</b> AIR 15 100 Overall 100 Physics	<b>HARSH JHA</b> AIR 23 100 Overall 100 Physics	<b>DEVYA RUSTAGI</b> AIR 28 100 Overall 100 Physics	<b>AMOGH BANSAL</b> AIR 29 100 Overall 100 Physics
<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92 100 Physics

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Sol.  $2\pi r_3 = 3\lambda_e$

$$\lambda_e = \frac{2\pi r_3}{3}$$

$$\lambda_n = \frac{h}{p} = \frac{h}{\sqrt{2km_n}}$$

$$\frac{2\pi r_3}{3} = \frac{h}{\sqrt{2K_B T m_n}}$$

$$r_3 = \frac{a_0 \times (3)^2}{Z}$$

$$\frac{6\pi a_0}{Z} = \frac{h}{\sqrt{2K_B T m_n}}$$

$$T = \frac{h^2 Z^2}{36\pi^2 a_0^2 \times 2K_B m_n}$$

$$= \frac{h^2 Z^2}{72\pi^2 a_0^2 K_B m_n}$$

$\alpha = 72$

**SECTION 4 (Maximum Marks : 12)**

- This section contains **THREE (03)** Matching List Sets.
- Each set has **ONE** Multiple Choice Question.
- Each set has **TWO** lists: **List-I** and **List-II**.
- **List-I** has **Four** entries (P), (Q), (R) and (S) and **List-II** has **Five** entries (1), (2), (3), (4) and (5).
- **FOUR** options are given in each Multiple Choice Question based on **List-I** and **List-II** and **ONLY ONE** of these four options satisfies the condition asked in the Multiple Choice Question.
- Answer to each question will be evaluated **according to the following marking scheme:**

*Full Marks* : +4 **ONLY** if the option corresponding to the correct combination is chosen;

*Zero Marks* : 0 If none of the options is chosen (i.e. the question is unanswered);

*Negative Marks* : -1 In all other cases.

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SHREYAS LOHIYA AIR 6 100 Overall 100 Physics	KUSHAGRA BANGAHA AIR 7 100 Overall 100 Physics	HARSH A GUPTA AIR 15 100 Overall 100 Physics	HARSH JHA AIR 23 100 Overall 100 Physics	DEVYA RUSTAGI AIR 28 100 Overall 100 Physics	AMOGH BANSAL AIR 29 100 Overall 100 Physics
SARVESH ANAND S AIR 42 100 Maths	KRISHNA AGRAWAL AIR 48 100 Physics	DISHAANTH BASU AIR 50 100 Physics	YASH KUMAR AIR 76 100 Physics	ADITYA KUMAR AIR 79 100 Physics	GURURAJ S SAJJAN AIR 92 100 Physics

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14. List-I shows four configurations, each consisting of a pair of ideal electric dipoles. Each dipole has a dipole moment of magnitude  $p$ , oriented as marked by arrows in the figures. In all the configurations the dipoles are fixed such that they are at a distance  $2r$  apart along the  $x$  direction. The midpoint of the line joining the two dipoles is  $X$ . The possible resultant electric fields  $\vec{E}$  at  $X$  are given in List-II.

Choose the option that describes the correct match between the entries in List-I to those in List-II.

	List-I		List-II
(P)		(1)	$\vec{E} = 0$
(Q)		(2)	$\vec{E} = -\frac{p}{2\pi\epsilon_0 r^3} \hat{j}$
(R)		(3)	$\vec{E} = -\frac{p}{4\pi\epsilon_0 r^3} (\hat{i} - \hat{j})$
(S)		(4)	$\vec{E} = \frac{p}{4\pi\epsilon_0 r^3} (2\hat{i} - \hat{j})$
		(5)	$\vec{E} = \frac{p}{\pi\epsilon_0 r^3} \hat{i}$

(A) P→3, Q→1, R→2, S→4

(B) P→4, Q→5, R→3, S→1

(C) P→2, Q→1, R→4, S→5

(D) P→2, Q→1, R→3, S→5

Answer (C)

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<b>SHREYAS LOHIYA</b> AIR 6 100 Overall 100 Physics	<b>KUSHAGRA BANGAHA</b> AIR 7 100 Overall 100 Physics	<b>HARSH A GUPTA</b> AIR 15 100 Overall 100 Physics	<b>HARSH JHA</b> AIR 23 100 Overall 100 Physics	<b>DEVYA RUSTAGI</b> AIR 28 100 Overall 100 Physics	<b>AMOGH BANSAL</b> AIR 29 100 Overall 100 Physics
<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92 100 Physics

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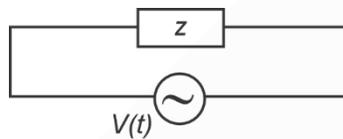
Sol. (P)  $E = \frac{-2kp}{r^3} \hat{j} = -\frac{\rho}{2\pi\epsilon_0 r^3} \hat{j}$ , P→(2)

(Q)  $E = 0$ , Q→(1)

(R)  $E = \frac{2kp}{r^3} \hat{i} - \frac{kp}{r^3} \hat{j}$ , R→(4)

(S)  $E = \frac{4kp}{r^3} \hat{i}$ , S→(5)

15. A circuit with an electrical load having impedance  $Z$  is connected with an AC source as shown in the diagram. The source voltage varies in time as  $V(t) = 300 \sin(400t)$  V, where  $t$  is time in s. List-I shows various options for the load. The possible currents  $i(t)$  in the circuit as a function of time are given in List-II.



Choose the option that describes the correct match between the entries in List-I to those in List-II.

	List-I		List-II
(P)	$30\Omega$ 	(1)	
(Q)	$30\Omega$ $100\text{ mH}$ 	(2)	

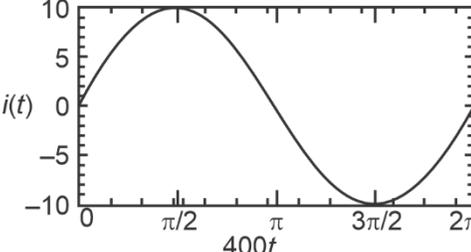
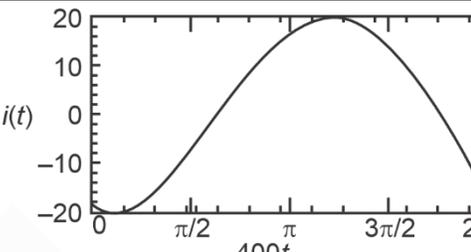
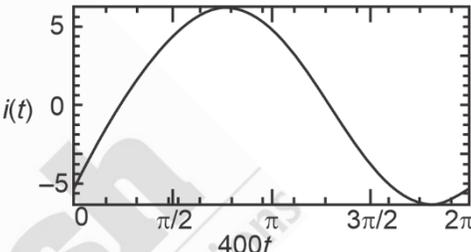
**Aakashians Rise High in JEE (Main) 2025**

<b>SHREYAS LOHIYA</b> AIR 6 100 Overall 	<b>KUSHAGRA BANGAHA</b> AIR 7 100 Overall 	<b>HARSH A GUPTA</b> AIR 15 100 Overall 	<b>HARSH JHA</b> AIR 23 100 Overall 	<b>DEVYA RUSTAGI</b> AIR 28 100 Physics 	<b>AMOGH BANSAL</b> AIR 29 100 Overall 
<b>SARVESH ANAND S</b> AIR 42 100 Maths 	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics 	<b>DISHAANTH BASU</b> AIR 50 100 Physics 	<b>YASH KUMAR</b> AIR 76 100 Physics 	<b>ADITYA KUMAR</b> AIR 79 100 Physics 	<b>GURURAJ S SAJJAN</b> AIR 92 100 Overall 

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(R)	$50 \mu\text{F}$ $30\Omega$ $25 \text{ mH}$ 	(3)	
(S)	$50 \mu\text{F}$ $60\Omega$ $125 \text{ mH}$ 	(4)	
		(5)	

(A) P→3, Q→5, R→2, S→1

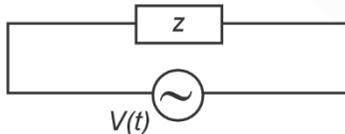
(B) P→1, Q→5, R→2, S→3

(C) P→3, Q→4, R→2, S→1

(D) P→1, Q→4, R→2, S→5

**Answer (A)**

**Sol.**  $V(t) = 300 \sin(400t)$



$$\Rightarrow i_0 = \frac{300}{30} = 10 \text{ A}$$

and  $\phi = 0$

$\Rightarrow (P) \rightarrow (3)$

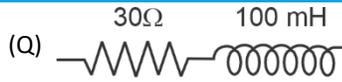
**Aakashians Rise High in JEE (Main) 2025**

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$$\Rightarrow Z = \sqrt{R^2 + (\omega L)^2}$$

$$= \sqrt{(30)^2 + (400 \times 100 \times 10^{-3})^2} = 50 \Omega$$

$$\therefore i_0 = \frac{300}{50} = 6 \text{ A}$$

$$\phi = \tan^{-1}\left(\frac{\omega L}{R}\right) = 53^\circ \text{ (lag)}$$

(Q)→(5)

(R) 
$$Z = \sqrt{(30)^2 + \left(\frac{1}{400 \times 50 \times 10^{-6}} - 400 \times 25 \times 10^{-3}\right)^2}$$

$$= \sqrt{(30)^2 + (40)^2} = 50 \Omega$$

∴ R→(2)

(S) 
$$Z = \sqrt{(60)^2 + \left(\frac{1}{50 \times 10^{-6} \times 400} - 125 \times 10^{-3} \times 400\right)^2}$$

$$= \sqrt{(60)^2 + (50 - 50)^2}$$

$$= 60 \Omega$$

$$\therefore i_0 = \frac{300}{60} = 5 \text{ A}$$

(S)→1

## Aakashians Rise High in JEE (Main) 2025

<b>SHREYAS LOHIYA</b> AIR 6 100 Overall 	<b>KUSHAGRA BANGAHA</b> AIR 7 100 Overall 	<b>HARSSH A GUPTA</b> AIR 15 100 Overall 	<b>HARSH JHA</b> AIR 23 100 Overall 	<b>DEVYA RUSTAGI</b> AIR 28 100 Physics 	<b>AMOGH BANSAL</b> AIR 29 100 Overall 
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16. List-I shows various functional dependencies of energy ( $E$ ) on the atomic number ( $Z$ ). Energies associated with certain phenomena are given in List-II.

Choose the option that describes the correct match between the entries in List-I to those in List-II.

	List-I		List-II
(P)	$E \propto Z^2$	(1)	energy of characteristic x-rays
(Q)	$E \propto (Z - 1)^2$	(2)	electrostatic part of the nuclear binding energy for stable nuclei with mass numbers in the range 30 to 170
(R)	$E \propto Z(Z - 1)$	(3)	energy of continuous x-rays
(S)	$E$ is practically independent of $Z$	(4)	average nuclear binding energy per nucleon for stable nuclei with mass number in the range 30 to 170
		(5)	energy of radiation due to electronic transitions from hydrogen-like atoms

(A) P→4, Q→3, R→1, S→2

(B) P→5, Q→2, R→1, S→4

(C) P→5, Q→1, R→2, S→4

(D) P→3, Q→2, R→1, S→5

**Answer (C)**

Sol.  $\therefore E \propto Z^2 \left( \frac{1}{n_1^2} - \frac{1}{n_2^2} \right)$

⇒ (P)→(5)

$\therefore E \propto (Z - 1)^2$

⇒ Energy of characteristic x-rays.

⇒ (Q)→(1)

Also,  $E \propto Z(Z - 1)$

Electrostatic energy of proton in nucleus.

⇒ (R)→(2)

(S)  $E$  is independent of  $Z$

⇒ Average binding energy per nucleon in range of 30 to 170.

⇒ (S)→(4)

**Aakashians Rise High in JEE (Main) 2025**

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## PART-III : CHEMISTRY

### SECTION 1 (Maximum Marks : 12)

- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated **according to the following marking scheme:**

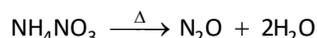
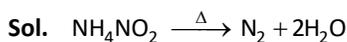
*Full Marks* : +3 If **ONLY** the correct option is chosen;

*Zero Marks* : 0 If none of the options is chosen (i.e. the question is unanswered);

*Negative Marks* : -1 In all other cases.

1. The heating of  $\text{NH}_4\text{NO}_2$  at  $60\text{--}70^\circ\text{C}$  and  $\text{NH}_4\text{NO}_3$  at  $200\text{--}250^\circ\text{C}$  is associated with the formation of nitrogen containing compounds **X** and **Y**, respectively. **X** and **Y**, respectively, are
- (A)  $\text{N}_2$  and  $\text{N}_2\text{O}$  (B)  $\text{NH}_3$  and  $\text{NO}_2$   
 (C)  $\text{NO}$  and  $\text{N}_2\text{O}$  (D)  $\text{N}_2$  and  $\text{NH}_3$

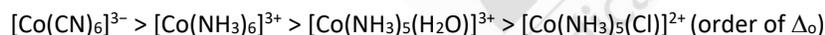
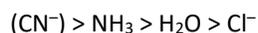
**Answer (A)**



2. The correct order of the wavelength maxima of the absorption band in the ultraviolet-visible region for the given complexes is
- (A)  $[\text{Co}(\text{CN})_6]^{3-} < [\text{Co}(\text{NH}_3)_6]^{3+} < [\text{Co}(\text{NH}_3)_5(\text{H}_2\text{O})]^{3+} < [\text{Co}(\text{NH}_3)_5(\text{Cl})]^{2+}$   
 (B)  $[\text{Co}(\text{NH}_3)_5(\text{Cl})]^{2+} < [\text{Co}(\text{NH}_3)_5(\text{H}_2\text{O})]^{3+} < [\text{Co}(\text{NH}_3)_6]^{3+} < [\text{Co}(\text{CN})_6]^{3-}$   
 (C)  $[\text{Co}(\text{CN})_6]^{3-} < [\text{Co}(\text{NH}_3)_5(\text{Cl})]^{2+} < [\text{Co}(\text{NH}_3)_5(\text{H}_2\text{O})]^{3+} < [\text{Co}(\text{NH}_3)_6]^{3+}$   
 (D)  $[\text{Co}(\text{NH}_3)_6]^{3+} < [\text{Co}(\text{CN})_6]^{3-} < [\text{Co}(\text{NH}_3)_5(\text{Cl})]^{2+} < [\text{Co}(\text{NH}_3)_5(\text{H}_2\text{O})]^{3+}$

**Answer (A)**

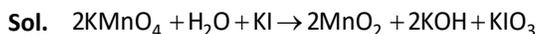
**Sol.** Spectrochemical series



So order of  $\lambda_{\text{max}}$  will be opposite.

3. One of the products formed from the reaction of permanganate ion with iodide ion in neutral aqueous medium is
- (A)  $\text{I}_2$  (B)  $\text{IO}_3^-$   
 (C)  $\text{IO}_4^-$  (D)  $\text{IO}_2^-$

**Answer (B)**



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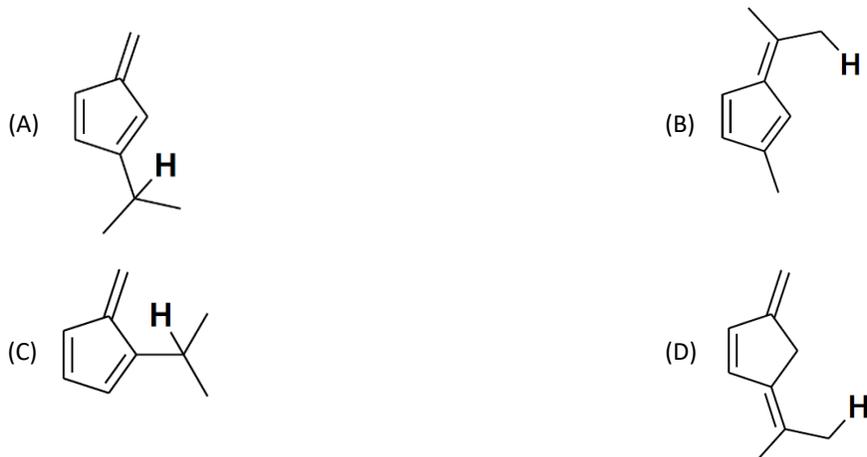
<b>SHREYAS LOHIYA</b> AIR 6 <small>100%ile 100</small>	<b>KUSHAGRA BAINGAHA</b> AIR 7 <small>100%ile 100</small>	<b>HARSSH A GUPTA</b> AIR 15 <small>100%ile 100</small>	<b>HARSH JHA</b> AIR 23 <small>100%ile 100</small>	<b>DEVYA RUSTAGI</b> AIR 28 <small>100%ile 100</small>	<b>AMOGH BANSAL</b> AIR 29 <small>100%ile 100</small>
<b>SARVESH ANAND S</b> AIR 42 <small>100%ile 100</small>	<b>KRISHNA AGRAWAL</b> AIR 48 <small>100%ile 100</small>	<b>DISHAANTH BASU</b> AIR 50 <small>100%ile 100</small>	<b>YASH KUMAR</b> AIR 76 <small>100%ile 100</small>	<b>ADITYA KUMAR</b> AIR 79 <small>100%ile 100</small>	<b>GURURAJ S SAJJAN</b> AIR 92 <small>100%ile 100</small>

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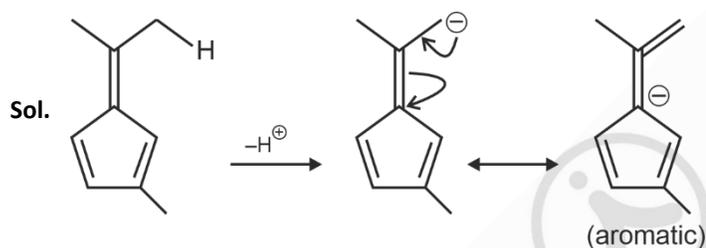
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4. Consider the depicted hydrogen (H) in the hydrocarbons given below. The most acidic hydrogen (H) is



Answer (B)



The conjugate base of (B) formed is most stable hence, H is most acidic in (B)

**SECTION 2 (Maximum Marks : 12)**

- This section contains **THREE (03)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated **according to the following marking scheme:**

*Full Marks* : +4 **ONLY** if (all) the correct option(s) is(are) chosen;

*Partial Marks* : +3 If all the four options are correct but **ONLY** three options are chosen;

*Partial Marks* : +2 If three or more options are correct but **ONLY** two options are chosen, both of which are correct;

*Partial Marks* : +1 If two or more options are correct but **ONLY** one option is chosen and it is a correct option;

*Zero Marks* : 0 If none of the options is chosen (i.e. the question is unanswered);

*Negative Marks* : -2 In all other cases.

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<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92 100 Physics

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5. Regarding the molecular orbital (MO) energy levels for homonuclear diatomic molecules, the **INCORRECT** statement(s) is(are)
- (A) Bond order of  $\text{Ne}_2$  is zero.
  - (B) The highest occupied molecular orbital (HOMO) of  $\text{F}_2$  is  $\sigma$ -type.
  - (C) Bond energy of  $\text{O}_2^+$  is smaller than the bond energy of  $\text{O}_2$ .
  - (D) Bond length of  $\text{Li}_2$  is larger than the bond length of  $\text{B}_2$ .

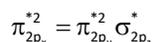
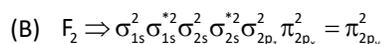
**Answer (B, C)**

**Sol.** (A) According to MOT, number of Bonding electrons and number of antibonding electron in  $\text{Ne}_2$  is same

$$\text{So, BO} = \frac{N_b - N_a}{2}$$

is zero

(A) is correct



HOMO of  $\text{F}_2$  is  $\pi$ -type not  $\sigma$ -type

(B) is incorrect

(C)  $\text{BE} \propto \text{BO}$

BO of  $\text{O}_2$  is = 2

BO of  $\text{O}_2^+$  is = 2.5

BE of  $\text{O}_2^+$  > BE of  $\text{O}_2$

(C) is incorrect

(D) Bond length of  $\text{B}_2$  = 118 pm

Bond length of  $\text{Li}_2$  = 267 pm

B.L. of  $\text{Li}_2$  > B.L. of  $\text{B}_2$

(D) is correct

6. The pair(s) of diamagnetic ions is(are)

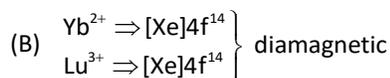
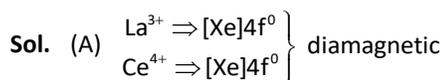
(A)  $\text{La}^{3+}$ ,  $\text{Ce}^{4+}$

(B)  $\text{Yb}^{2+}$ ,  $\text{Lu}^{3+}$

(C)  $\text{La}^{2+}$ ,  $\text{Ce}^{3+}$

(D)  $\text{Yb}^{3+}$ ,  $\text{Lu}^{2+}$

**Answer (A, B)**



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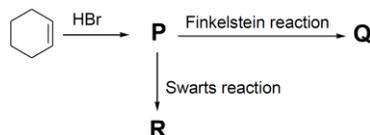
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- (C)  $\left. \begin{array}{l} \text{La}^{2+} \Rightarrow [\text{Xe}]5d^1 \\ \text{Ce}^{3+} \Rightarrow [\text{Xe}]4f^1 \end{array} \right\} \text{Paramagnetic}$
- (D)  $\left. \begin{array}{l} \text{Yb}^{3+} \Rightarrow [\text{Xe}]4f^{13} \\ \text{Lu}^{2+} \Rightarrow [\text{Xe}]4f^{14} 5d^1 \end{array} \right\} \text{Paramagnetic}$

Diamagnetic species are those which have all electrons paired

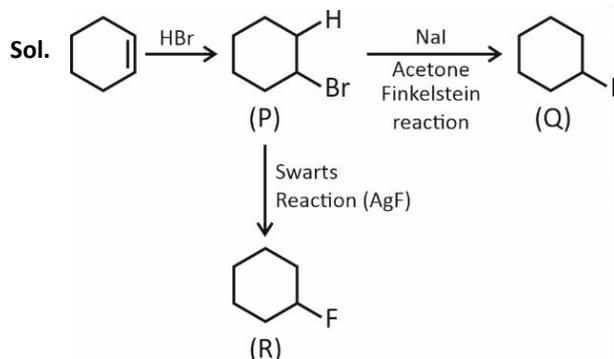
7. For the reaction sequence given below, the correct statement(s) is(are)



(In the options, X is any atom other than carbon and hydrogen, and it is different in P, Q and R)

- (A) C-X bond length in P, Q and R follows the order  $Q > R > P$ .
- (B) C-X bond enthalpy in P, Q and R follows the order  $R > P > Q$ .
- (C) Relative reactivity toward  $S_N2$  reaction in P, Q and R follows the order  $P > R > Q$ .
- (D)  $pK_a$  value of the conjugate acids of the leaving groups in P, Q and R follows the order  $R > Q > P$ .

Answer (B)



- (A) Bond length order  $C-F < C-Br < C-I$   
 $R < P < Q$
- (B) Bond enthalpy  $\Rightarrow R > P > Q$
- (C) Reactivity towards  $S_N2$   $C-I > C-Br > C-F$   
 $Q > P > R$
- (D) Leaving group
- |                |                     |                                      |                    |
|----------------|---------------------|--------------------------------------|--------------------|
|                | P                   | Q                                    | R                  |
|                | $\text{Br}^\ominus$ | $\text{I}^\ominus$                   | $\text{F}^\ominus$ |
| Conjugate acid | HBr                 | HI                                   | HF                 |
| $pK_a$ order   |                     | $\text{HI} < \text{HBr} < \text{HF}$ |                    |
|                |                     | $Q < P < R$                          |                    |

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## SECTION 3 (Maximum Marks : 24)

- This section contains **SIX (06)** questions.
- The answer to each question is a **NUMERICAL VALUE**.
- For each question, enter the correct numerical value of the answer using the mouse and the onscreen virtual numeric keypad in the place designated to enter the answer.
- If the numerical value has more than two decimal places, **truncate/round-off** the value to **TWO** decimal places.
- Answer to each question will be evaluated **according to the following marking scheme**:

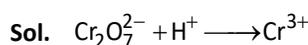
**Full Marks** : +4 If ONLY the correct numerical value is entered in the designated place;

**Zero Marks** : 0 In all other cases.

8. In an electrochemical cell, dichromate ions in aqueous acidic medium are reduced to  $\text{Cr}^{3+}$ . The current (in amperes) that flows through the cell for 48.25 minutes to produce 1 mole of  $\text{Cr}^{3+}$  is \_\_\_\_\_.

**Use:** 1 Faraday =  $96500 \text{ C mol}^{-1}$

**Answer (100.00)**



g eq of  $\text{Cr}^{3+}$  produced = Faraday of charge passed

$$\text{Number of Moles} \times n\text{-factor} = \frac{i \times t}{96500}$$

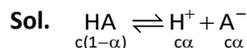
$$1 \times 3 = \frac{i \times 2895}{96500}$$

$$i = 100 \text{ A}$$

9. At  $25^\circ\text{C}$ , the concentration of  $\text{H}^+$  ions in  $1.00 \times 10^{-3} \text{ M}$  aqueous solution of a weak monobasic acid having acid dissociation constant ( $K_a$ ) of  $4.00 \times 10^{-11}$  is  $X \times 10^{-7} \text{ M}$ . The value of X is \_\_\_\_\_.

**Use:** Ionic product of water ( $K_w$ ) =  $1.00 \times 10^{-14}$  at  $25^\circ\text{C}$

**Answer (02.24)**



$$K_a = \frac{c\alpha^2}{1-\alpha}$$

$$\text{H}^+_{\text{total}} = \sqrt{K_{a1}c_1 + K_{a2}c_2 + K_w}$$

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SHREYAS LOHIYA AIR 6 100 Maths	KUSHAGRA BAINGAHA AIR 7 100 Physics	HARSH A GUPTA AIR 15 100 Physics	HARSH JHA AIR 23 100 Physics	DEVYA RUSTAGI AIR 28 100 Maths	AMOGH BANSAL AIR 29 100 Physics
SARVESH ANAND S AIR 42 100 Maths	KRISHNA AGRAWAL AIR 48 100 Physics	DISHAANTH BASU AIR 50 100 Physics	YASH KUMAR AIR 76 100 Physics	ADITYA KUMAR AIR 79 100 Physics	GURURAJ S SAJJAN AIR 92 100 Physics

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$$\begin{aligned} H^+_{\text{total}} &= \sqrt{(4 \times 10^{-11} \times 10^{-3}) + 1 \times 10^{-14}} \\ &= \sqrt{4 \times 10^{-14} + 10^{-14}} \\ &= \sqrt{5 \times 10^{-14}} \\ &= \sqrt{5} \times 10^{-7} \\ &= 2.236 \times 10^{-7} \\ X &= 2.24 \end{aligned}$$

10. Molar volume ( $V_m$ ) of a van der Waals gas can be calculated by expressing the van der Waals equation as a cubic equation with  $V_m$  as the variable. The ratio (in  $\text{mol dm}^{-3}$ ) of the coefficient of  $V_m^2$  to the coefficient of  $V_m$  for a gas having van der Waals constants  $a = 6.0 \text{ dm}^6 \text{ atm mol}^{-2}$  and  $b = 0.060 \text{ dm}^3 \text{ mol}^{-1}$  at 300 K and 300 atm is \_\_\_\_\_.

Use: Universal gas constant ( $R$ ) =  $0.082 \text{ dm}^3 \text{ atm mol}^{-1} \text{ K}^{-1}$

Answer (–07.10)

Sol.  $\left(P + \frac{a}{V_m^2}\right)(V_m - b) = RT$

$$PV_m^3 - PbV_m^2 - RTV_m^2 + aV_m - ab = 0$$

$$V_m^3 - \left(b + \frac{RT}{P}\right)V_m^2 + \frac{aV_m}{P} - \frac{ab}{P} = 0$$

$$\frac{\text{Coefficient of } V_m^2}{\text{Coefficient of } V_m} = \frac{-\left(b + \frac{RT}{P}\right)}{+\frac{a}{P}}$$

$$= -\left(\frac{bP + RT}{a}\right)$$

$$= -\left(\frac{0.06 \times 300 + 0.082 \times 300}{a}\right)$$

$$= -\left(\frac{18 + 24.6}{6}\right) = -\frac{42.6}{6} = -7.1$$

Answer : –7.10

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<b>SHREYAS LOHIYA</b> AIR 6 100 Overall	<b>KUSHAGRA BAINGAHA</b> AIR 7 100 Overall	<b>HARSH A GUPTA</b> AIR 15 100 Overall	<b>HARSH JHA</b> AIR 23 100 Overall	<b>DEVYA RUSTAGI</b> AIR 28 100 Overall	<b>AMOGH BANSAL</b> AIR 29 100 Overall
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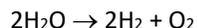
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11. Considering ideal gas behavior, the expansion work done (in kJ) when 144 g of water is electrolyzed completely under constant pressure at 300 K is \_\_\_\_\_.

**Use:** Universal gas constant (R) = 8.3 J K<sup>-1</sup> mol<sup>-1</sup>; Atomic mass (in amu): H = 1, O = 16

**Answer (29.88)**

**Sol.** Number of moles of H<sub>2</sub>O =  $\frac{144}{18} = 8$  moles



2 moles water → 3 moles of gases

8 moles water → 12 moles of gases

$$\text{Volume of gases} = \frac{12 \times R \times 300}{P} \text{ m}^3$$

$$\text{Work done} = -P_{\text{ext}} \Delta V$$

$$= -P_{\text{ext}} \times \left[ \frac{12 \times 8.3 \times 300}{P} - 0 \right]$$

$$= -29880 \text{ J}$$

$$= -29.88 \text{ kJ}$$

**Ans. 29.88**

12. The monomer (X) involved in the synthesis of Nylon 6,6 gives positive carbylamine test. If 10 moles of X are analyzed using Dumas method, the amount (in grams) of nitrogen gas evolved is \_\_\_\_\_.

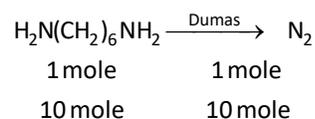
**Use:** Atomic mass of N (in amu) = 14

**Answer (280.00)**

**Sol.** Monomer of Nylon 6,6 ⇒ Adipic acid

+  
hexamethylene diamine

↓  
+ve carbylamine test



Mass of N<sub>2</sub> formed = 10 × 28 = 280 g

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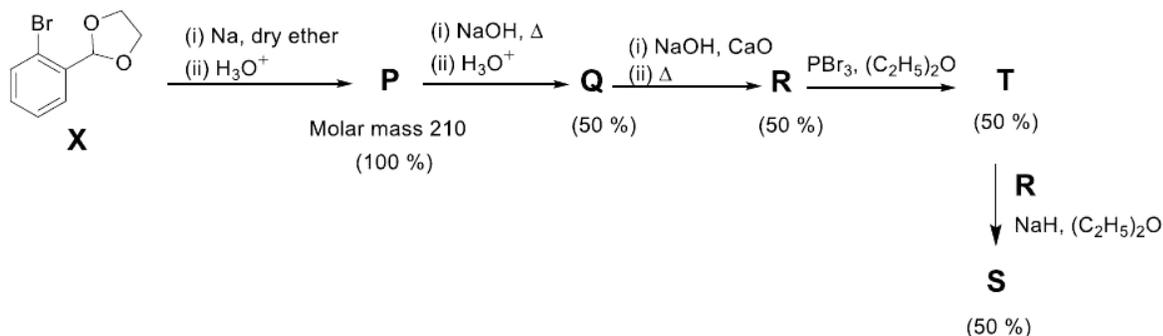
<b>SHREYAS LOHIYA</b> AIR 6 100 Overall	<b>KUSHAGRA BAINGAHA</b> AIR 7 100 Overall	<b>HARSH A GUPTA</b> AIR 15 100 Overall	<b>HARSH JHA</b> AIR 23 100 Overall	<b>DEVYA RUSTAGI</b> AIR 28 100 Overall	<b>AMOGH BANSAL</b> AIR 29 100 Overall
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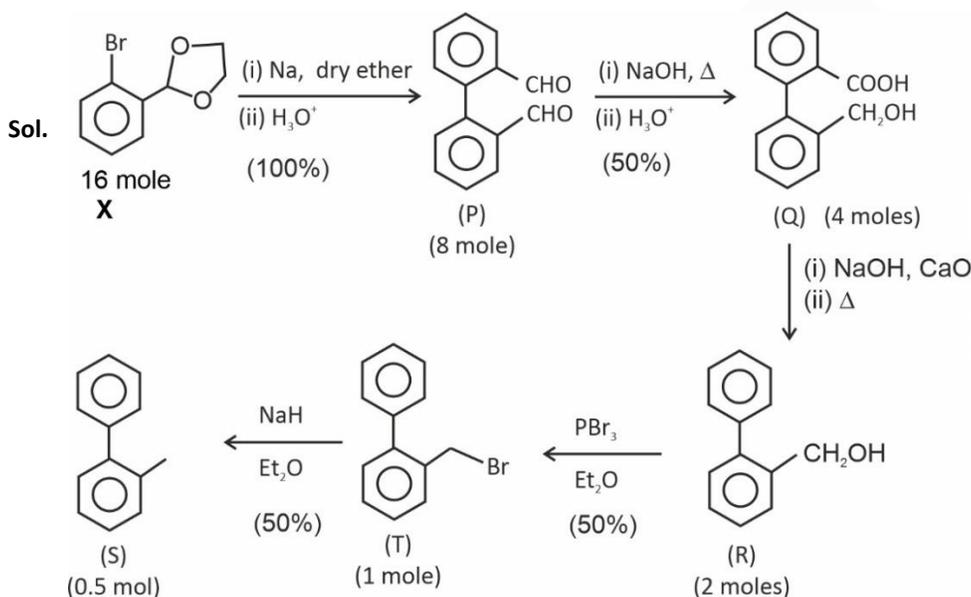
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13. The reaction sequence given below is carried out with 16 moles of X. The yield of the major product in each step is given below the product in parentheses. The amount (in grams) of S produced is \_\_\_\_\_.

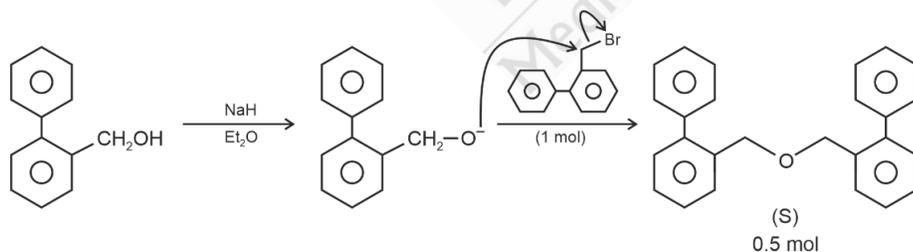


Use: Atomic mass (in amu): H = 1, C = 12, O = 16, Br = 80

Answer (175.00)



When NaH is added, it reacts with R



The amount of S formed =  $0.5 \times 350 \text{ g} = 175 \text{ g}$

**Aakashians Rise High in JEE (Main) 2025**

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## SECTION 4 (Maximum Marks : 12)

- This section contains **THREE (03)** Matching List Sets.
- Each set has **ONE** Multiple Choice Question.
- Each set has **TWO** lists: **List-I** and **List-II**.
- List-I** has **Four** entries (P), (Q), (R) and (S) and **List-II** has **Five** entries (1), (2), (3), (4) and (5).
- FOUR** options are given in each Multiple Choice Question based on **List-I** and **List-II** and **ONLY ONE** of these four options satisfies the condition asked in the Multiple Choice Question.
- Answer to each question will be evaluated **according to the following marking scheme:**

**Full Marks** : +4 **ONLY** if the option corresponding to the correct combination is chosen;

**Zero Marks** : 0 If none of the options is chosen (i.e. the question is unanswered);

**Negative Marks** : -1 In all other cases.

14. The correct match of the group reagents in **List-I** for precipitating the metal ion given in **List-II** from solutions, is

	List-I		List-II
(P)	Passing $H_2S$ in the presence of $NH_4OH$	(1)	$Cu^{2+}$
(Q)	$(NH_4)_2CO_3$ in the presence of $NH_4OH$	(2)	$Al^{3+}$
(R)	$NH_4OH$ in the presence of $NH_4Cl$	(3)	$Mn^{2+}$
(S)	Passing $H_2S$ in the presence of dilute $HCl$	(4)	$Ba^{2+}$
		(5)	$Mg^{2+}$

(A)  $P \rightarrow 3; Q \rightarrow 4; R \rightarrow 2; S \rightarrow 1$

(B)  $P \rightarrow 4; Q \rightarrow 2; R \rightarrow 3; S \rightarrow 1$

(C)  $P \rightarrow 3; Q \rightarrow 4; R \rightarrow 1; S \rightarrow 5$

(D)  $P \rightarrow 5; Q \rightarrow 3; R \rightarrow 2; S \rightarrow 4$

**Answer (A)**

**Sol.** Passing  $H_2S$  in the presence of  $NH_4OH$  is group reagent for Group IV cations - $Mn^{2+}$

$NH_4OH$  in the presence of  $NH_4Cl$  is group reagent for Group III cations - $Al^{3+}$

Passing  $H_2S$  in the presence of  $HCl$  is Group reagent for group II cations - $Cu^{2+}$

$(NH_4)_2CO_3$  in the presence of  $NH_4OH$  is used for detection of  $Ba^{2+}$

$P \rightarrow 3; Q \rightarrow 4; R \rightarrow 2; S \rightarrow 1$

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<b>SARVESH ANAND S</b> AIR 42 <small>100 Maths</small>	<b>KRISHNA AGRAWAL</b> AIR 48 <small>100 Physics</small>	<b>DISHAANTH BASU</b> AIR 50 <small>100 Physics</small>	<b>YASH KUMAR</b> AIR 76 <small>100 Physics</small>	<b>ADITYA KUMAR</b> AIR 79 <small>100 Physics</small>	<b>GURURAJ S SAJJAN</b> AIR 92 <small>and many more...</small>

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15. The major products obtained from the reactions in List-II are the reactants for the named reactions mentioned in List-I. Match each entry in List-I with the appropriate entry in List-II and choose the correct option.

	List-I		List-II
(P)	Stephen reaction	(1)	Toluene $\xrightarrow[\text{(ii) H}_3\text{O}^+]{\text{(i) CrO}_2\text{Cl}_2/\text{CS}_2}$
(Q)	Sandmeyer reaction	(2)	Benzoic acid $\xrightarrow[\text{(iii) P}_4\text{O}_{10}, \Delta]{\text{(i) PCl}_5, \text{(ii) NH}_3}$
(R)	Hoffmann bromamide degradation reaction	(3)	Nitrobenzene $\xrightarrow[\text{(273-278 K), H}_2\text{O}]{\text{(i) Fe, HCl, (ii) HCl, NaNO}_2}$
(S)	Cannizzaro reaction	(4)	Toluene $\xrightarrow[\text{(iv) NH}_3]{\text{(i) Cl}_2/h\nu, \text{H}_2\text{O}, \text{(ii) Tollen's reagent, (iii) SO}_2\text{Cl}_2}$
		(5)	Aniline $\xrightarrow[\text{(iii) aq. NaOH}]{\text{(i) (CH}_3\text{CO)}_2\text{O, Pyridine, (ii) HNO}_3, \text{H}_2\text{SO}_4, 288 \text{ K}}$

(A) P → 2; Q → 4; R → 1; S → 3

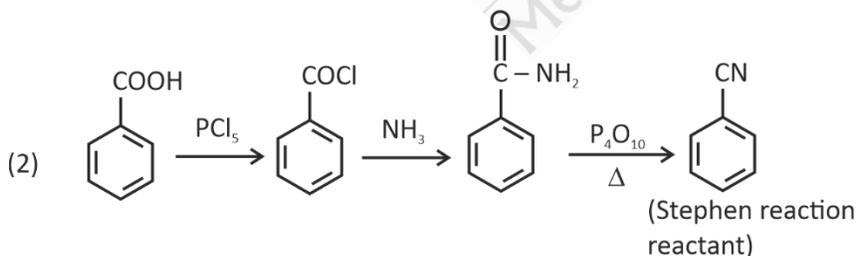
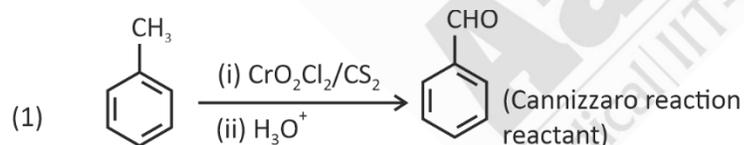
(B) P → 2; Q → 3; R → 4; S → 1

(C) P → 5; Q → 3; R → 4; S → 2

(D) P → 5; Q → 4; R → 2; S → 1

Answer (B)

Sol.



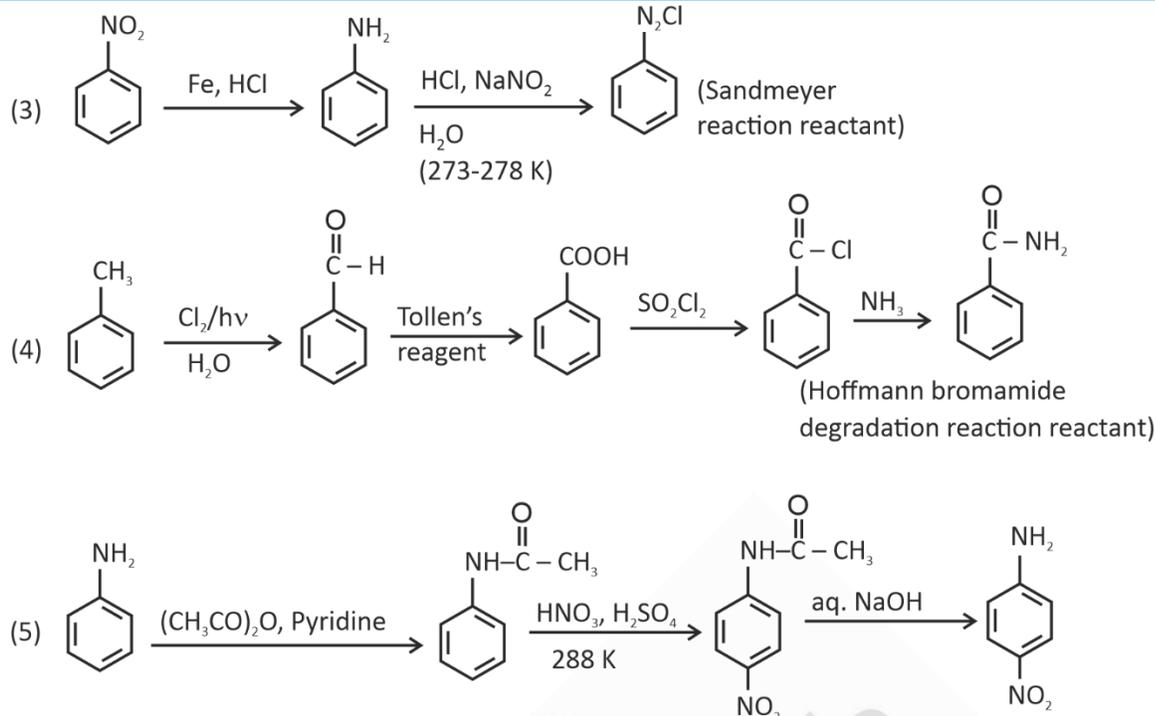
**Aakashians Rise High in JEE (Main) 2025**

<b>SHREYAS LOHIYA</b> AIR 6 100 All India Topper	<b>KUSHAGRA BAINGAHA</b> AIR 7 100 All India Topper	<b>HARSH A GUPTA</b> AIR 15 100 All India Topper	<b>HARSH JHA</b> AIR 23 100 All India Topper	<b>DEVYA RUSTAGI</b> AIR 28 100 All India Topper	<b>AMOGH BANSAL</b> AIR 29 100 All India Topper
<b>SARVESH ANAND S</b> AIR 42 100 All India Topper	<b>KRISHNA AGRAWAL</b> AIR 48 100 All India Topper	<b>DISHAANTH BASU</b> AIR 50 100 All India Topper	<b>YASH KUMAR</b> AIR 76 100 All India Topper	<b>ADITYA KUMAR</b> AIR 79 100 All India Topper	<b>GURURAJ S SAJJAN</b> AIR 92 100 All India Topper

\*Aakash Invicta Contact Program

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16. Match the compounds in List-I with the appropriate observations in List-II and choose the correct option.

	List-I		List-II
(P)	<chem>OC(=O)C(N)Cc1ccc(O)cc1</chem>	(1)	Reaction with phenyl diazonium salt gives yellow dye.
(Q)	<chem>CC(=O)Nc1ccccc1C(=O)Nc2cc(C)cc(C)cc2</chem>	(2)	Reaction with ninhydrin gives purple color and it also reacts with FeCl <sub>3</sub> to give violet color.
(R)	<chem>[NH3+][Cl-]c1ccccc1</chem>	(3)	Reaction with glucose will give corresponding hydrazone.

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<b>SARVESH ANAND S</b> AIR 42 100 Maths	<b>KRISHNA AGRAWAL</b> AIR 48 100 Physics	<b>DISHAANTH BASU</b> AIR 50 100 Physics	<b>YASH KUMAR</b> AIR 76 100 Physics	<b>ADITYA KUMAR</b> AIR 79 100 Physics	<b>GURURAJ S SAJJAN</b> AIR 92 100 Physics

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(S)		(4)	Lassaigne extract of the compound treated with dilute HCl followed by addition of aqueous FeCl <sub>3</sub> gives blood red color.
		(5)	After complete hydrolysis, it will give ninhydrin test and it <b>DOES NOT</b> give positive phthalein dye test.

(A) P → 1; Q → 5; R → 4; S → 2

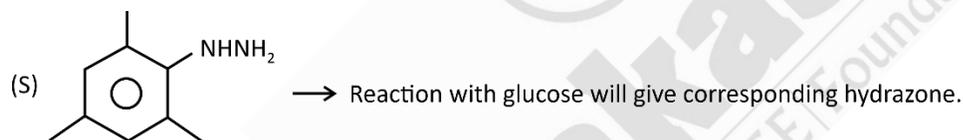
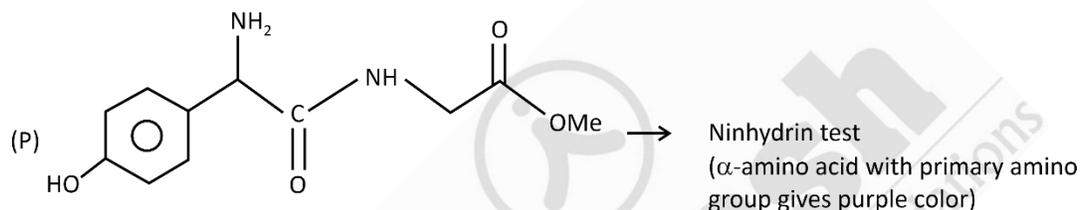
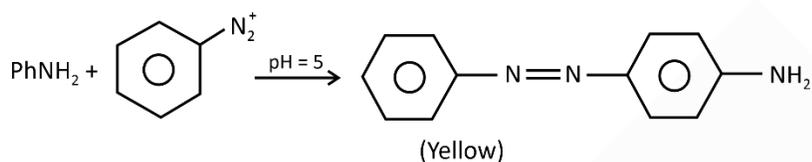
(B) P → 2; Q → 5; R → 1; S → 3

(C) P → 5; Q → 2; R → 1; S → 4

(D) P → 2; Q → 1; R → 5; S → 3

**Answer (B)**

**Sol.**



□ □ □

**Aakashians Rise High in JEE (Main) 2025**

<b>SHREYAS LOHIYA</b> AIR 6 100 Physics	<b>KUSHAGRA BAINGAHA</b> AIR 7 100 Physics	<b>HARSSH A GUPTA</b> AIR 15 100 Physics	<b>HARSH JHA</b> AIR 23 100 Physics	<b>DEVYA RUSTAGI</b> AIR 28 100 Maths	<b>AMOGH BANSAL</b> AIR 29 100 Physics
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\*Aakash Invictus Contact Program and many more...

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